

# Methoden moderner Röntgenphysik: Streuung und Abbildung

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Lecture 16	Vorlesung zum Haupt- oder Masterstudiengang Physik, SoSe 2019 G. Grübel, <u>F. Lehmkuhler</u> , L. Müller, O. Seeck, L. Frenzel, M. Martins, W. Wurth		
Location	Lecture hall AP, Physics, Jungiusstraße		
Date	Tuesday	12:30 - 14:00	(starting 2.4.)
	Thursday	8:30 - 10:00	(until 11.7.)



## Soft Matter – Timeline


- Di 07.05.2019 Soft Matter studies I: Methods & experiments  
*Definitions, complex liquids, colloids, storage ring and FEL experiments, setups, liquid jets, ...*
- Do 09.05.2019 Soft Matter studies II: Structure  
*SAXS & WAXS applications, X-ray cross correlations, ...*
- Di 14.05.2019 Soft Matter studies III: Dynamics  
*XPCS applications, diffusion, dynamical heterogeneities, ...*
- Do 16.05.2019 XPCS and XCCA simulation and modelling
- Di 21.05.2019 Case study I: Glass transition  
*Supercooled liquids, glasses vs. crystals, glass transition concepts, structure-dynamics relations, ...*
- Do 23.05.2019 **Case study II: Water**  
*Phase diagram, anomalies, crystalline and glassy forms, FEL studies, ...*



Quick links ▼ Print

# WATER STRUCTURE AND SCIENCE

*Martin Chaplin*



## Water Structure and Science

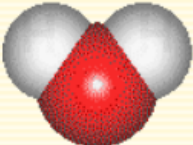
This page forms the entrance to a website concerned with the physical, chemical and biological properties of water.

[Table of Contents](#) | [Site Map](#)

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*Liquid water is not a bit player in the theatre of life — it's the headline act*

Many regard water (H<sub>2</sub>O) as a rather uninteresting substance because it is transparent, odorless, tasteless and ubiquitous. It is the simplest compound of the two most common reactive elements in the universe, consisting of just two hydrogen atoms attached to a single oxygen atom. Indeed, very few molecules are smaller or lighter. Liquid water, however, is the most extraordinary material contradicting its apparently simple molecular constituent. ⇒

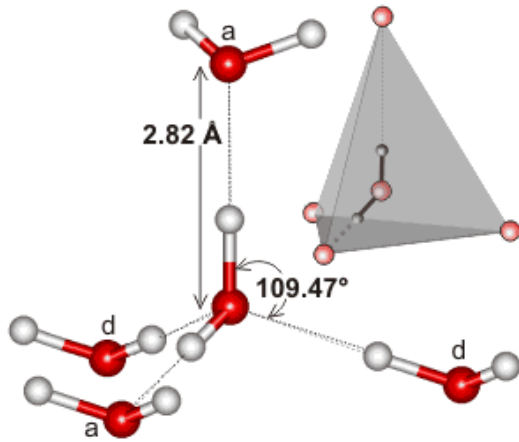


Although we drink it, wash, fish and swim in it, and cook with it (although probably not all at the same time), we nearly always overlook the special relationship it has with our lives. Droughts cause famines and floods cause death and disease. It makes up over about half of us and, without it, we die within a few days. Liquid water has importance as a solvent, a solute, a reactant, a catalyst and a biomolecule, structuring proteins, nucleic acids and cells and controlling our consciousness. H<sub>2</sub>O is the second most common molecule in the Universe (behind hydrogen, H<sub>2</sub>), the most abundant solid material and fundamental to star formation. There is a hundred times as many water molecules in our bodies than the sum of all the other molecules put together. Life cannot evolve or continue without liquid water, which is why there is so much excitement about finding it on Mars and other planets and moons. It is unsurprising that water plays a central role in many of the World's religions. This web site discusses many aspects of water science. ⇒

Water science online: <http://www1.lsbu.ac.uk/water/>



## Why study water?

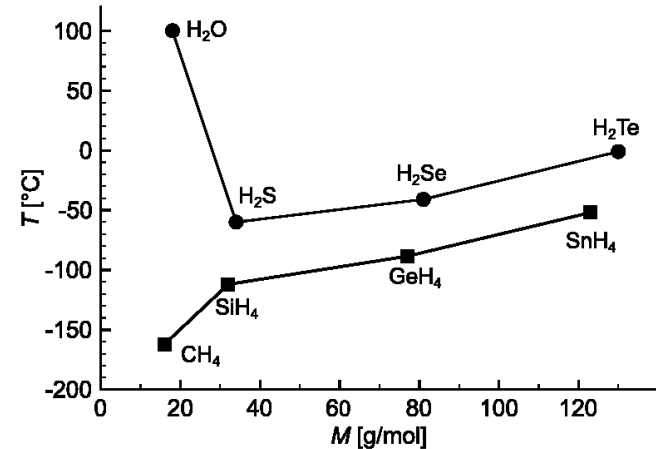
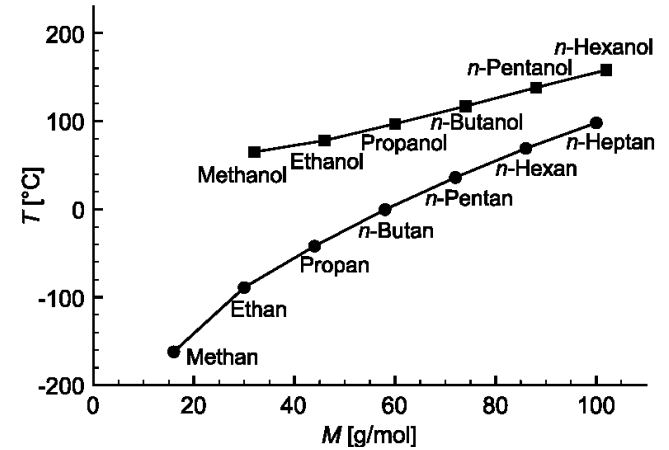
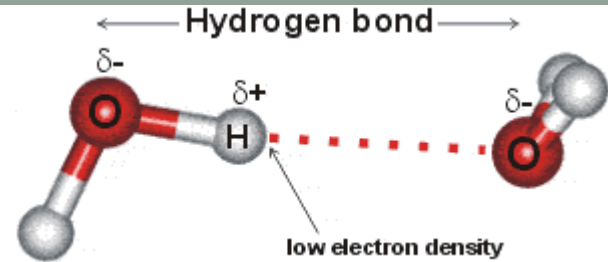


Most important liquid for life (biology), as solvent (chemistry), geo-science, ...

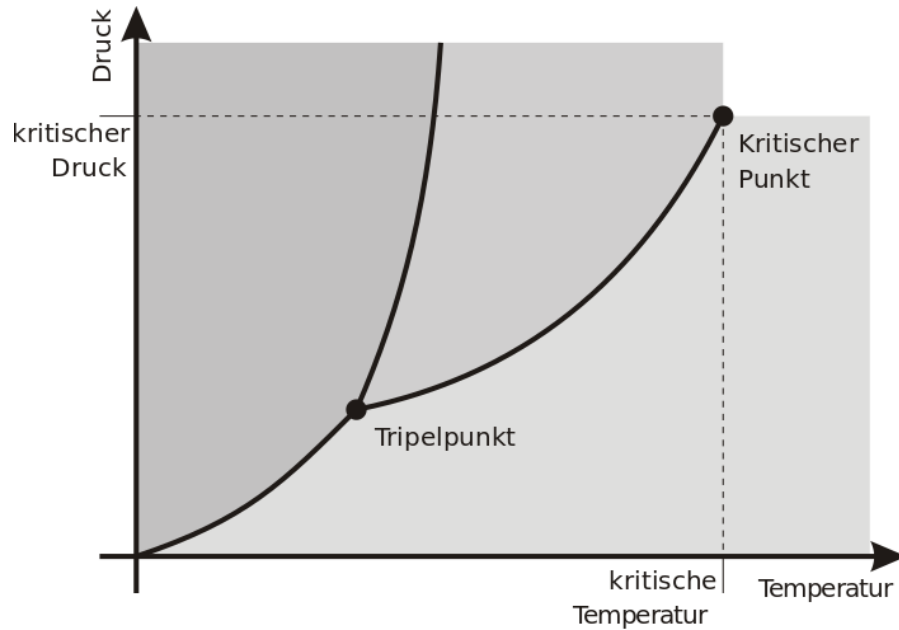
Complex **hydrogen bond** network

- Strength O-H...O: ~21 kJ/mol
- Tetrahedral coordination
- E.g. high boiling points

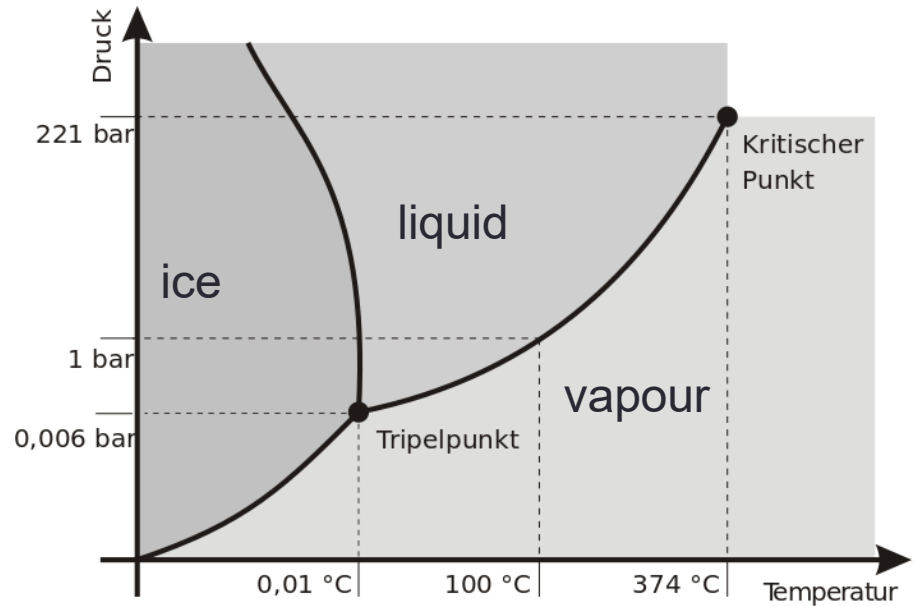
<http://www1.lsbu.ac.uk/water/>



# Water – phase diagram



Normal liquid

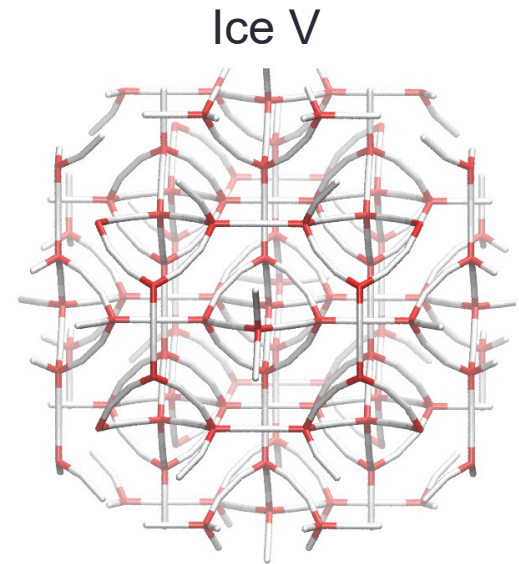
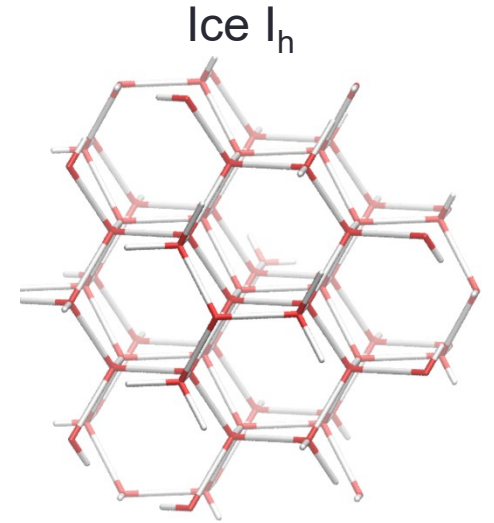
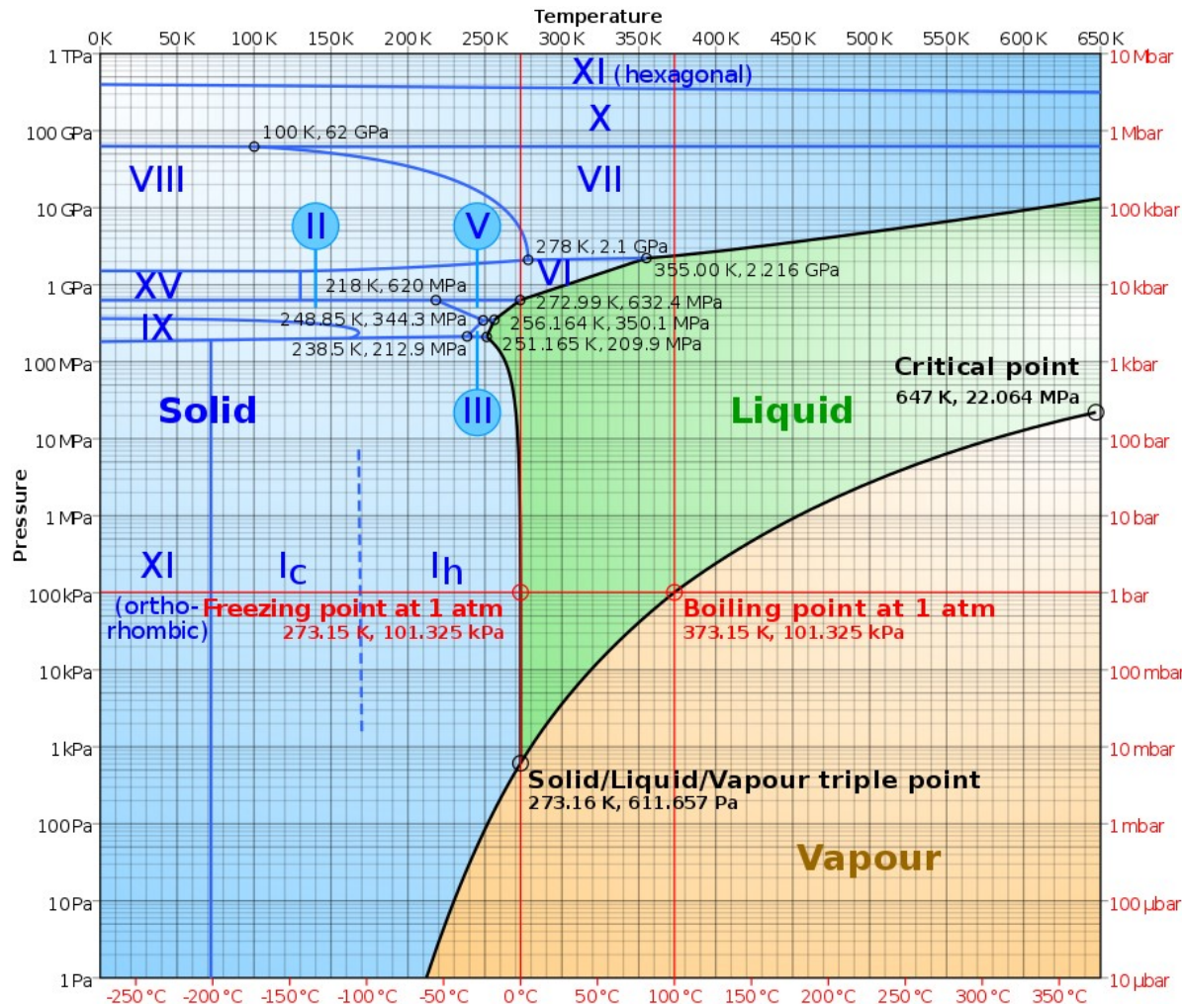


Water  
→ anomalies

Figures: wikipedia

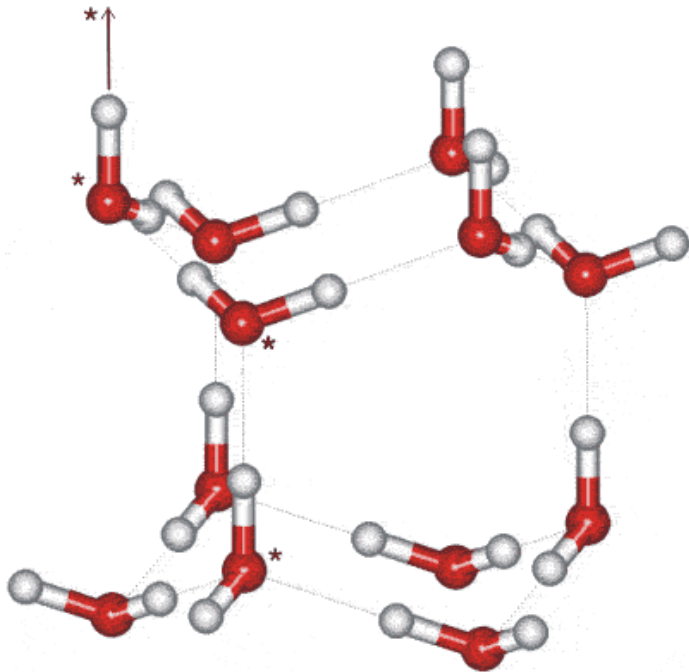


# Crystalline ice – polymorphism



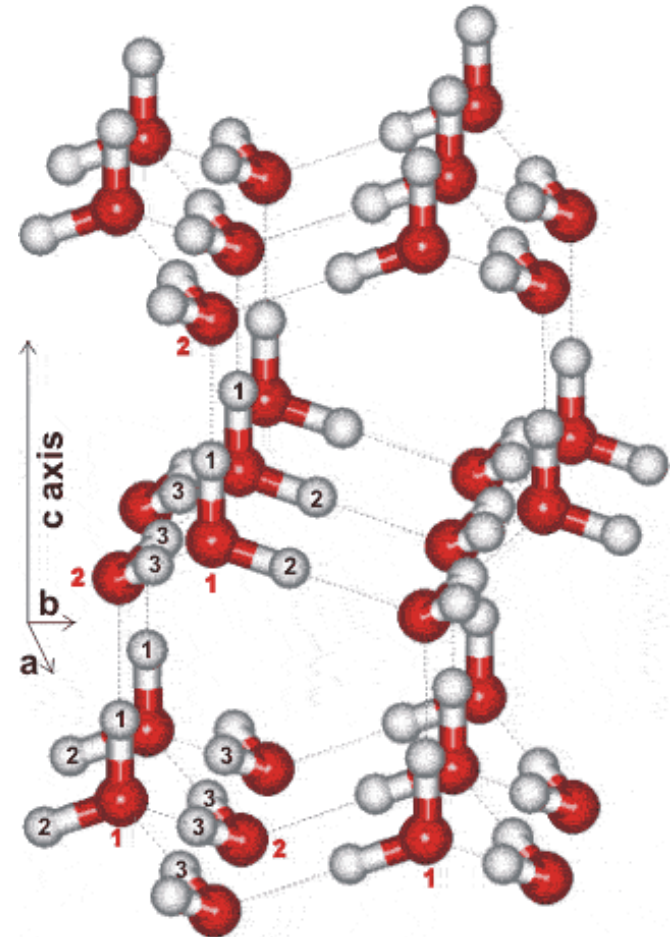
# Crystalline ice – polymorphism

## Hexagonal ice (ice I<sub>h</sub>)



Tetrahedral coordination  
4 H-bonds per molecule

Ice rule: one hydrogen  
between two oxygens

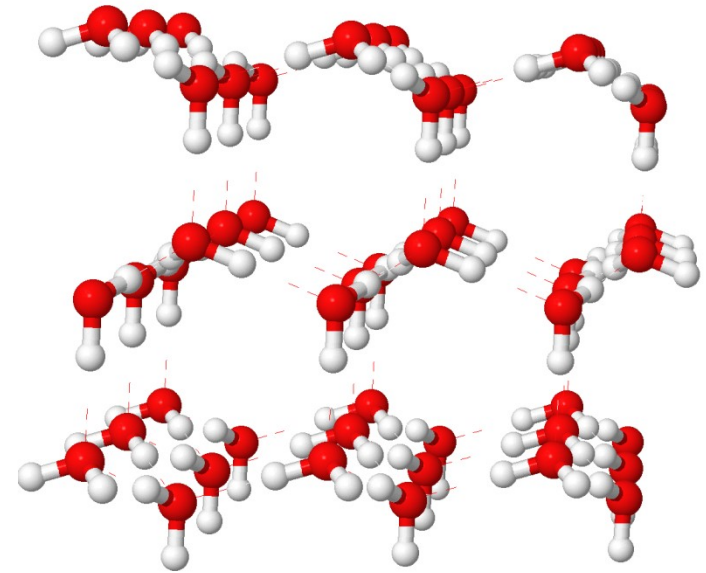


<http://www1.lsbu.ac.uk/water>

## Crystalline ice – polymorphism

There are hydrogen-disordered and hydrogen-ordered ice phases

Disordered phase	Ordered phase	$T_{o \rightarrow d}$
Ih	XI	72 K
III	IX	170 K
VII	VIII	270 K
XII	XIV	100 K
IV	???	-
???	II	-
V	XIII	~120 K
VI	XV	~130 K



Ice XI: hydrogen-ordered form of hexagonal ice  $I_h$



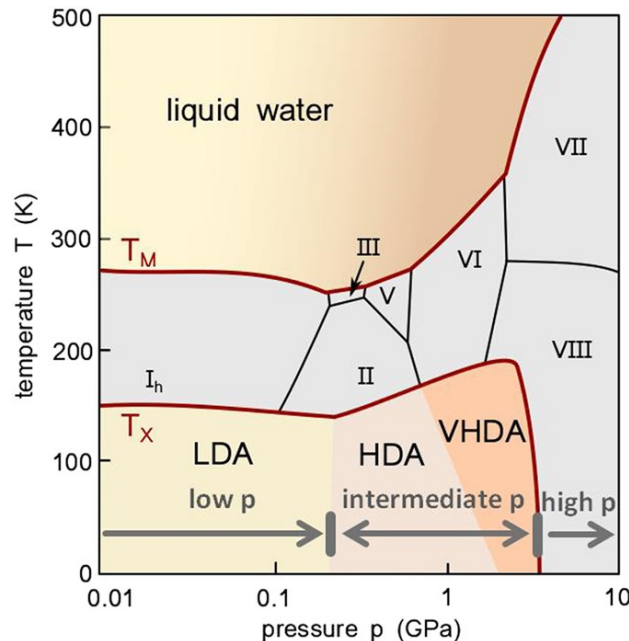
## Amorphous ice

- Earth: hexagonal ice
- Space: amorphous forms of ice

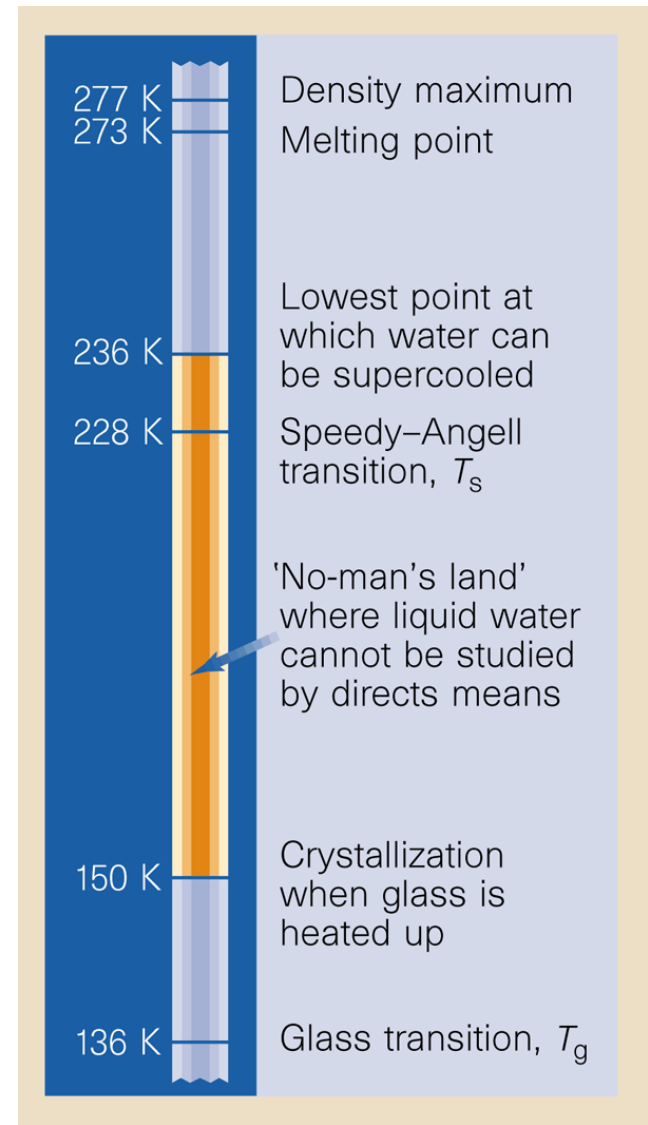
### Three forms of amorphous ice

- Low-density (LDA), 0.92 g/cm<sup>3</sup>
- High-density (HDA), 1.17 g/cm<sup>3</sup>
- Very-high-density (VHDA), 1.26 g/cm<sup>3</sup>

### Glass transition: no man's land



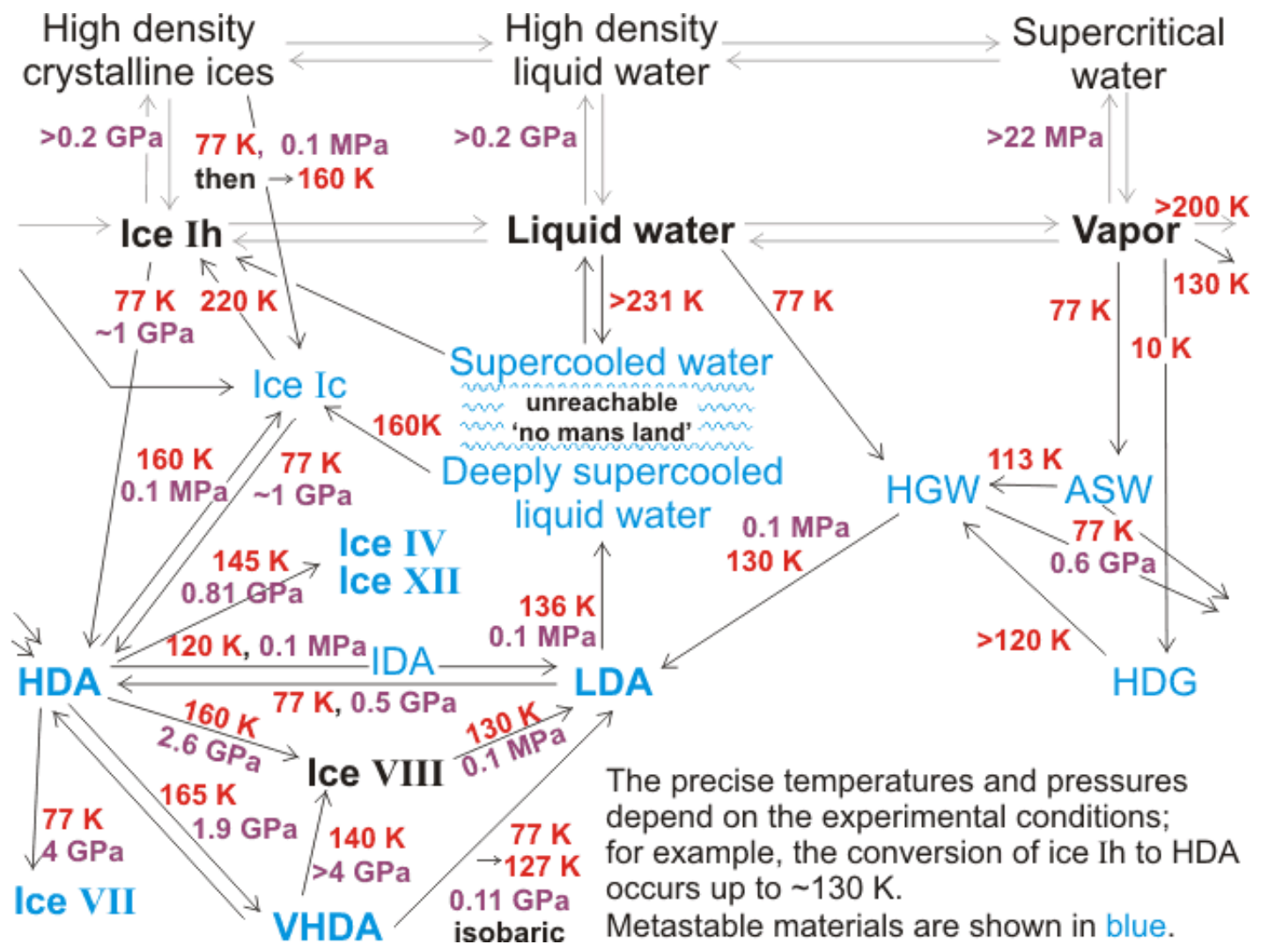
**J. Stern and T. Loerting.**  
**Sci. Rep. 7, 3995 (2017)**



**S. Sastry. Nature 398, 467 (1999)**



# Water – solid states



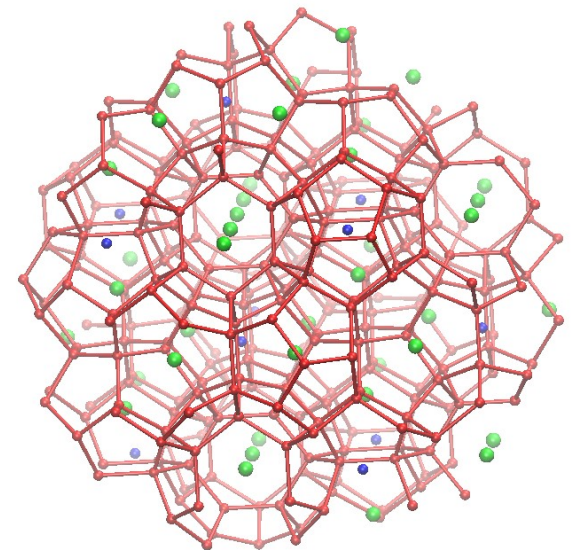
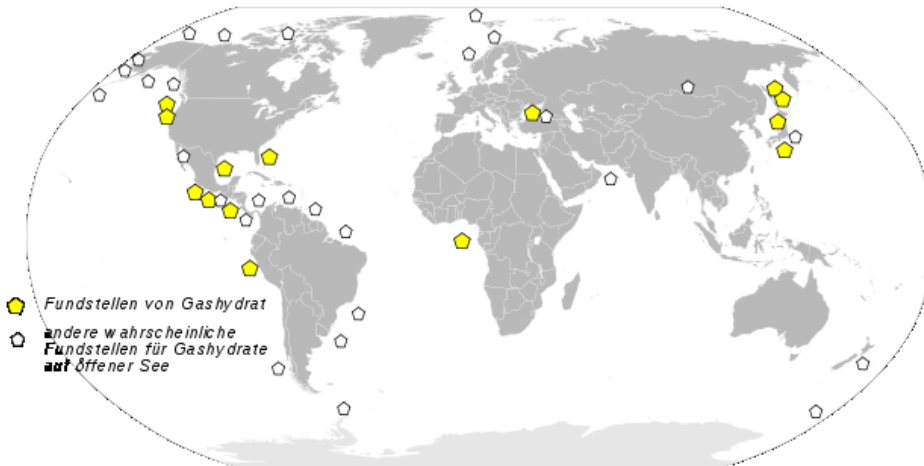
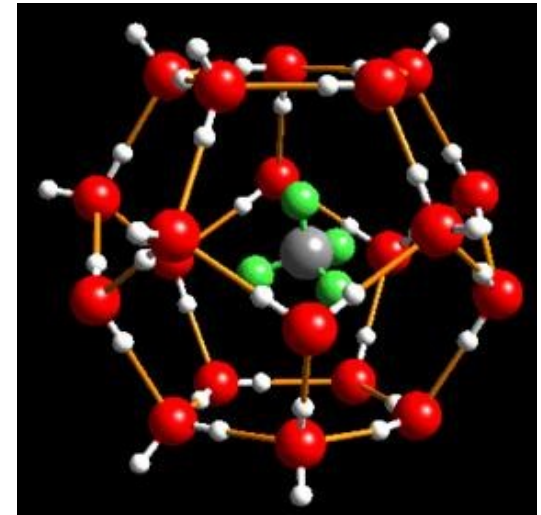
ASW – amorphous solid water

HGW – Hyperquenched glassy water



## Clathrate hydrates

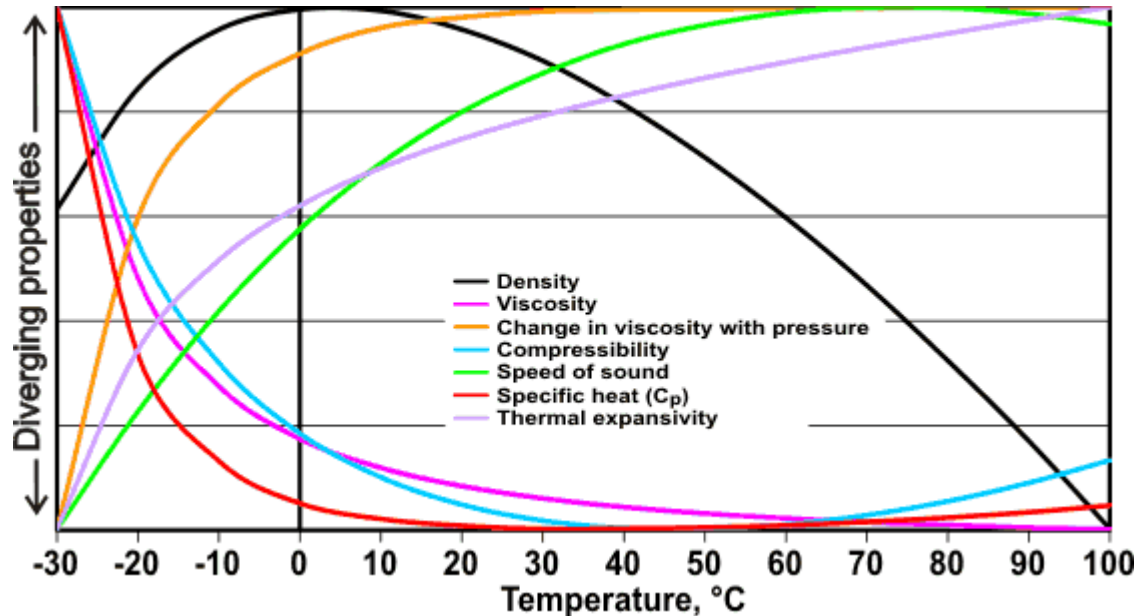
- In presence of gas molecules (e.g. methane,  $\text{CO}_2$ ,  $\text{O}_2$ ,  $\text{H}_2$ , ...) water forms ice-like inclusion compounds
- Typically "more stable" than ice
- Methane hydrate at ocean floor and in permafrost regions



## Water – anomalies

Water shows a large number of anomalous properties compared to "simple liquids", e.g.

- Density anomalies (e.g. well-known highest density at 4°C)
- Phase anomalies (e.g. high boiling point)
- Thermodynamic anomalies (e.g. high heat capacity)
- Physical anomalies (e.g. high surface tension)



→ Complex hydrogen bond network

→ Diverging properties upon supercooling around -45°C

→ Connection to water structure

<http://www1.lsbu.ac.uk/water>

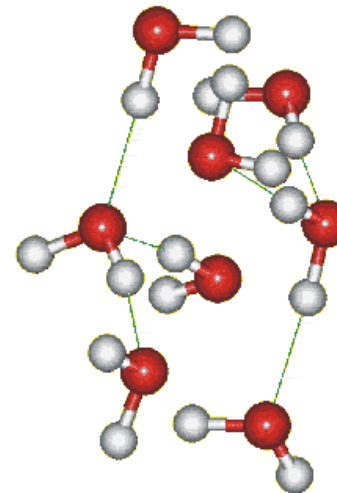
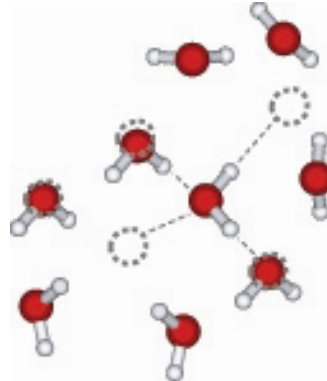
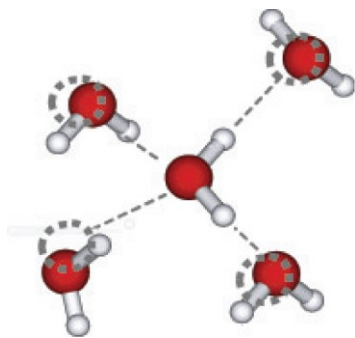
## Liquid water: continuum and mixture models

Long-standing debate: Liquid water as...

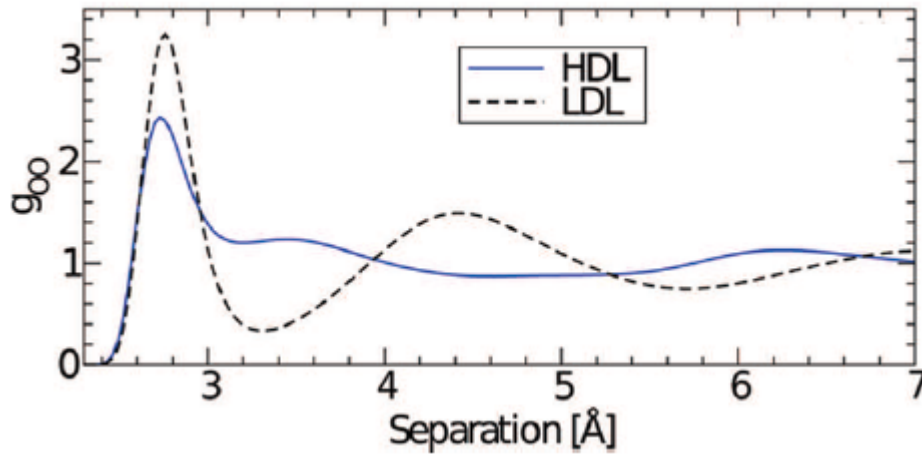
- (1) network of disordered tetrahedrally coordinated molecules with  $\sim 3.5$  hydrogen bonds per molecules
- (2) Mixture of different species with different geometry (goes back to Röntgen 1892 to explain anomalous properties of water)

In more recent years: two-liquids hypothesis

- Low density liquid (LDL): strong tetrahedral coordination
- High density liquid (HDL): broken hydrogen bonds  $\rightarrow$  higher density  
Dominates at room temperature



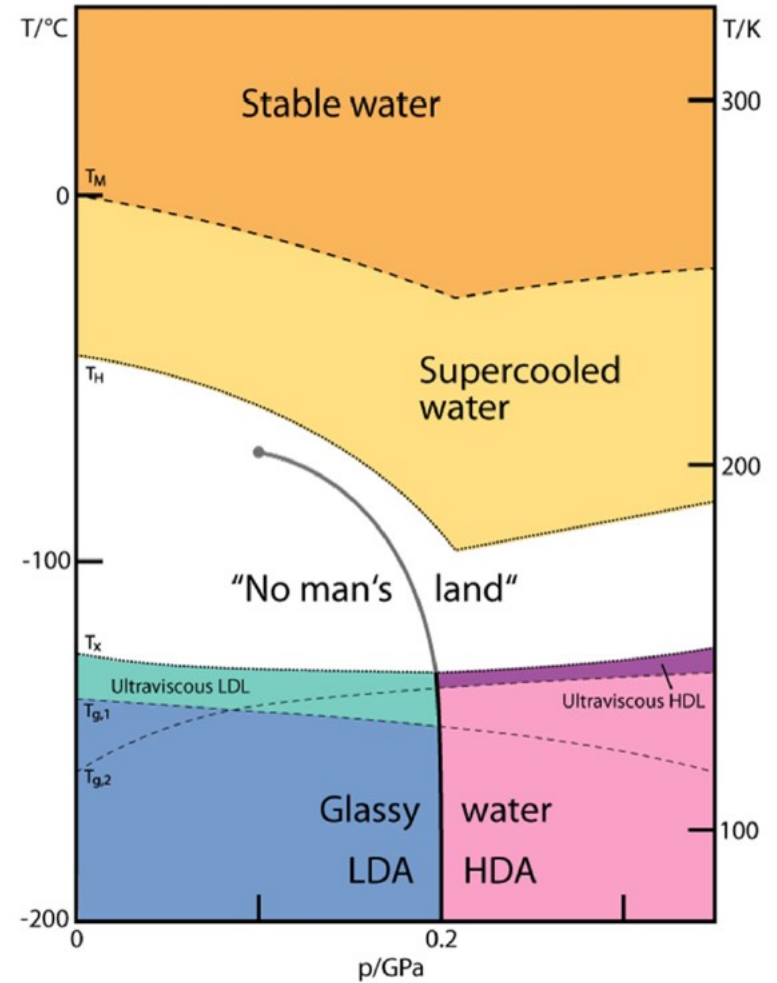
## Liquid water: continuum and mixture models



Molecular dynamics simulations:

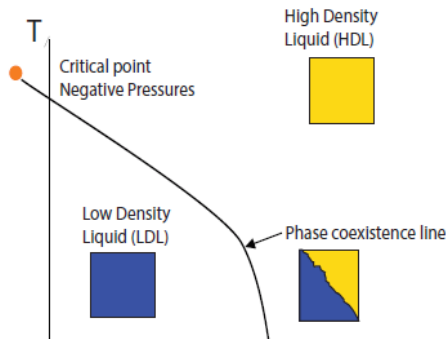
- LDL: tetrahedral liquid
- HDL: broken hydrogen bonds

Phase diagram of amorphous water:  
Reaching "no man's land" to measure HDL/LDL

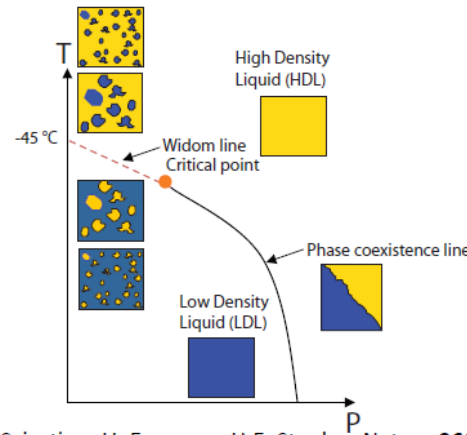


# Liquid water: continuum and mixture models

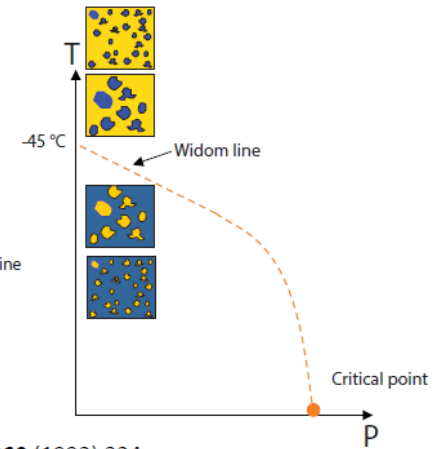
Critical Point Free Model  
Critical Point at -P



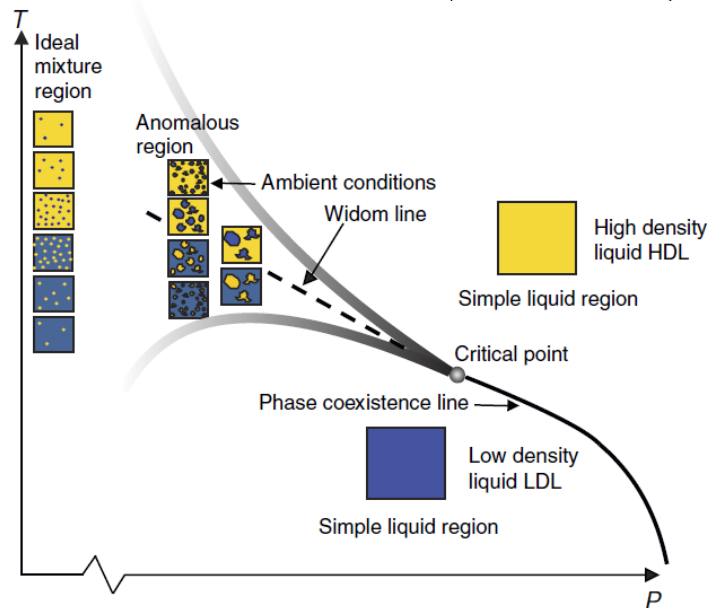
Critical Point Model  
Critical Point at +P



Singularity Free Model  
Critical Point at 0K



P.H. Poole, F. Sciortino, U. Essmann, H.E. Stanley, Nature **360** (1992) 324.



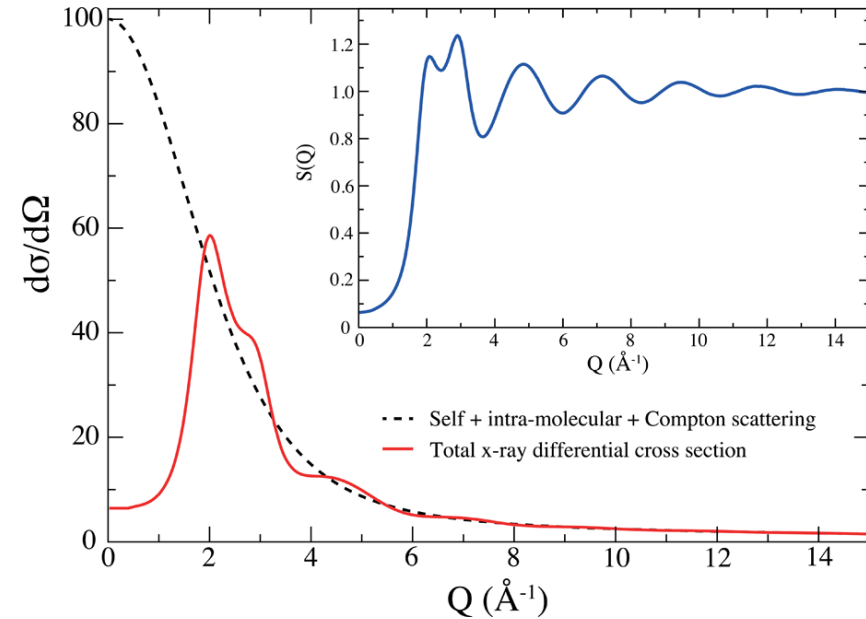
If there are two liquids, will there be a (2nd) critical point?

Widom line: locus of correlation length maxima in the pressure-temperature (P-T) plane. Thermodynamic response functions are expected to have maxima

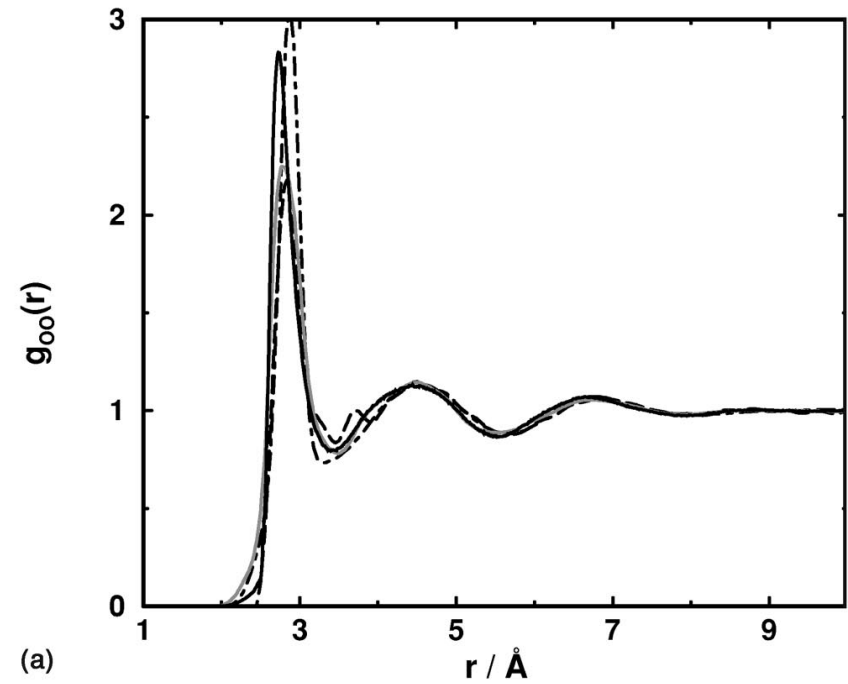
Nat. Comm. 6, 8998 (2015)



## X-ray studies: structure factors



Chem. Rev. 116, 7570 (2016)



(a)

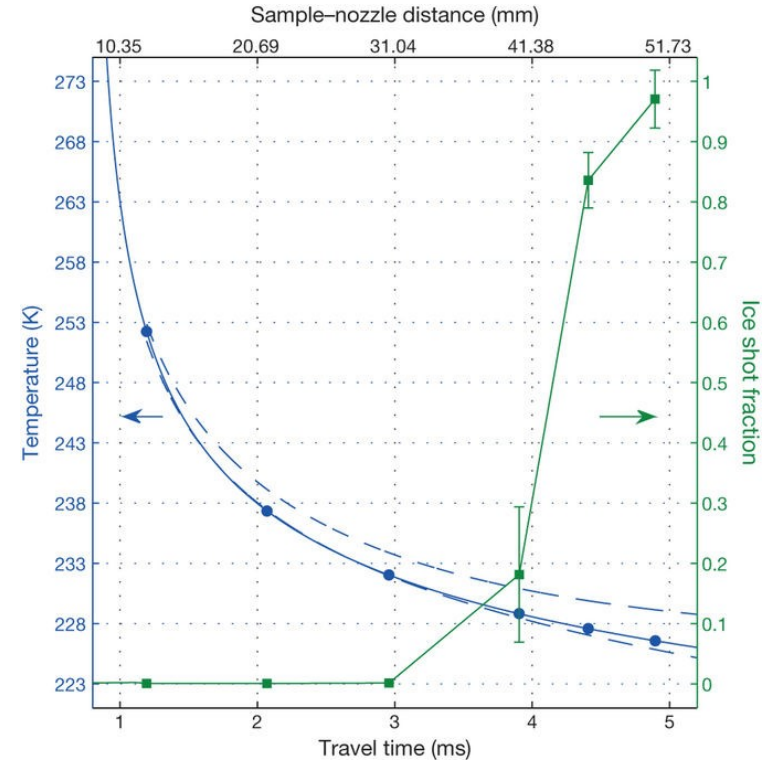
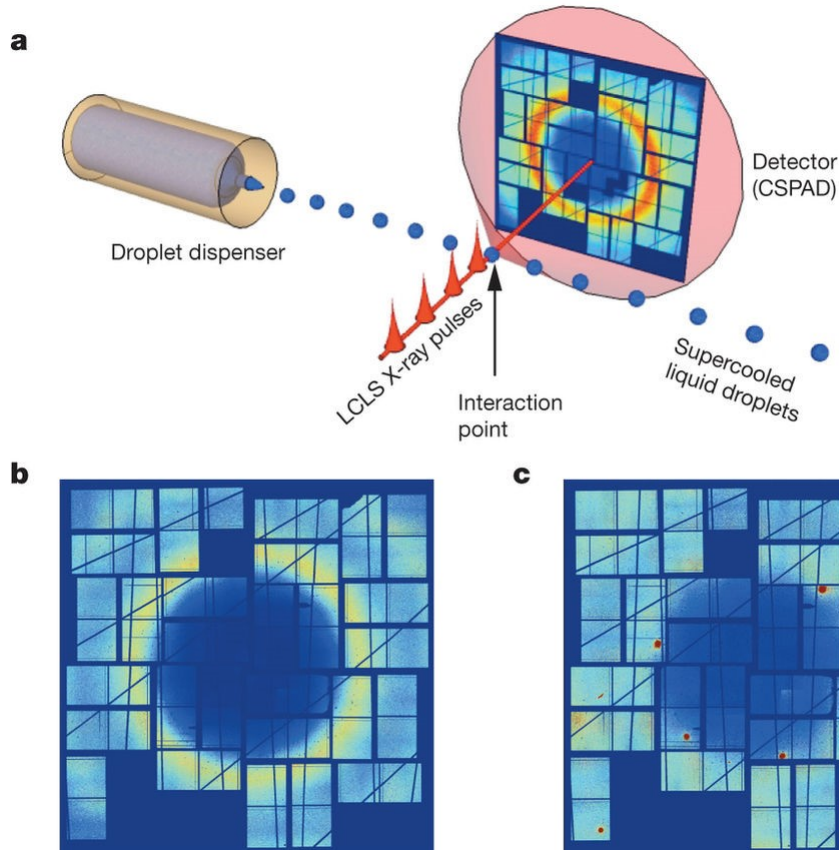
J. Chem. Phys. 113, 9140 (2000)

Structure factor of water around  $q = 2 \text{ \AA}^{-1} \rightarrow$  for 8 keV X-rays  $\rightarrow \theta \approx 29^\circ \rightarrow$  XRD

Experimental limit:  $\theta = 180^\circ \Rightarrow q_{max} = \frac{4\pi}{\lambda} \approx 8 \text{ \AA}^{-1}$  for 8 keV  $\rightarrow$  high-energy X-rays ( $\geq 50$  keV) for pair-distribution function (pdf) studies



# Liquid water: structure factors

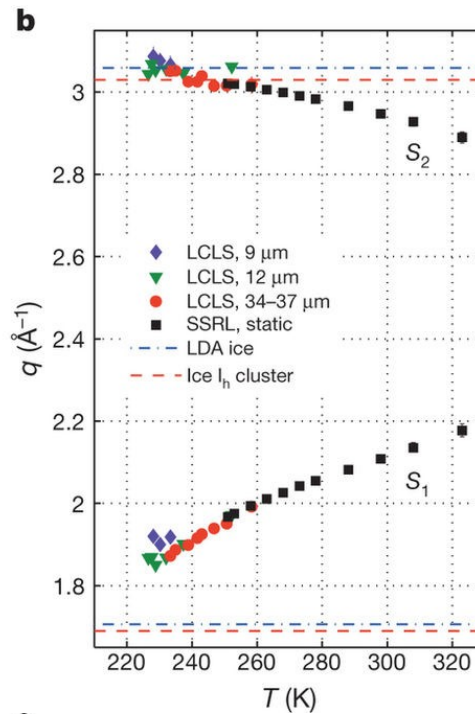
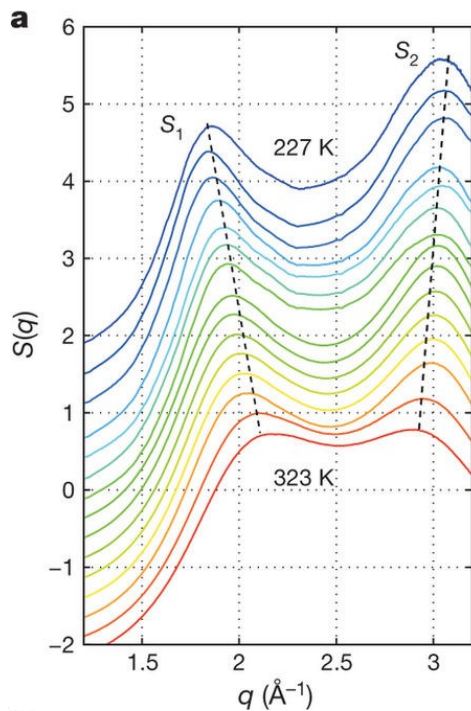


Liquid microdroplets: supercooling due to evaporation in vacuum

Ultrafast probing: FEL (~100 fs)

→ XRD patterns from single droplets

Nature 510, 381 (2014)

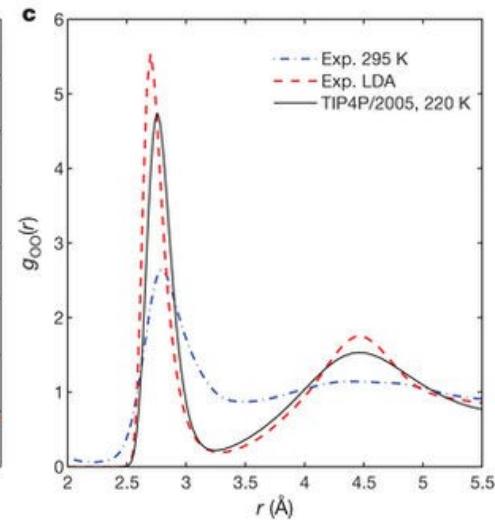
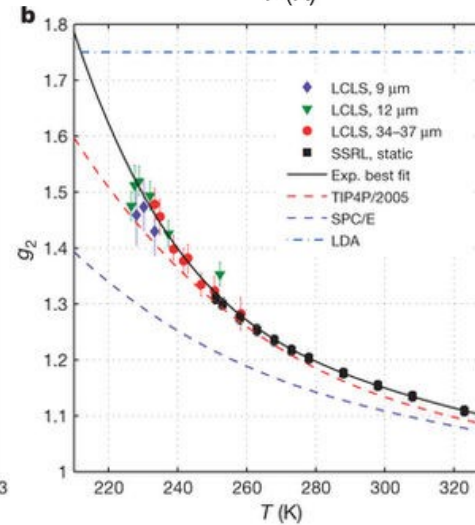
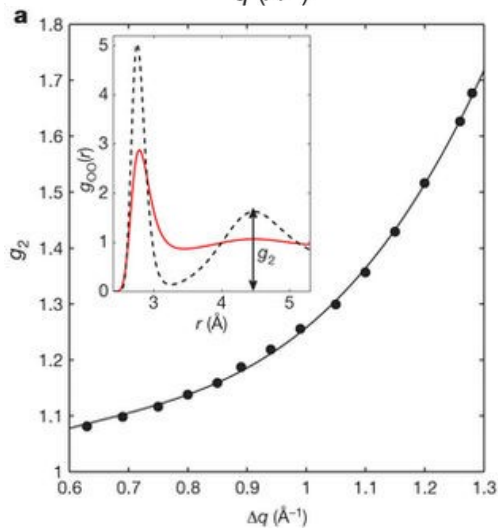


Structure factors: peaks shift upon supercooling

But: here limited to  $q \leq 3.2 \text{ \AA}^{-1}$

Degree of tetrahedrality: 2nd peak of  $g(r)$

Towards low-density liquid water?

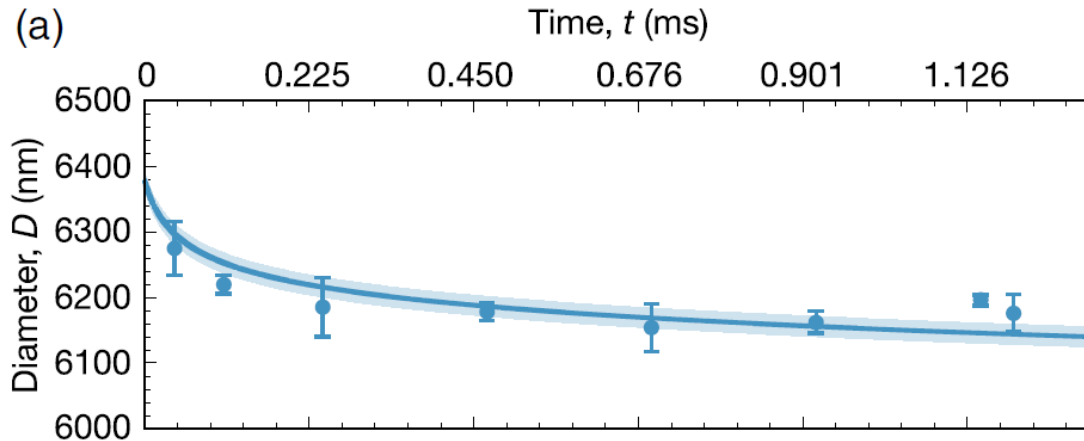


Nature 510, 381 (2014)

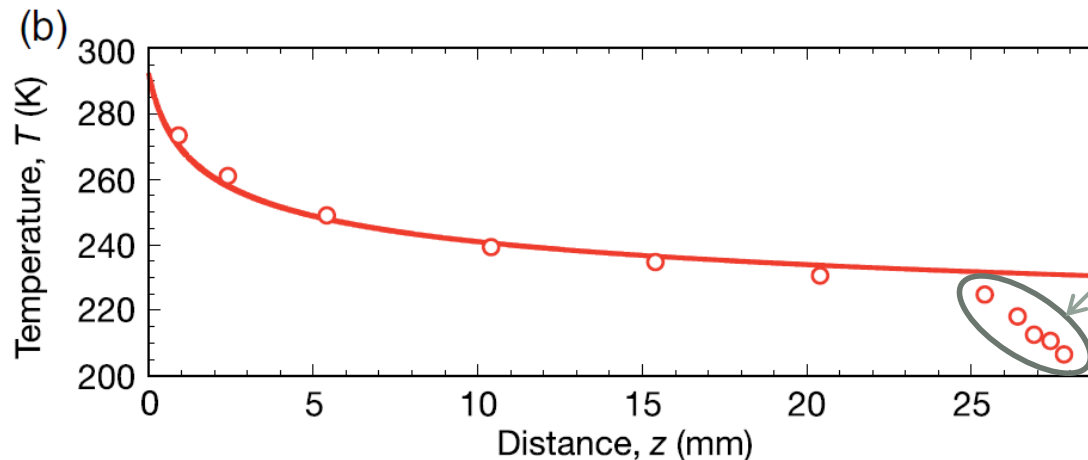


## How to measure temperature of water droplets?

Raman scattering → Interpretation debated



Droplet diameters from vibrational spectroscopy & Knudsen model of evaporation



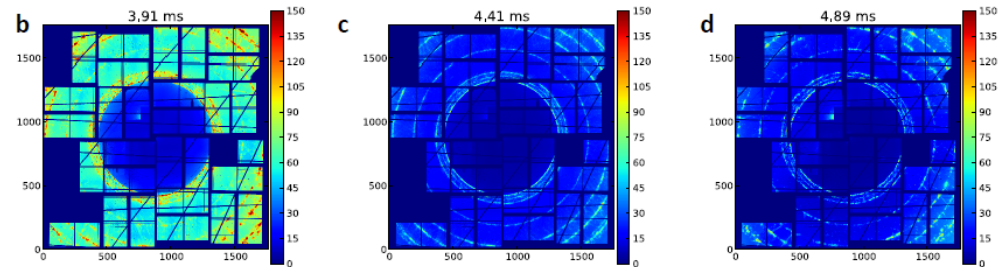
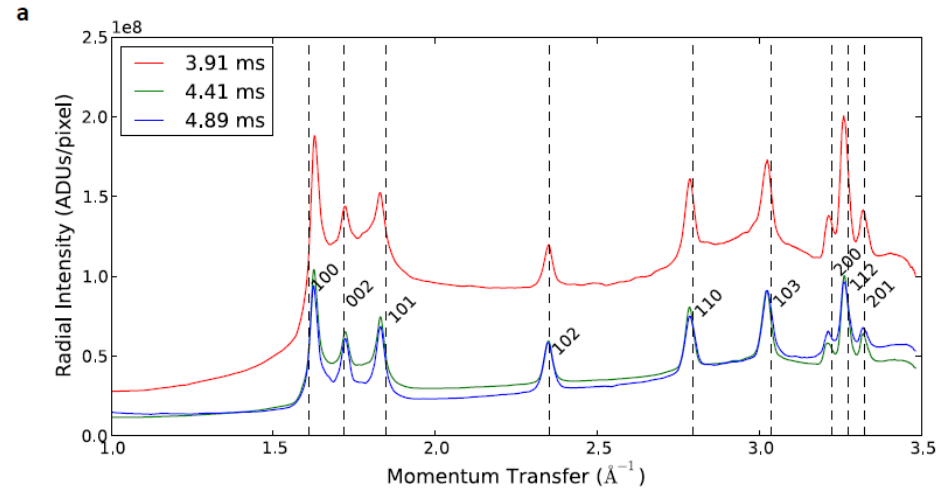
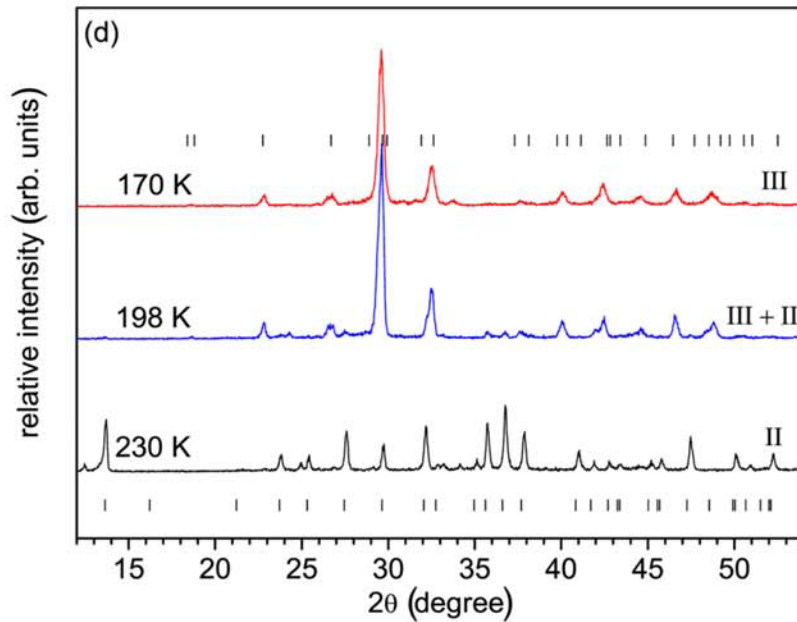
Ice formation

Phys. Rev. Lett. 120, 015501 (2018)

## X-ray diffraction: ices

Typical example: XRD of ice(s)

Fingerprint of structure  $\rightarrow$  no "new" ice without XRD proof

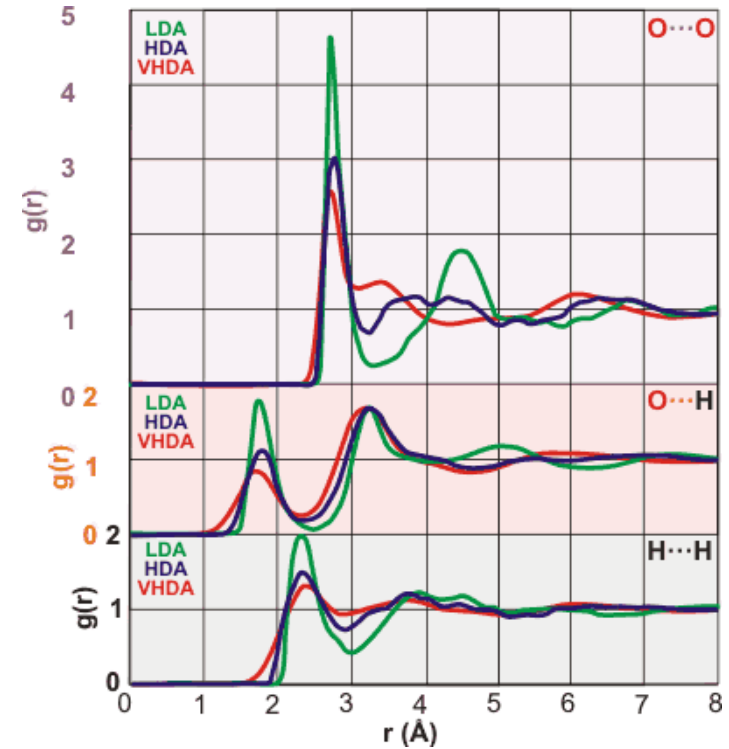
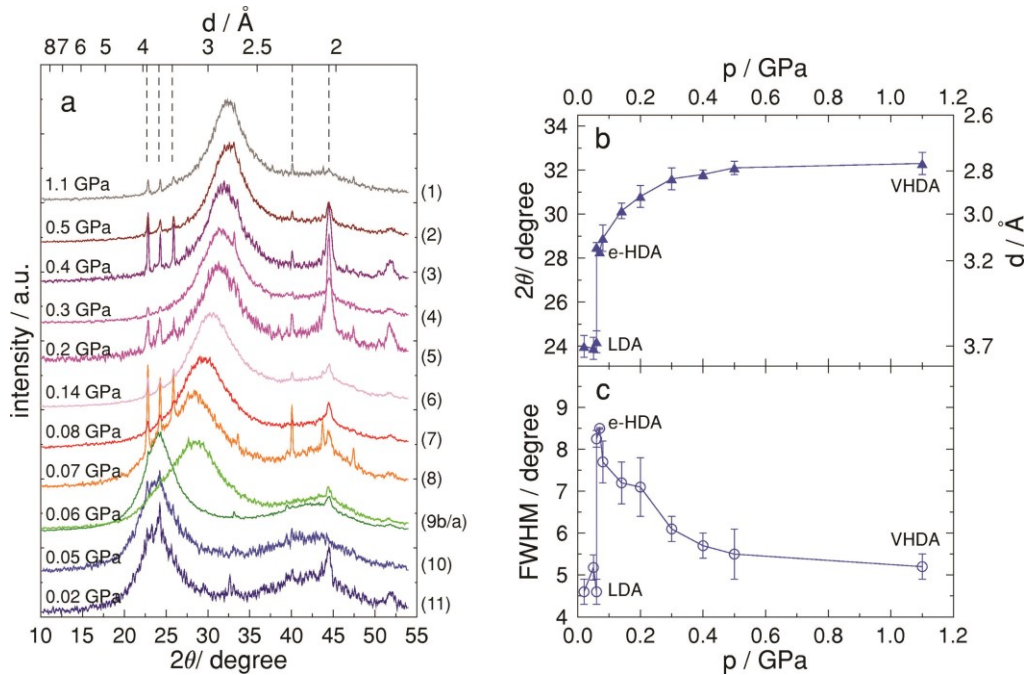


Crystallisation upon fast cooling

Nature 510, 381 (2014)

Phys. Rev. B 77, 220105 (2008)

## Transition of amorphous ices

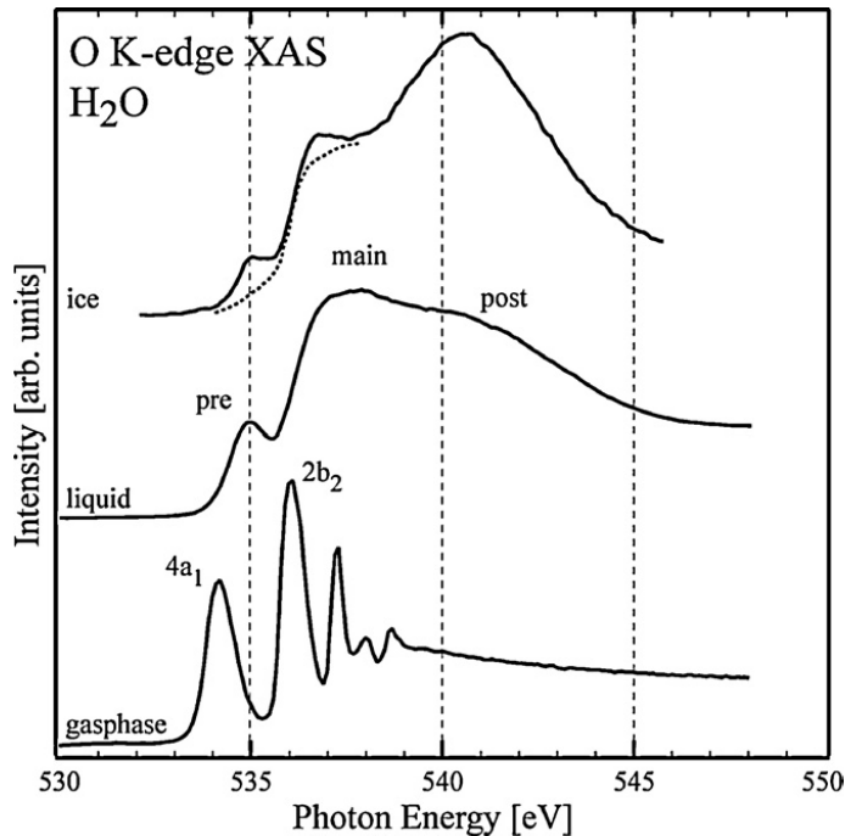


Isothermal decompression of VHDA at 140K to several selected pressures

J. Chem. Phys. doi: 10.1063/1.2830029 (2008)

<http://www1.lsbu.ac.uk/water>

## X-ray spectroscopy



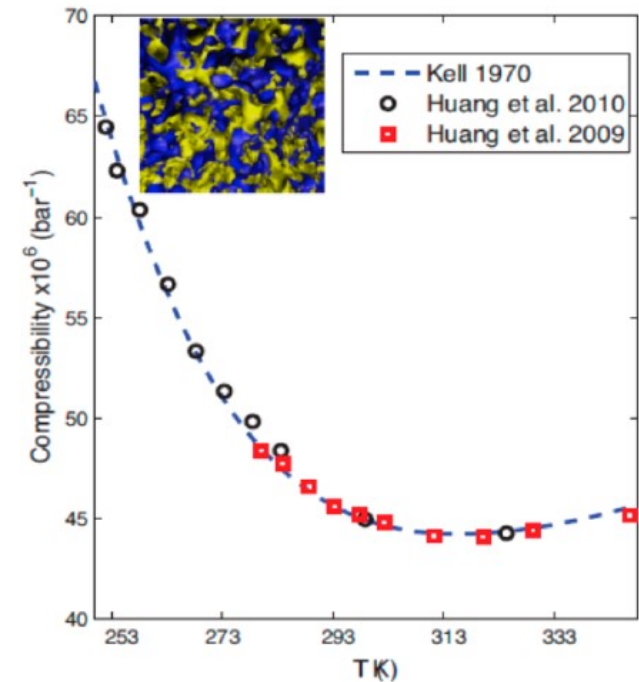
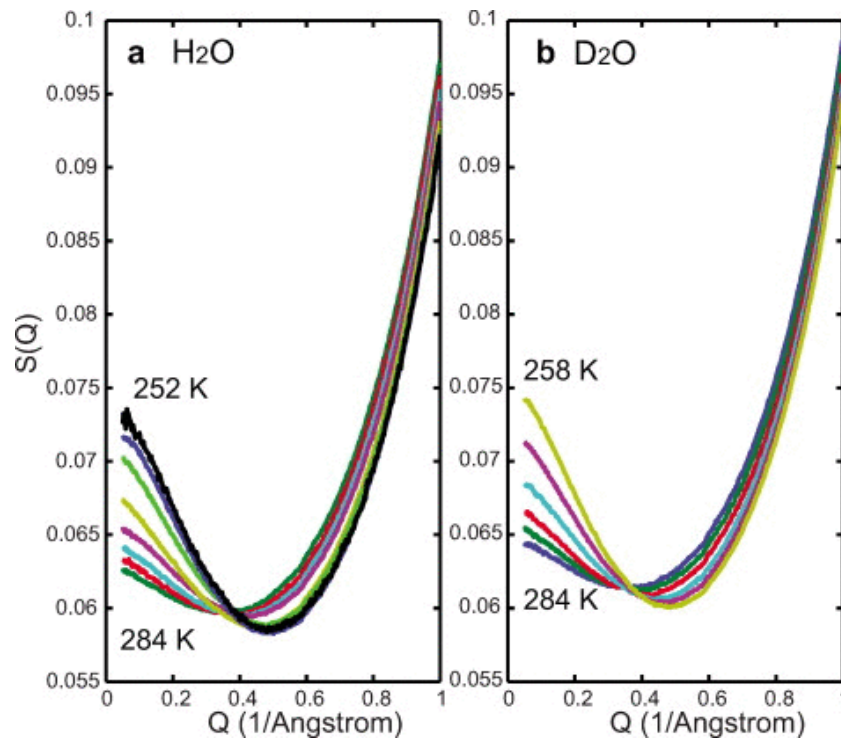
- XAS = X-ray Absorption Spectroscopy
- Fine structure of absorption edge ↔ local structure of sample
- Only indirect access, need e.g. DFT calculations
- Intense debate to which extent XAS results provide information on water models (e.g. LDL/HDL)

J. El. Spec. Rel. Phen. 177, 99 (2010)

## Liquid water: SAXS

Small  $q$  limit in SAXS:  $S(q \rightarrow 0) \propto$  density fluctuations (see Lecture 7)

Isothermal compressibility  $\chi_T$  can be extracted for  $q \rightarrow 0$ :  $S(0) = k_B T \rho_n \chi_T$



J. Chem. Phys. 133, 134504 (2010)

Chem. Rev. 116, 7570 (2016)

# Liquid water: SAXS

Is there a connection between compressibility and the two-liquid hypothesis?  
 → Strongly debated!

## The inhomogeneity at ambient conditions

C. Huang<sup>1</sup>, K. T. Wilkinson<sup>2</sup>, Y. Horikawa<sup>3</sup>, M. L. Huggins<sup>4</sup>, G. M. Pettersson<sup>5</sup>

<sup>1</sup>Stanford Synchrotron Radiation Laboratory, 510691 Stockton, CA, USA; <sup>2</sup>Department of Chemistry, University of California, San Diego, La Jolla, CA, USA; <sup>3</sup>Department of Chemistry, University of Tokyo, Tokyo, Japan; <sup>4</sup>Department of Chemistry, University of California, San Diego, La Jolla, CA, USA; <sup>5</sup>Department of Chemistry, University of California, San Diego, La Jolla, CA, USA

Small-angle X-ray scattering (SAXS) reveals the presence of density fluctuations in liquid water with a length-scale of ~1 nm, while the magnitude of these fluctuations is enhanced with decreasing temperature. Based on X-ray scattering data we propose a model of water in which the inhomogeneity is due to a fluctuation of hydrogen-bonded distorted tetrahedral regions in high density water. We propose a model of water in which the inhomogeneity is due to a fluctuation of hydrogen-bonded distorted tetrahedral regions in high density water. We propose a model of water in which the inhomogeneity is due to a fluctuation of hydrogen-bonded distorted tetrahedral regions in high density water.

Liquid water shows properties such as capacity (1–4). In the liquid point, these properties, related to a and low density water anomalies (5). Above supercooled region where most of waters' of importance occur, has traditionally been of near-tetrahedral with thermal fluctuation picture has been characterized by Raman (XRS) and coherent X-ray scattering (CXRS) (6), and X-ray scattering two distinct local and a highly hydrogen majority. In particular structure has been characterized by SAXS and small-angle direct probes of density in a liquid. Through an momentum transfer,  $Q$ , density at different length

## LETTER

### Is ambient water the nanometer scale

According to a recent study, the inhomogeneity in liquid water is made on the basis of absorption/emission of water molecules.

where  $N$  is the number of water molecules in the scattering volume,  $\Delta\rho$  is the density fluctuation, and  $Q$  is the scattering vector. In noncritical ambient water is heterogeneous. To understand the inhomogeneity in water, we consider a noncritical fluid,  $S(Q)$  is the structure factor,  $\chi$  is the compressibility, and the inhomogeneity in water is heterogeneous. (2), and that the correlation function in water is heterogeneous. (2), and that the correlation function in water is heterogeneous. (2), and that the correlation function in water is heterogeneous.

where  $\phi$  is the volume fraction of the high density phase,  $\Delta\rho$  is the density difference between the two phases, and  $\chi$  is the compressibility. "correlation volume"  $V_c$  is the volume of the correlation function,  $S_c(Q)$  is the structure factor of the correlation function, and  $\chi$  is the compressibility. Eq. 2 is indeterminate.

## LETTER

### Reply to Soper et al. on the two-liquid hypothesis

Soper et al. (1) propose that the two-liquid hypothesis is based on the observation of a bimodal distribution of the structure factor  $S(Q)$  in the small-angle X-ray scattering (SAXS) of liquid water. We argue that the bimodal distribution of  $S(Q)$  is caused by stochastic fluctuations in the structure factor of water. Water, however, exhibits fluctuations both at higher and lower density. The driving force cannot be the same for both. In ref. 2, we suggest that the bimodal distribution of  $S(Q)$  is caused by stochastic fluctuations in the structure factor of water. Water, however, exhibits fluctuations both at higher and lower density. The driving force cannot be the same for both. In ref. 2, we suggest that the bimodal distribution of  $S(Q)$  is caused by stochastic fluctuations in the structure factor of water.

Eq. 2 of ref. 1 applies to two-liquid models and a bimodal distribution of  $S(Q)$  is advocated in ref. 2; the LDL in noncritical ambient water is heterogeneous. In ref. 2, we suggest that the bimodal distribution of  $S(Q)$  is caused by stochastic fluctuations in the structure factor of water. Water, however, exhibits fluctuations both at higher and lower density. The driving force cannot be the same for both. In ref. 2, we suggest that the bimodal distribution of  $S(Q)$  is caused by stochastic fluctuations in the structure factor of water.

There is a recent water simulation (3) which displays nanometer-scale inhomogeneity in water. This is a more disordered (high-temperature) state of water. In ref. 4, we propose a model of water in which the inhomogeneity is due to a fluctuation of hydrogen-bonded distorted tetrahedral regions in high density water. We propose a model of water in which the inhomogeneity is due to a fluctuation of hydrogen-bonded distorted tetrahedral regions in high density water.

## Small-angle scattering of ambient liquid water

Gary N. I. Clark<sup>1</sup>, Greg L. Hura<sup>2</sup>, John D. Weeks<sup>3</sup>

<sup>1</sup>Department of Biomechanical Engineering, University of California, Berkeley, CA 94720; <sup>2</sup>Laboratoire Leon Brillouin, Scientifique (CEA/CNRS), CEA Saclay, 91191 Gif-sur-Yvette, France; <sup>3</sup>Department of Chemistry, University of Maryland, College Park, MD 20742

Edited by John D. Weeks, University of Maryland

Structural polymorphism has been proposed to explain the anomalous thermodynamic properties of water in the experimentally inaccessible metastable liquid region, theory predicts a liquid-liquid critical point from which two water species of high and low density emerge. We analyze X-ray scattering data from a large number of experiments to test the two-liquid hypothesis. We find that the structure factor  $S(Q)$  is consistent with a single liquid phase. We find that the structure factor  $S(Q)$  is consistent with a single liquid phase. We find that the structure factor  $S(Q)$  is consistent with a single liquid phase.

anomalous scattering | density distribution | structural polymorphism

Water appears to be a unique liquid exhibiting several anomalous features. Both experimental and simulation have shown that supercooled water exhibits response properties that appear to diverge near the transition temperature, experimental data are polyamorphic states of water, in of low-density amorphous and high-density (2, 3). This polymorphism has been identified as the anomalous thermodynamic properties of water, such as the large increase in density with decreasing temperature, which is experimentally inaccessible supercooled water. This is a more disordered (high-temperature) state of water. In ref. 4, we propose a model of water in which the inhomogeneity is due to a fluctuation of hydrogen-bonded distorted tetrahedral regions in high density water. We propose a model of water in which the inhomogeneity is due to a fluctuation of hydrogen-bonded distorted tetrahedral regions in high density water.

However, recent studies have shown low-temperature criticality in the ST2 model of water. This is a more disordered (high-temperature) state of water. In ref. 4, we propose a model of water in which the inhomogeneity is due to a fluctuation of hydrogen-bonded distorted tetrahedral regions in high density water. We propose a model of water in which the inhomogeneity is due to a fluctuation of hydrogen-bonded distorted tetrahedral regions in high density water.

Pure Appl. Chem., Vol. 82, No. 10, pp. 1855–1867, 2010.  
 doi:10.1039/C9PP00000A  
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## Recent water myths

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**Abstract:** Recently, there have been a number of claims about the nature of water as a liquid that seem to contradict traditional views. The present paper takes a close look at two of these claims—namely, that water is not the tetrahedral network that it is traditionally regarded as but a chain-like liquid, and that water is intrinsically heterogeneous by nature—and attempts to make sense of them.

**Keywords:** chain structure; computer simulation; mixture models; neutron diffraction; water; X-ray absorption spectroscopy; X-ray diffraction; X-ray emission spectroscopy; X-ray Raman spectroscopy.

## INTRODUCTION

Because it is so important in many different fields of science, water quite naturally attracts an enormous amount of research into its properties and the atom-scale origin of those properties, both in its pure state and in solutions of ions and molecules of all shapes and sizes. Homeopathy, for example, arises from the perceived ability of water to remember its structure under a dissolved entity long after that entity has disappeared, the so-called memory effect of water. Perhaps two of the more bizarre recent claims are that the structure of water is affected by relatively modest magnetic fields [1] and that the structure of water is altered by sunlight [2]. This change in the structure of water due to sunlight appears unlikely: in Britain, for example, the rain during the day is just as wet as the rain at night. In [3] it is stated that water is not the tetrahedral structure traditionally assumed, but consists of chains of water molecules. In [4] it is proposed that ambient water is intrinsically heterogeneous, consisting of a mixture of low- and high-density forms, an idea which has been proposed on many previous occasions for more than 100 years. Given all this often conflicting information, it is not surprising there is much confusion on the true state of water.

Perhaps one of the most surprising facts about water is that it is a liquid. All of the elements that surround oxygen in the periodic table have hydrides which are gases at ambient temperature and pressure, while hydrogen oxide is definitely a liquid with quite a low vapor pressure,  $\approx 5$  mbar. Even more difficult to comprehend is that while water is a liquid with marked "hydrogen" bonds between its constituent molecules, water hydrogen bonds are being formed and broken extremely rapidly, typically around  $10^{12}$  times per second. The diffusion constant is also surprisingly large, around  $2 \times 10^{-5} \text{ cm}^2 \text{ s}^{-1}$ , which means that after 1 s any given water molecule has on average moved about 44  $\mu\text{m}$  from its starting position, corresponding to  $\approx 150000$  molecular diameters. Therefore, whenever we attempt to develop a picture of water we have to keep in mind the extremely dynamic nature of the underlying water molecules that form this material. Based on these numbers, it is difficult to envisage how water can re-

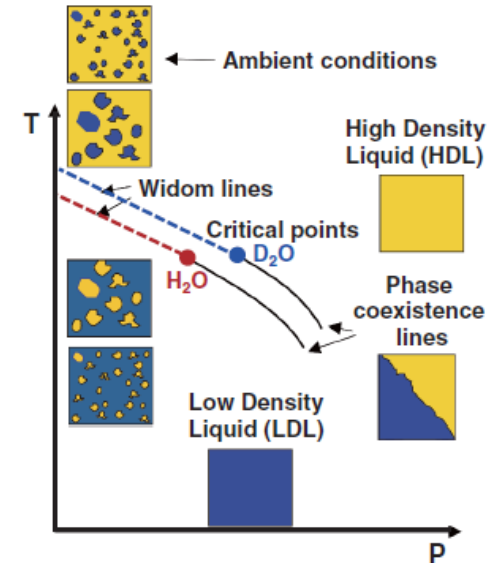
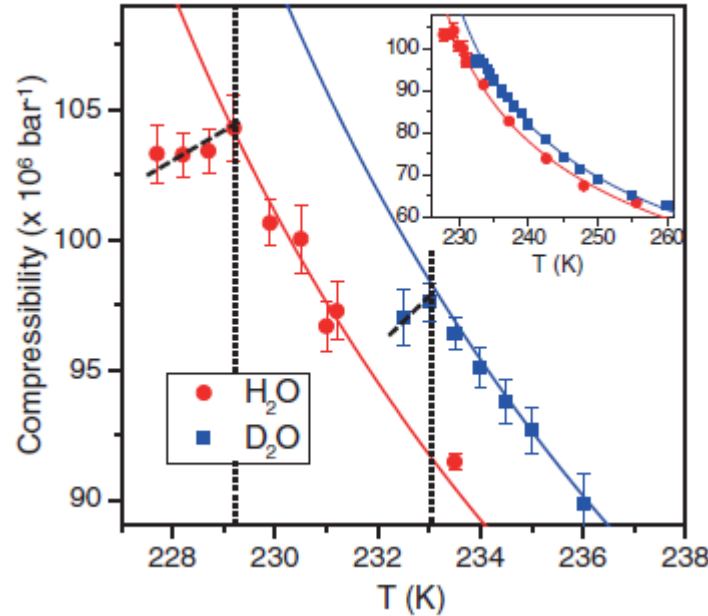
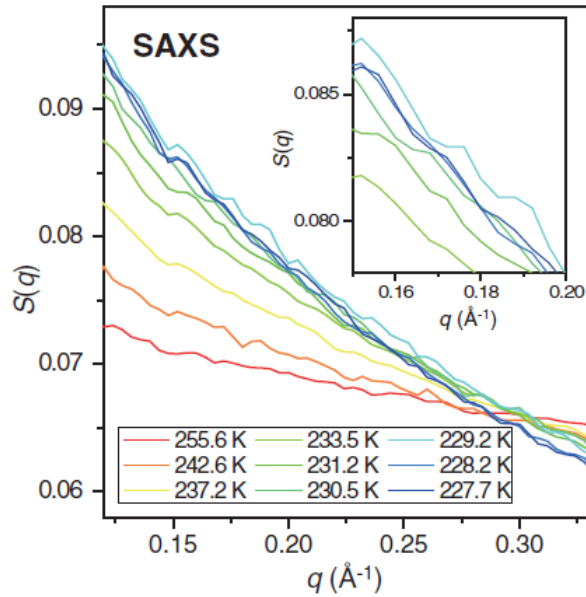
\*Paper based on a presentation at the 31<sup>st</sup> International Conference on Solution Chemistry (ICSC-31), 21–25 August 2009, Innsbruck, Austria. Other presentations are published in this issue, pp. 1855–1973.





# Liquid water: SAXS at FEL

Microdroplets → stronger supercooling possible



SAXS data:  $S(q \rightarrow 0)$

Compressibility

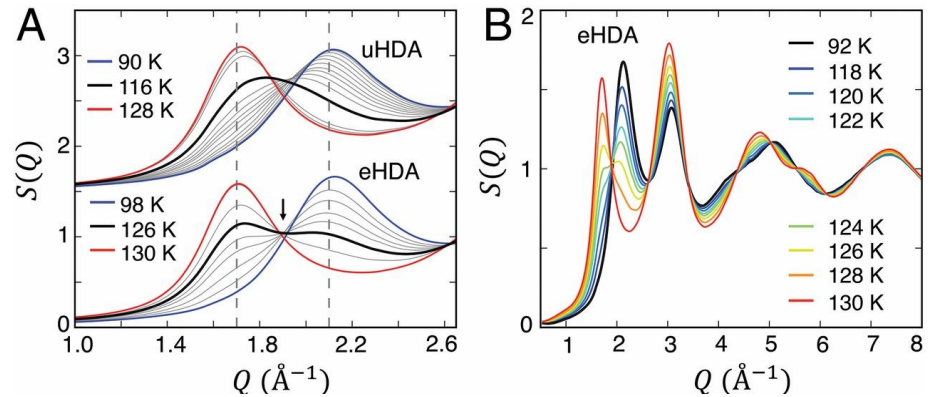
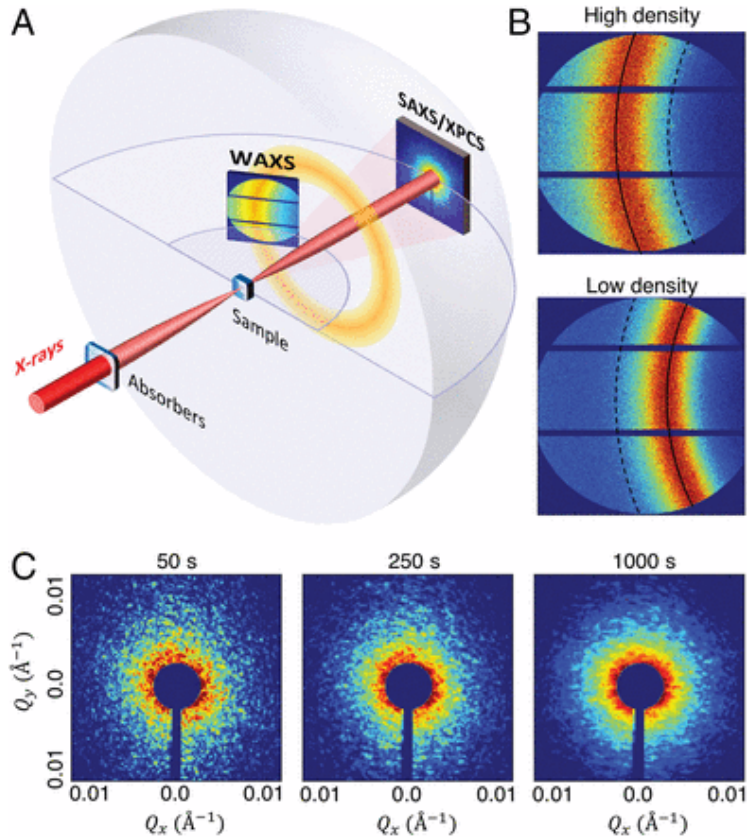
Proposed phase diagram

Science 358, 1589 (2017)

→ Compressibility maximum by crossing the Widom line

→ But: depends on the estimation of water density

# Dynamics in amorphous ices & liquid water



## X-ray diffraction

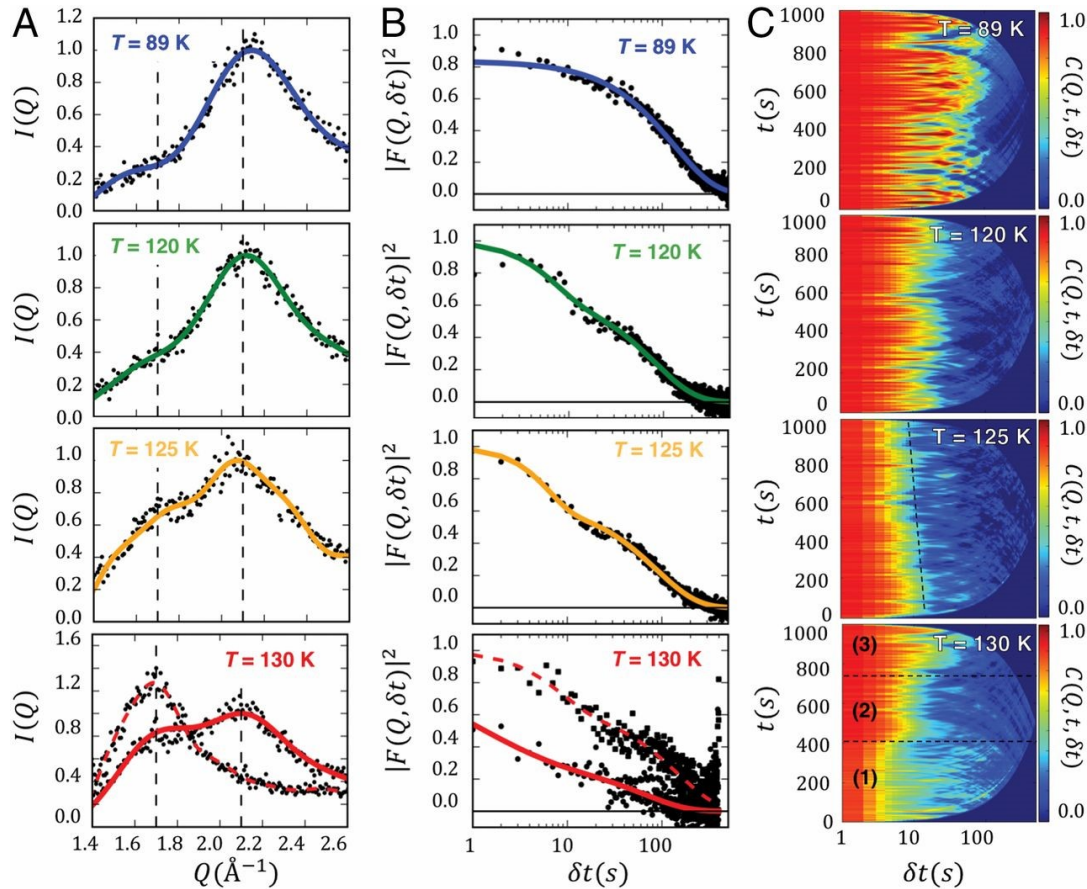
- Double peak for eHDA: coexistence of high- and low-density form
- Decomposition of  $S(Q)$  (and  $g(r)$ ) in two (main) contributions possible

## Transition of HDA to LDA

PNAS 114, 8793 (2017)

Dynamics information to quantify glass-glass or liquid-liquid transition

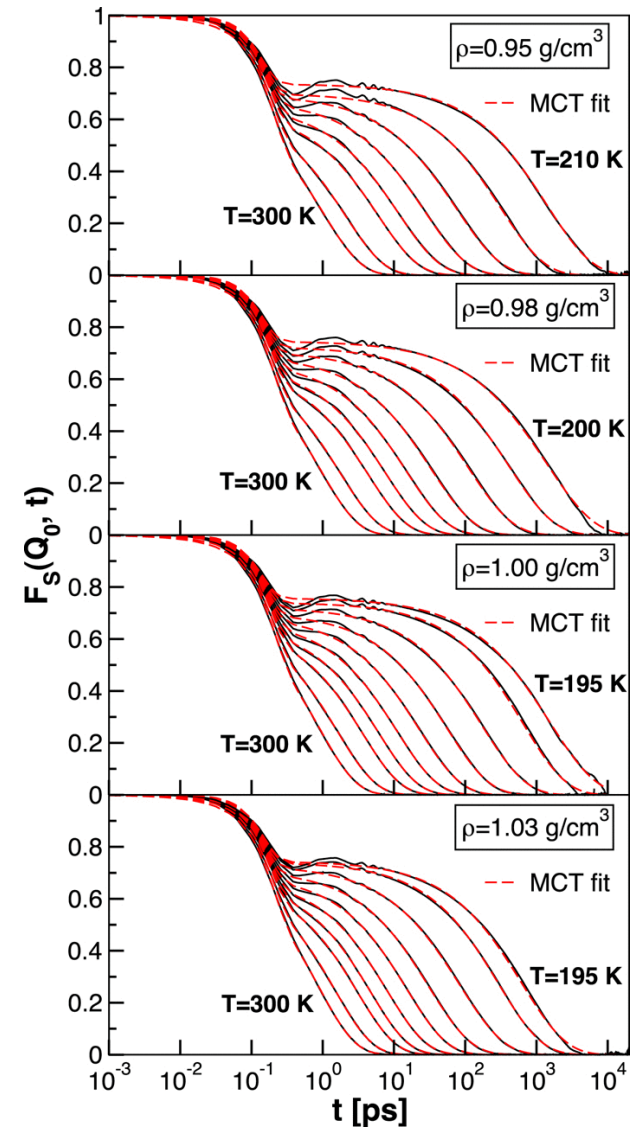
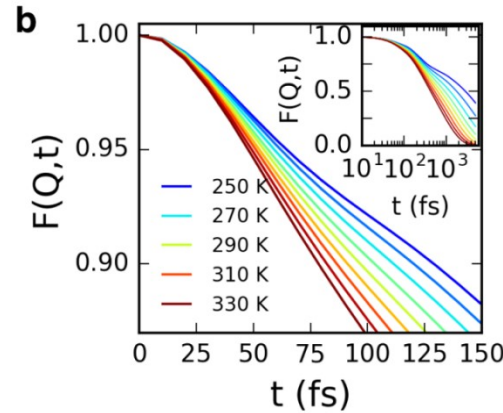
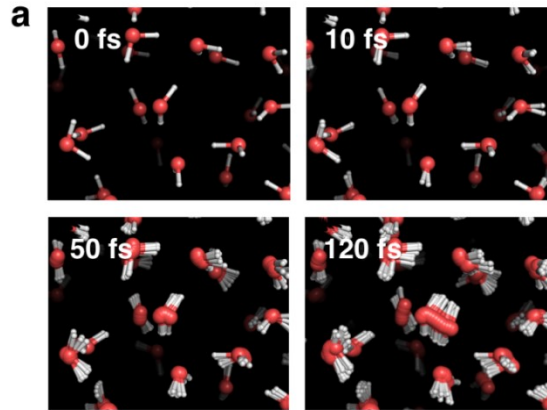
## Dynamics in amorphous ices & liquid water



- $T < 110 \text{ K}$ : viscoelastic relaxation of HDA
- Onset of diffusive dynamics for  $T \geq 110 \text{ K}$
- HDA domains transform to ultraviscous **HDL**
- Around  $T = 130 \text{ K}$ : transformation to ultraviscous **LDL**

PNAS 114, 8793 (2017)

# Dynamics in amorphous ices & liquid water



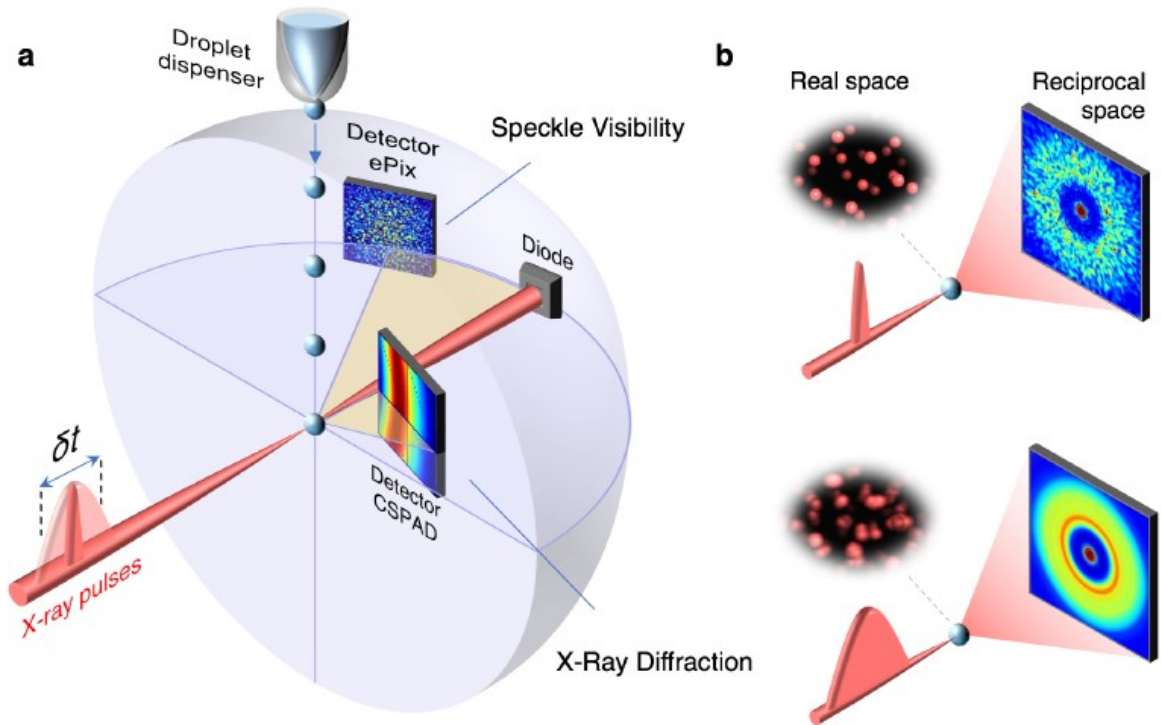
- Liquid water: fs dynamics → FEL pulse length
- MD simulations of liquid water show two-step decay of intermediate scattering function
  - fragile-to-strong crossover
  - LLCP hypothesis

Nature Comm. 9, 1917 (2018).

JCP 144,  
 074503 (2016)

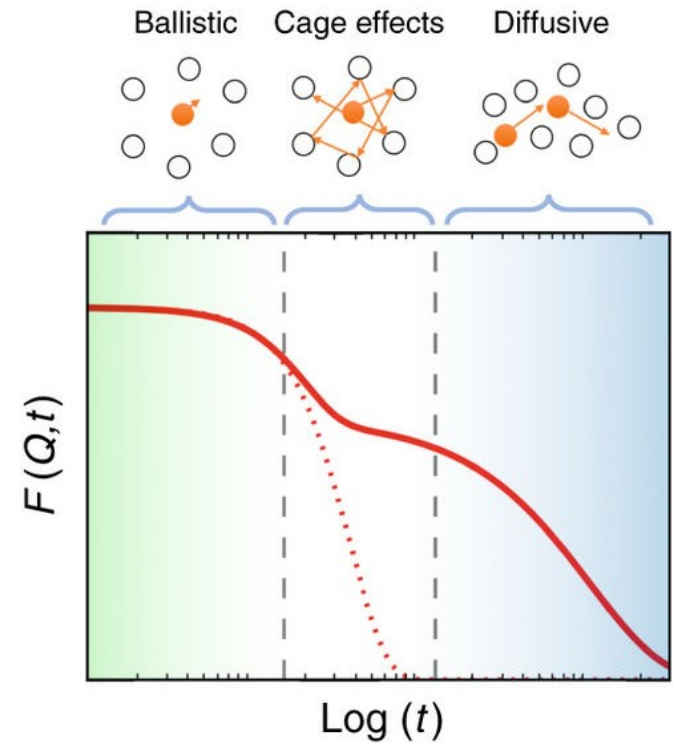
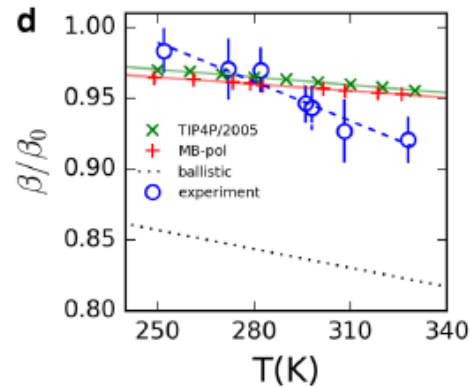
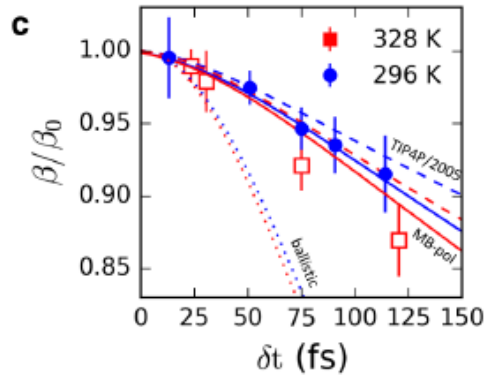
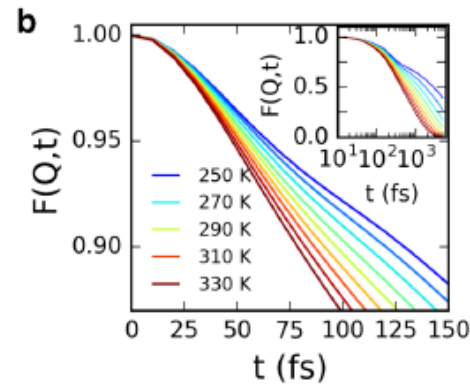
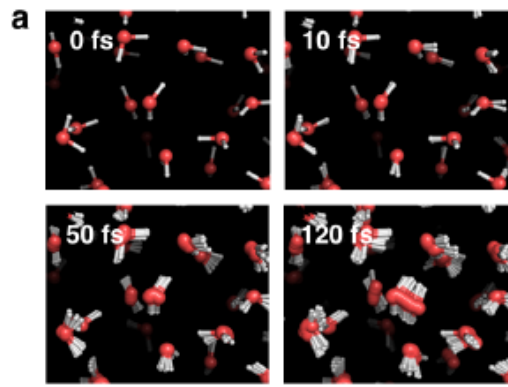


# Dynamics in amorphous ices & liquid water



- XSVS experiment
- Water structure factor peak around  $2 \text{ \AA}^{-1}$
- >10000 shots per setting

Nature Comm. 9, 1917 (2018).



- Molecular dynamics in real time experiments
- Influence from H-bonding at sub-100 fs time scales
- "Cage effects"

Nature Comm. 9, 1917 (2018).

## Further questions, interest, master thesis etc.

Soft matter, colloids, coherent X-ray scattering (XPCS, XCCA, ...), water

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