

Methoden moderner Röntgenphysik II: Streuung und Abbildung

Lecture 3	Vorlesung zum Haupt- oder Masterstudiengang Physik, SoSe 2016 G. Grübel, M. Martins, S. Roth, O. Seeck, T. Schneider
Location	Lecture hall AP, Physics, Jungiusstraße
Date	Tuesday 12:30 - 14:00 Thursday 8:30 - 10:00

Methoden moderner Röntgenphysik II: Streuung und Abbildung

Part I:

Basics of X-ray Physics

by Gerhard Grübel (GG)

Introduction

Overview, Introduction to X-ray Scattering

X-ray Scattering Primer

Elements of X-ray Scattering

Sources of X-rays, Synchrotron Radiation

Laboratory Sources, Accelerator Bases Sources



Reflection and Refraction from Interfaces

Snell's Law, Fresnel Equations

Kinematical Diffraction (I)

Diffraction from an Atom, a Molecule, from Liquids, Glasses, ...

Kinematical Diffraction (II)

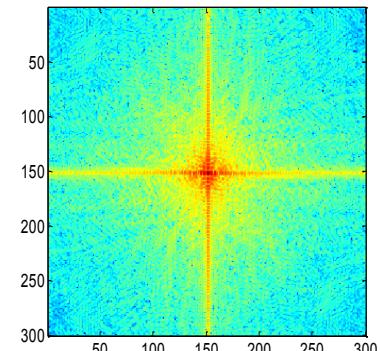
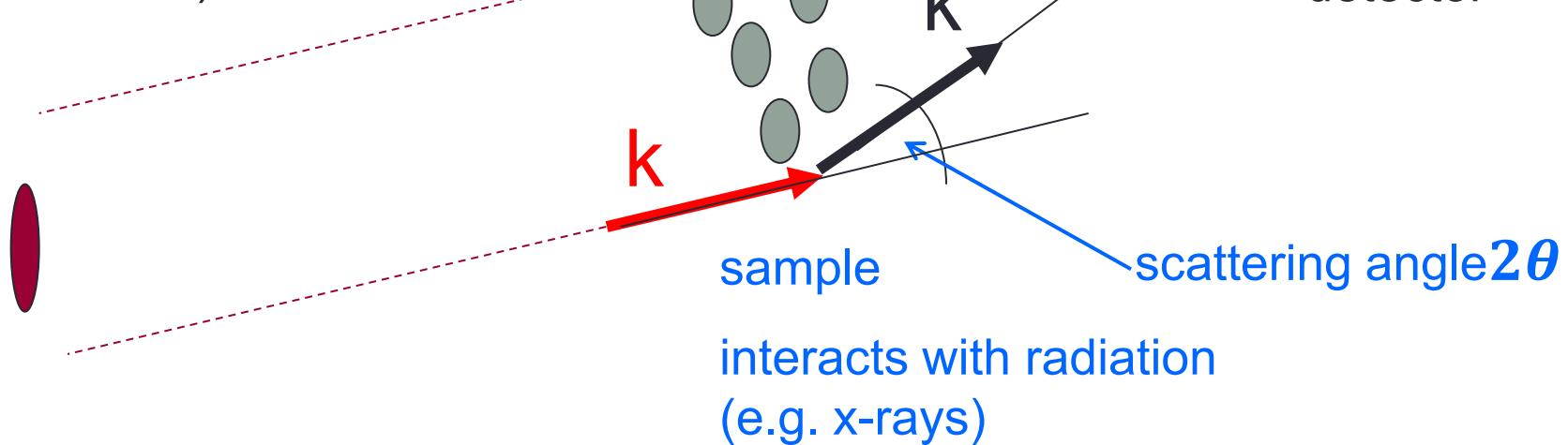
Diffraction from a Crystal, Reciprocal Lattice, Structure Factor, ...

Set-up for Scattering Experiments

source (visible light, x-rays,...)

source parameters: source size, λ , $\frac{\Delta\lambda}{\lambda}$...

coherence properties:
(incoherent, partially coherent,
coherent)

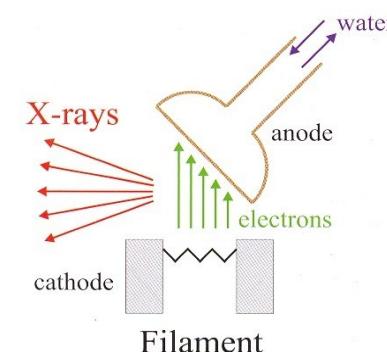


Source of X-Rays

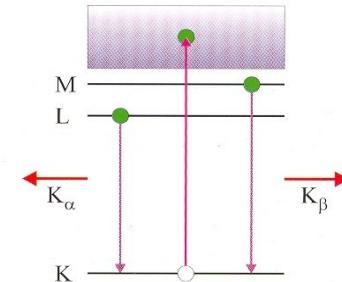
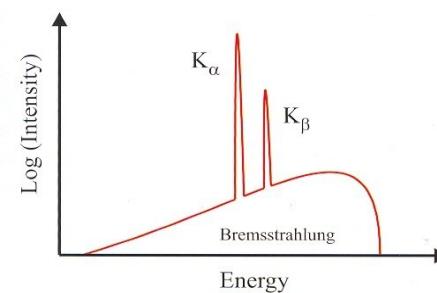
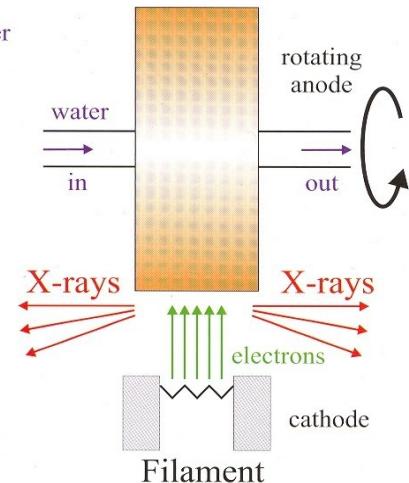
- 1895 Discovered by W.C. Röntgen
- 1912 First diffraction experiment (v. Laue)
- 1912 Coolidge tube (W.D. Coolidge, GE)
- 1946 Radiation from electrons in a synchrotron, GE,
Physical Review, 71,829 (1947)



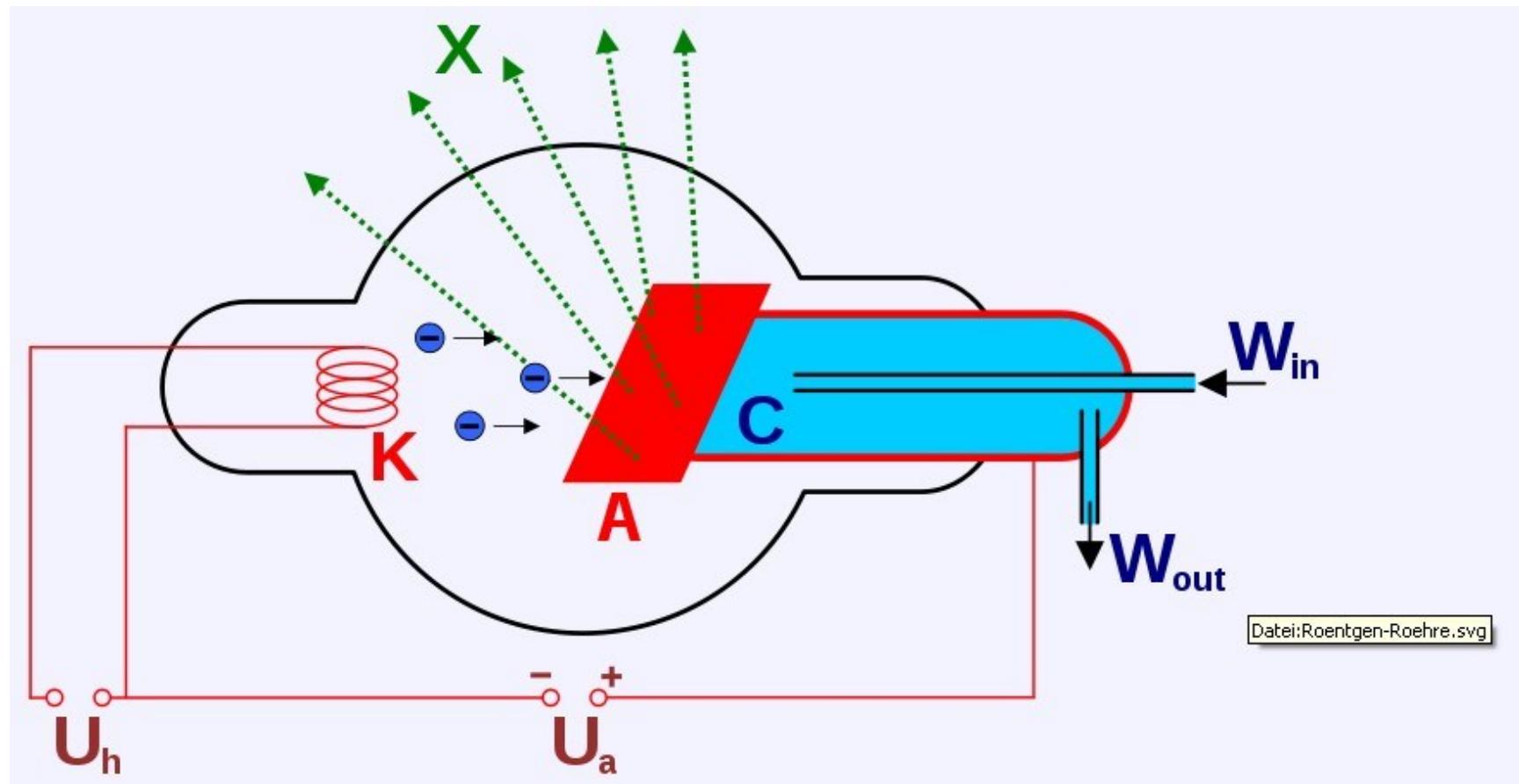
Coolidge Tube



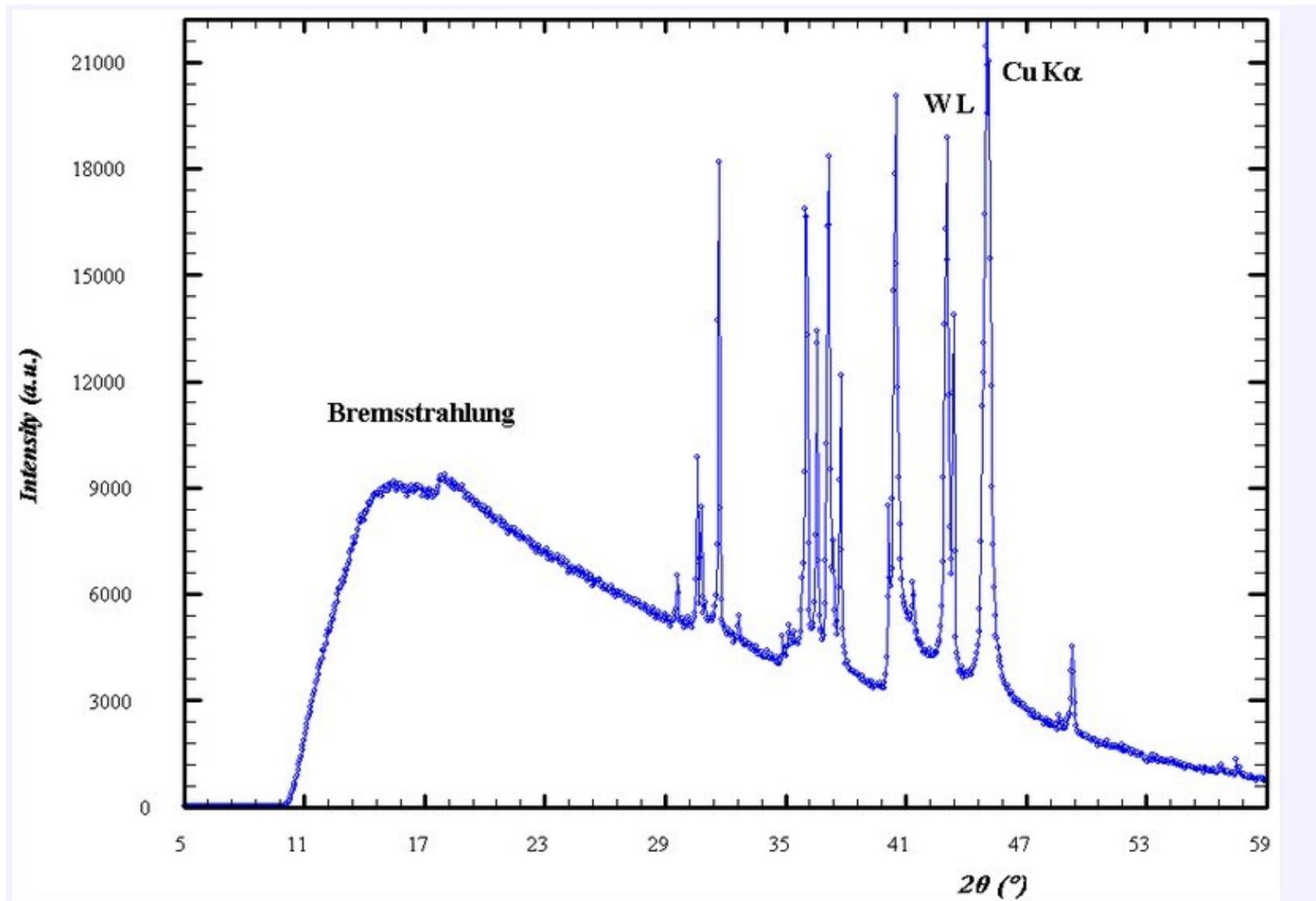
Rotating Anode



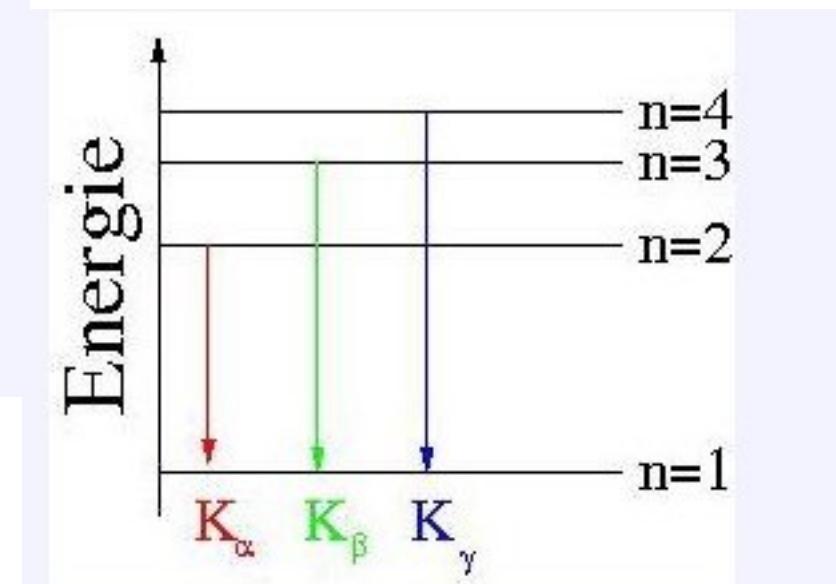
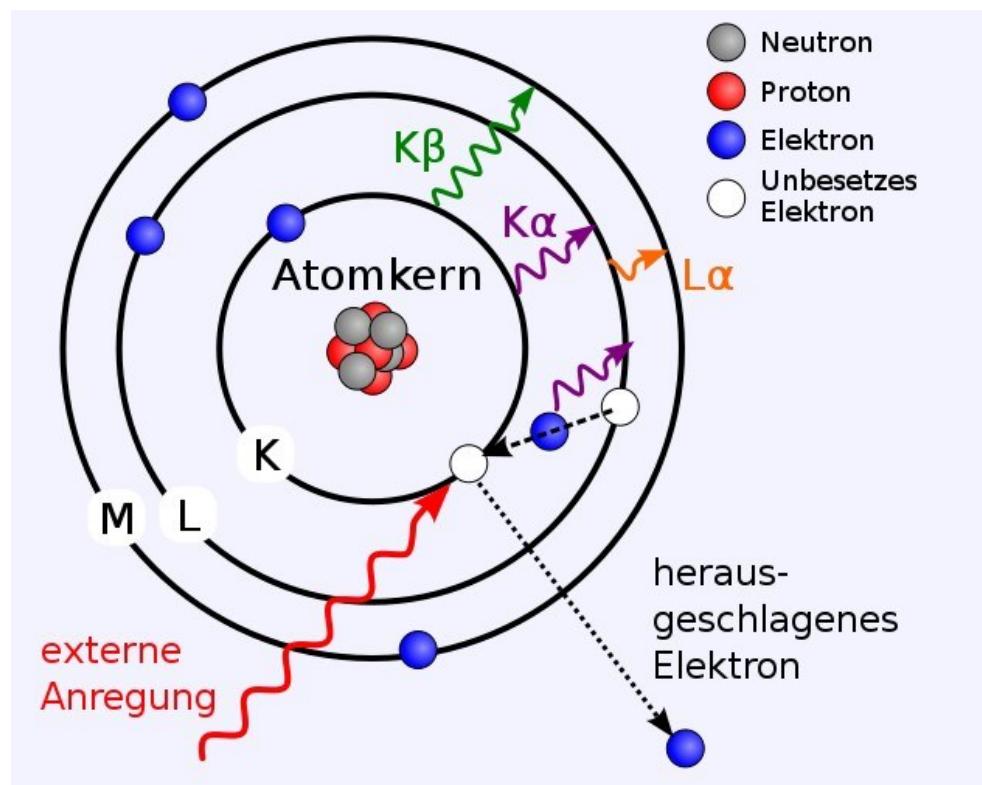
X-Ray Tube



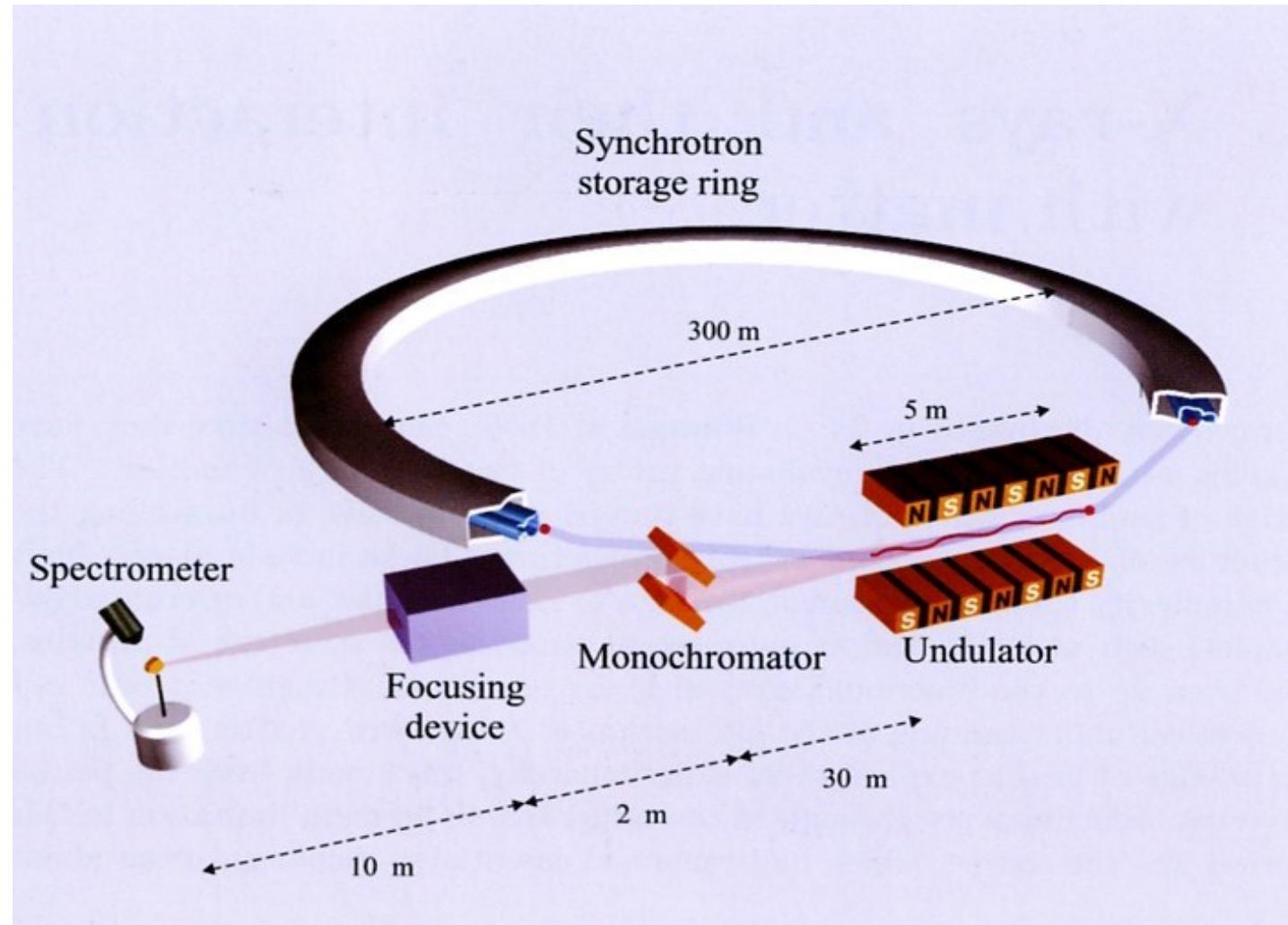
X-Ray Tube



X-Ray Tube



Synchrotron Radiation Storage Ring



Circular Accelerators

Cyclotron
Microtron
Synchrotron
Storage Ring

Cyclotron

- Proposed in 1930 by E.O. Lawrence
- Electrons circulate in a homogeneous magnetic field B
- Frequency for one cycle is given by

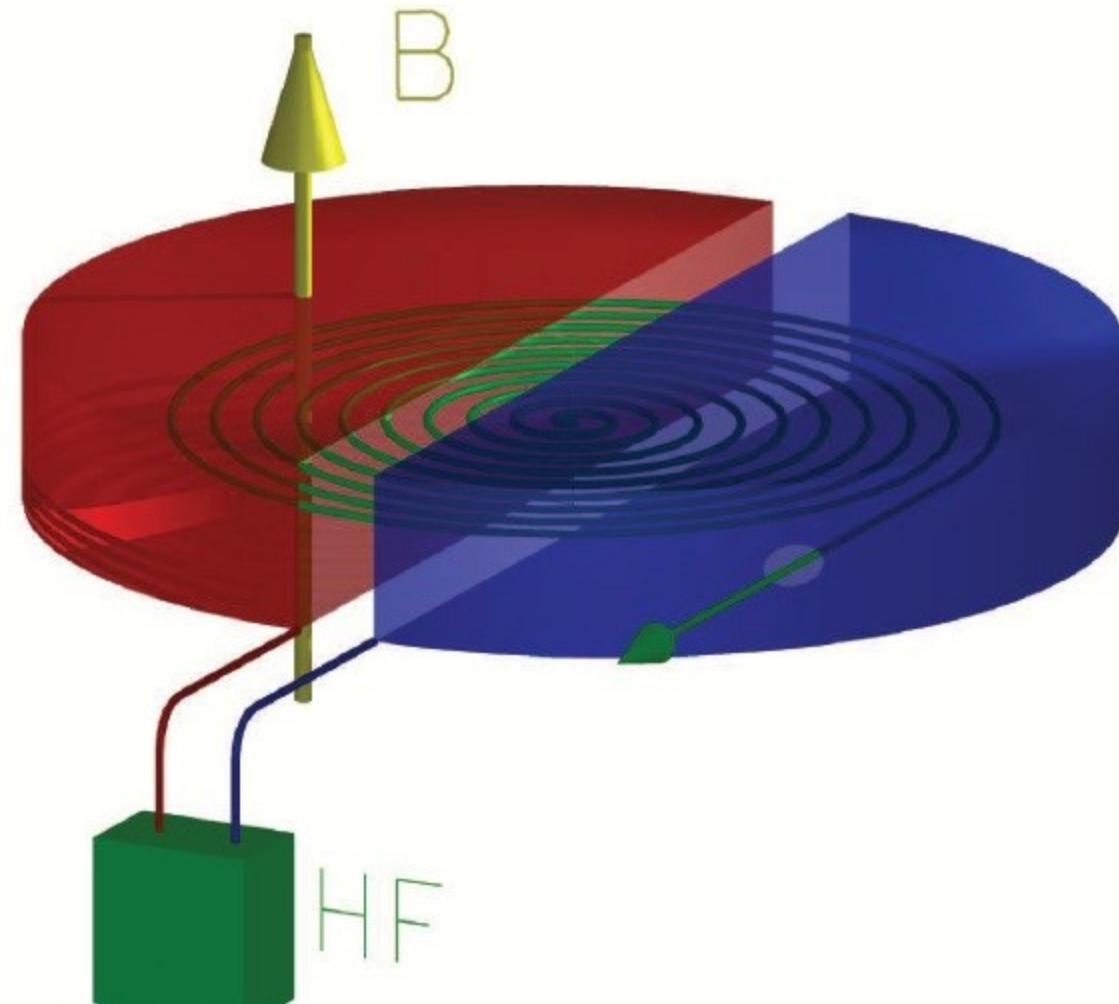
$$\omega_c = \left(\frac{e}{m}\right) B_z$$

- For non-relativistic electrons ω_c is independent of the velocity v
$$\left(\frac{v}{c} < 0.15\right)$$
- At high energies the mass changes and the frequency of the field needs to be adapted.

Example: $E_{\text{kin}} = 10\text{keV} = eU = m_e \frac{v_e^2}{2} \Rightarrow \frac{v_e}{c} = 0.2!$

- Electrons at 10 keV are already relativistic!

Cyclotron



Cyclotron



Zyklotron der
Uni Bonn

Microtron

- Acceleration with a linear accelerator
- Circular bend similar to a cyclotron
- Bending radius R in magnetic field B for relativistic particles

Lorentz Force = Radial Force

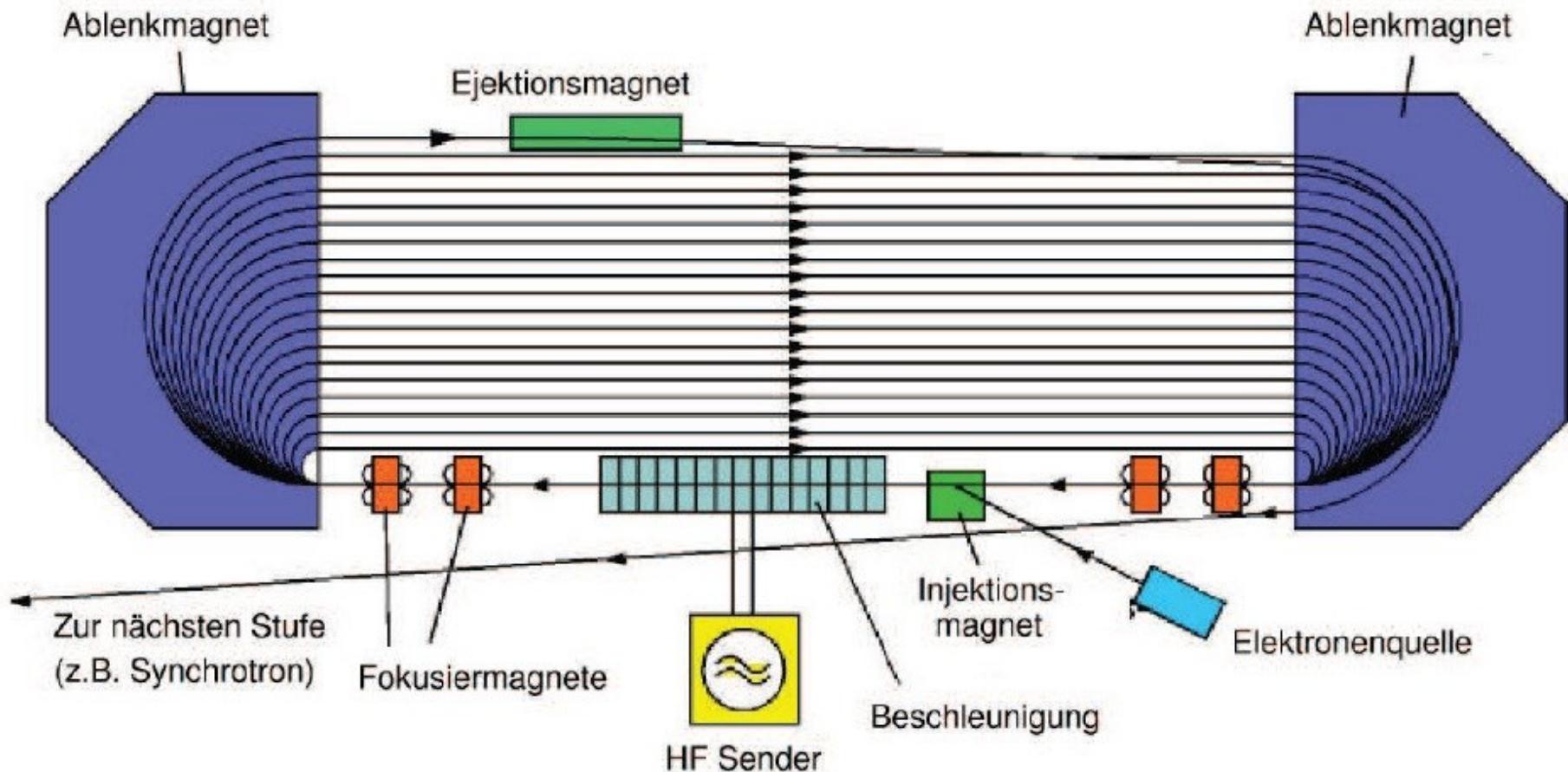
$$evB = m \frac{v^2}{R}$$

$$\Rightarrow R = \frac{mv}{eB} = \frac{vmc^2}{ec^2B} = \left(\frac{v}{ec^2B} \right) E$$

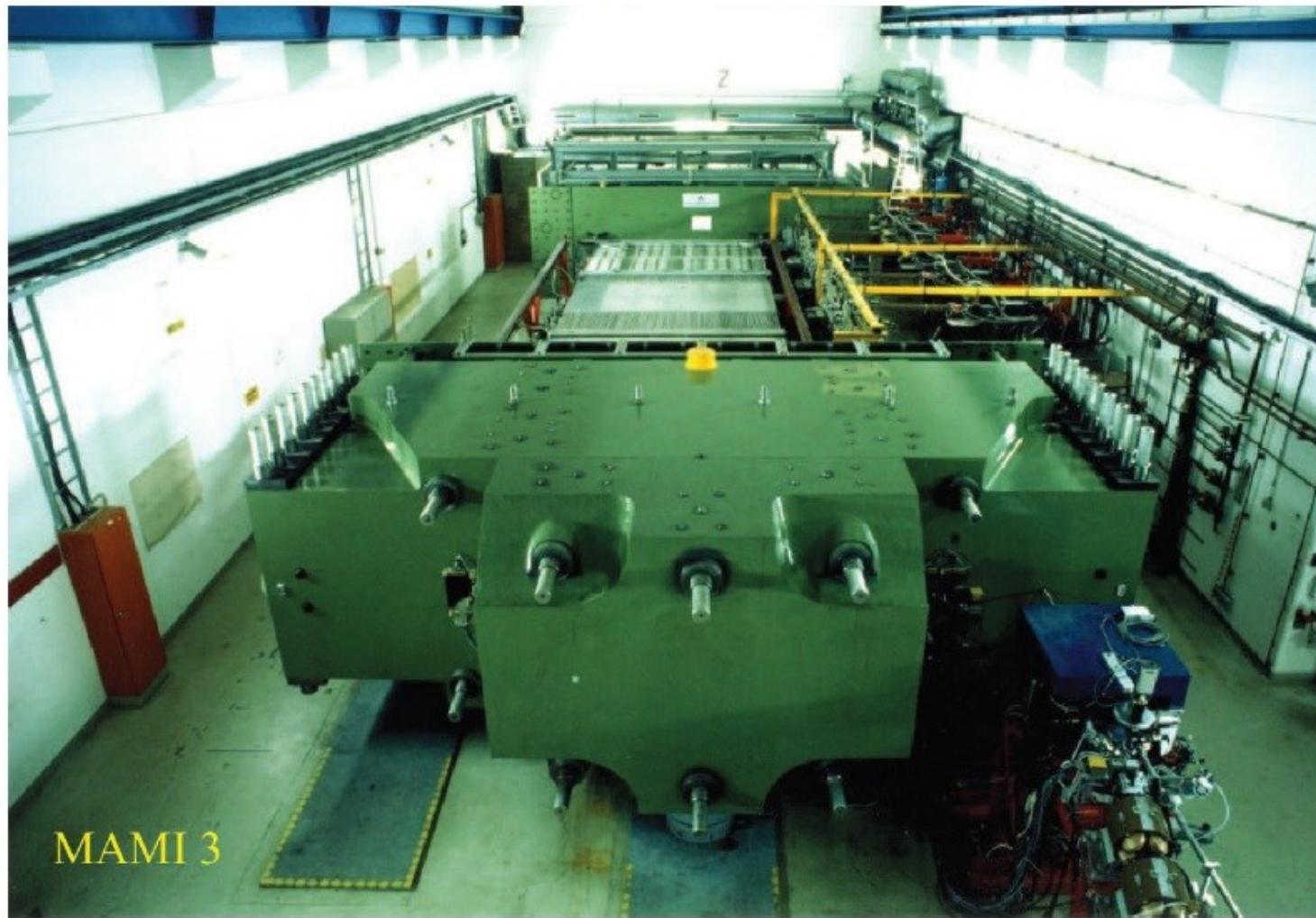
- Such Acceleration that electrons are in phase with RF field
- Energies up to 100 MeV can be reached

Example: BESSY II

Microtron



Microtron



Synchrotron

- For relativistic particles $v \cong c$ in a B field, the radius is given by

$$R = \frac{E}{ecB}$$

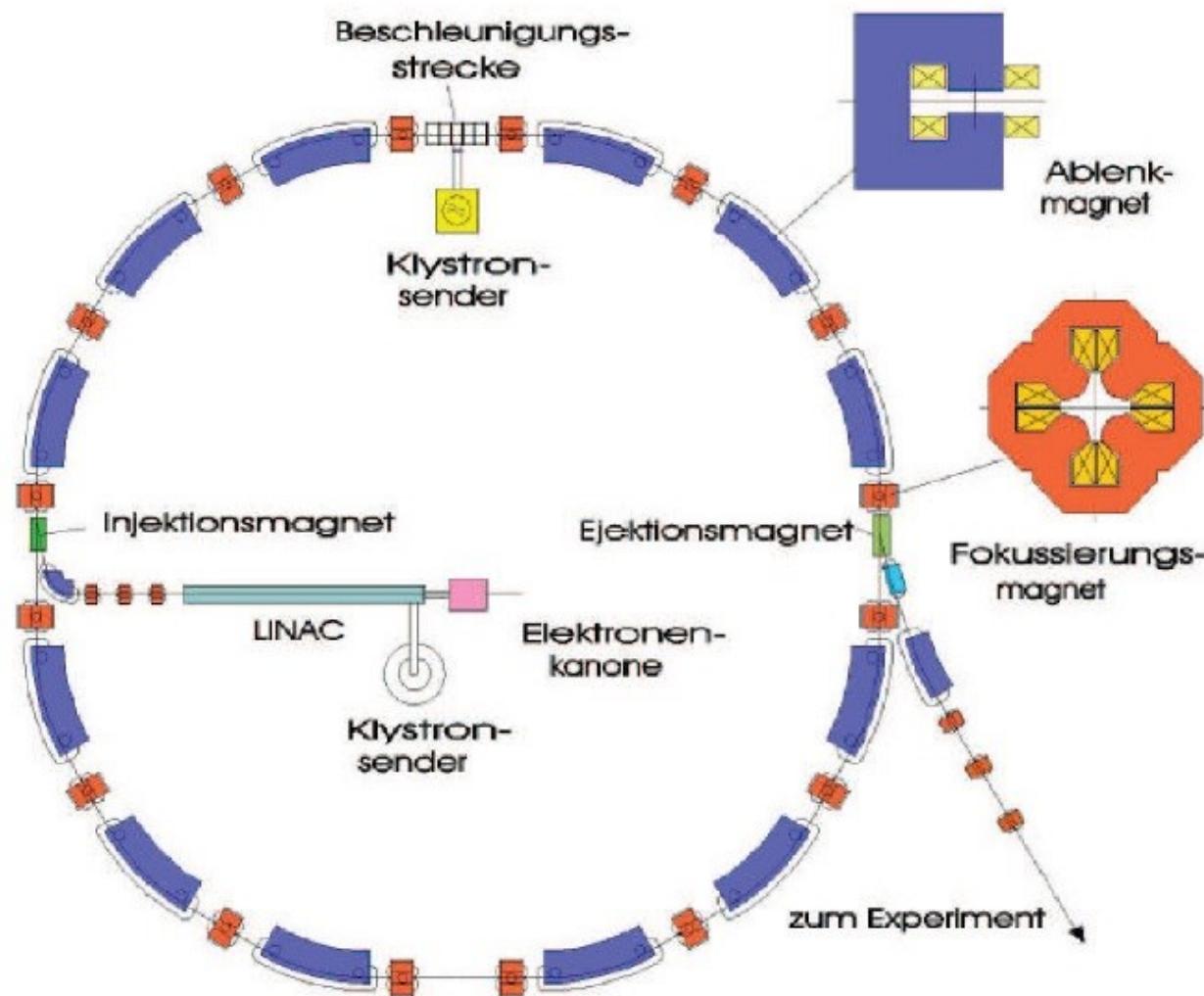
- For $E > 1$ GeV and $B = 5$ T : $R >$ several meter
- Technically difficult
- Enforce trajectory with constant radius

Bends in small , local magnets

$\frac{E}{B} = \text{const.} \Rightarrow$ synchronous ramping of E and B

⇒ Synchrotron

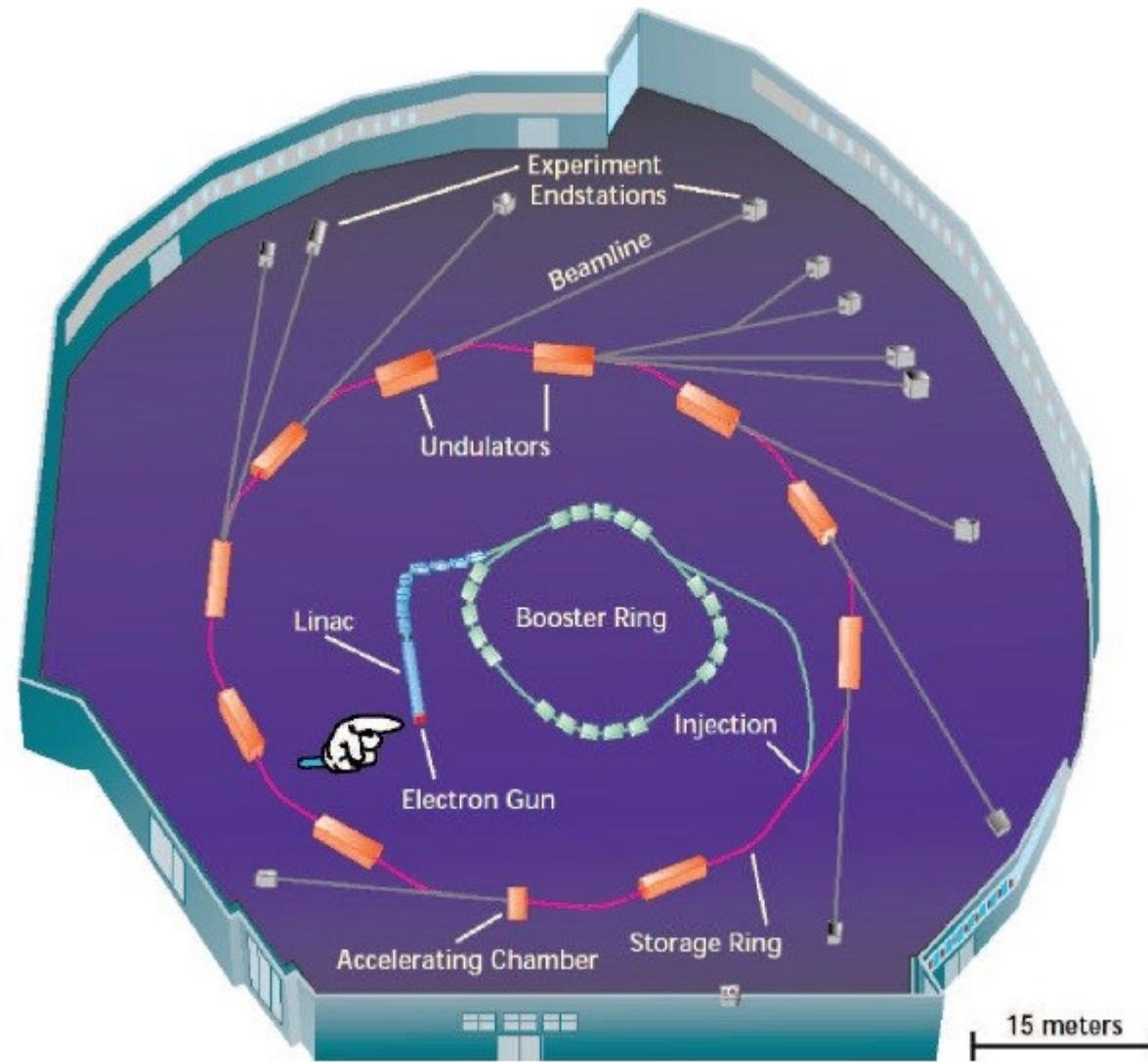
Synchrotron



Synchrotron

- Modern synchrotron radiation sources are built as storage rings
- Synchrotron cannot operate at $E=0$ since it requires $B=0$.
 - ⇒ Use LINAC or Microtron as pre-accelerator
 - Use synchrotron to reach the final energy E
 - Use storage ring to keep electrons at energy
- The storage ring supplies the energy lost by radiation in each turn.
- Typical parameters: Lifetime: up to 30 h
Current: 100 – 500 mA
- Current losses through interaction with residual gas ⇒ UHV
- Current supplied in bunches.

Storage Rings



Storage Rings



Photon Machines

The three largest and most powerful synchrotrons in the world



APS, USA



ESRF, Europe-France



Spring-8, Japan



Synchrotron Radiation Primer

Radiation of a non-relativistic, accelerated particle:

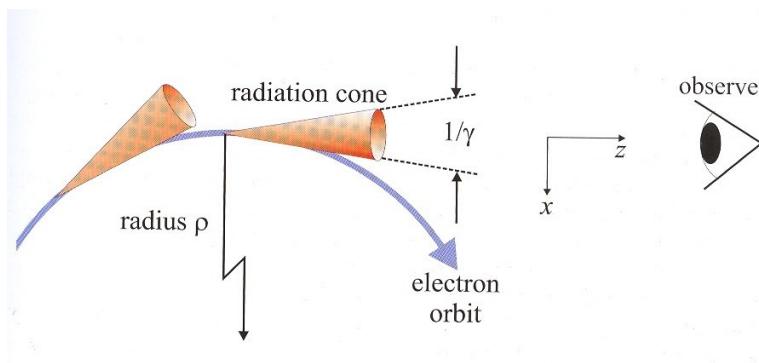
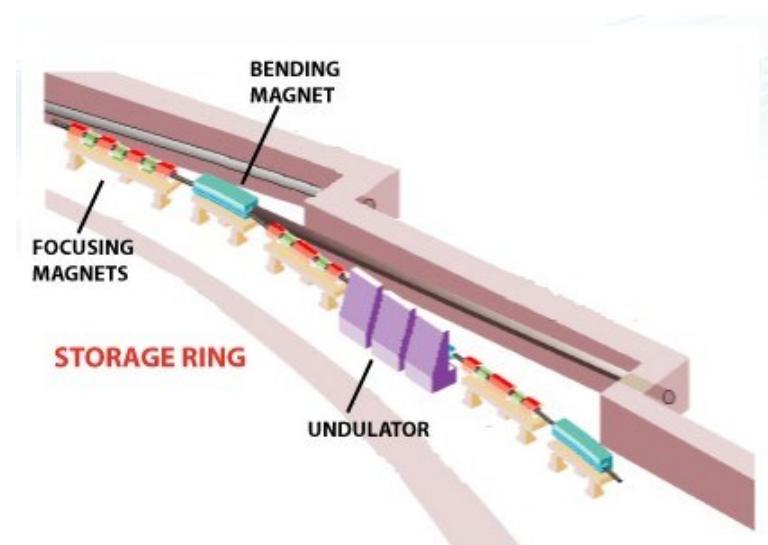
$$P = \left(\frac{e^2}{6\pi\epsilon_0 m_0^2 c^3} \right) \left(\frac{dp}{dt} \right)^2$$

Angular distribution resembles the one of a Hertz dipole:

$$\left(\frac{dP}{d\Omega} \right) = \left(\frac{e^2}{16\pi^2\epsilon_0 m_0^2 c^3} \right) \left(\frac{dp}{dt} \right)^2 \sin^2(\Psi)$$

Radiation is emitted (similar to the dipole) in the direction perpendicular to the acceleration

Synchrotron Radiation Primer



Energy E_e of an electron at speed v :

$$E_e = \frac{mc^2}{\sqrt{1 - \left(\frac{v}{c}\right)^2}} = \gamma mc^2$$

For 5GeV and $mc^2=0.511$ MeV get $\gamma \approx 10^4$

Centrifugal=Lorentz force yields for radius:

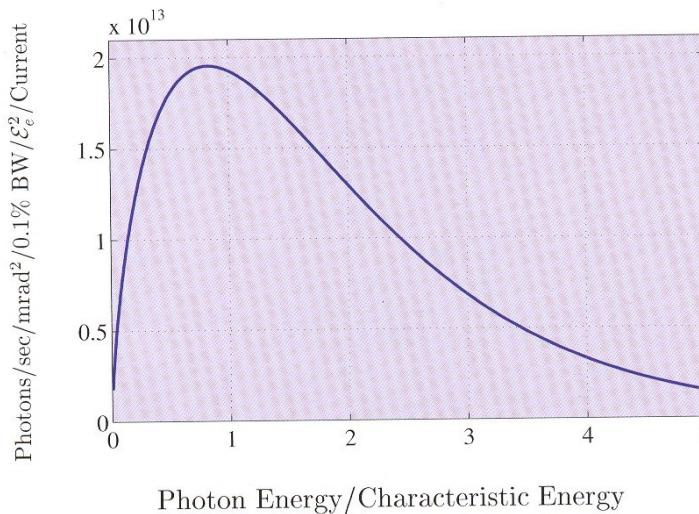
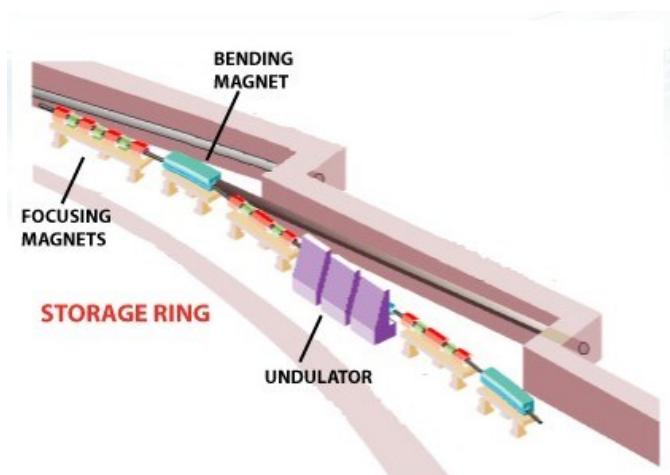
$$\rho = \frac{\gamma mc}{eB} = \frac{3.3 E [\text{GeV}]}{B [\text{T}]} \approx 25 \text{ m}$$

$$E_e = 6 \text{ GeV}, \quad B = 0.8 \text{ T}$$

Opening angle is of order $\frac{1}{\gamma} \approx 0.1 \text{ mrad}$



Bending Magnets



Characteristic energy $\hbar\omega_c$ for bend or wiggler:

$$\hbar\omega_c[\text{keV}] = 0.665 E_e^2 [\text{GeV}] B(\text{T}) \approx 20 \text{ keV}$$

$$\text{Flux} \sim E^2$$

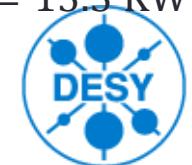
Energy loss by synchrotron radiation per turn:

$$\Delta E[\text{keV}] = \frac{88.5 E^4 [\text{GeV}]}{\rho[\text{m}]}$$

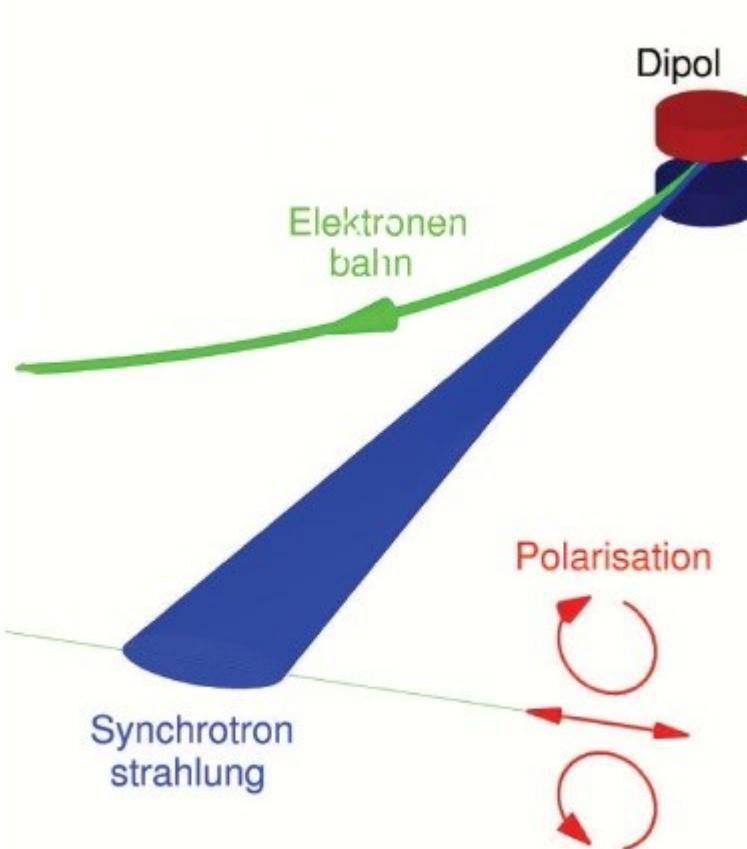
For 1 GeV and $p = 3.33 \text{ m}$: $\Delta E = 26.6 \text{ keV/turn}$

$$\text{For } I = 500 \text{ mA} \equiv 0.5 \frac{C}{s} = 0.5 \times 6.25 \times 10^{18} \frac{e^-}{s}$$

$$\begin{aligned} \rightarrow P &= 0.5 \times 6.25 \times 10^{18} \frac{e^-}{s \times 26.6 \text{ keV}} \\ &= 8.3125 \times 10^{22} \times 1.6 \times 10^{-19} = 13.3 \frac{\text{kJ}}{\text{s}} = 13.3 \text{ KW} \end{aligned}$$



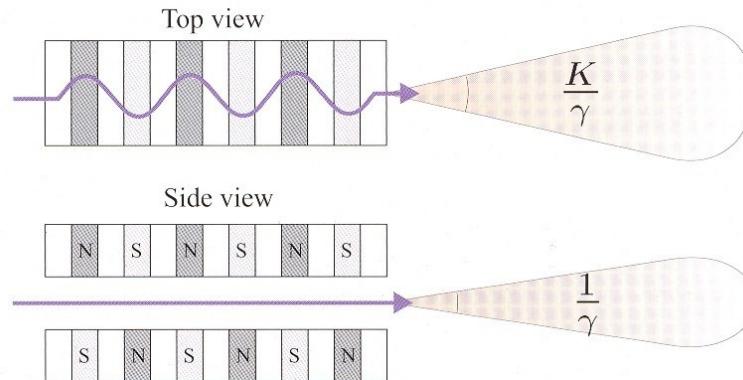
Polarization



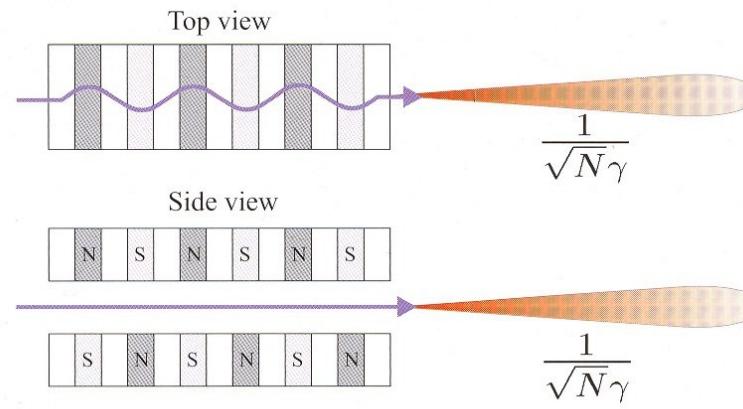
- Synchrotron radiation is polarized linearly in the plane of the orbit
- Above and below the orbital plane of the polarization is circular
- Important applications for magnetic x-ray scattering

Insertion Devices (Wiggler and Undulators)

(a) Wiggler



(b) Undulator



Wiggler:

$$P[\text{kW}] = 0.633 E_e^2 [\text{GeV}] B^2 [\text{T}] L[\text{m}] I[\text{A}]$$

$$\text{Flux} \sim E^2 \times N$$

N: number poles

Undulator:

$$k = eB / mc \quad k_u = 0.934 \lambda_u [\text{cm}] \quad B_0 [\text{T}]$$

with λ_u undulator period

undulator fundamental:

$$\lambda_0 = \frac{\lambda_u}{2\gamma^2} \left(1 + \frac{k^2}{2} + \gamma\theta \right)$$

~~on axis~~

$$\text{Flux} \sim E^2 \times N^2$$

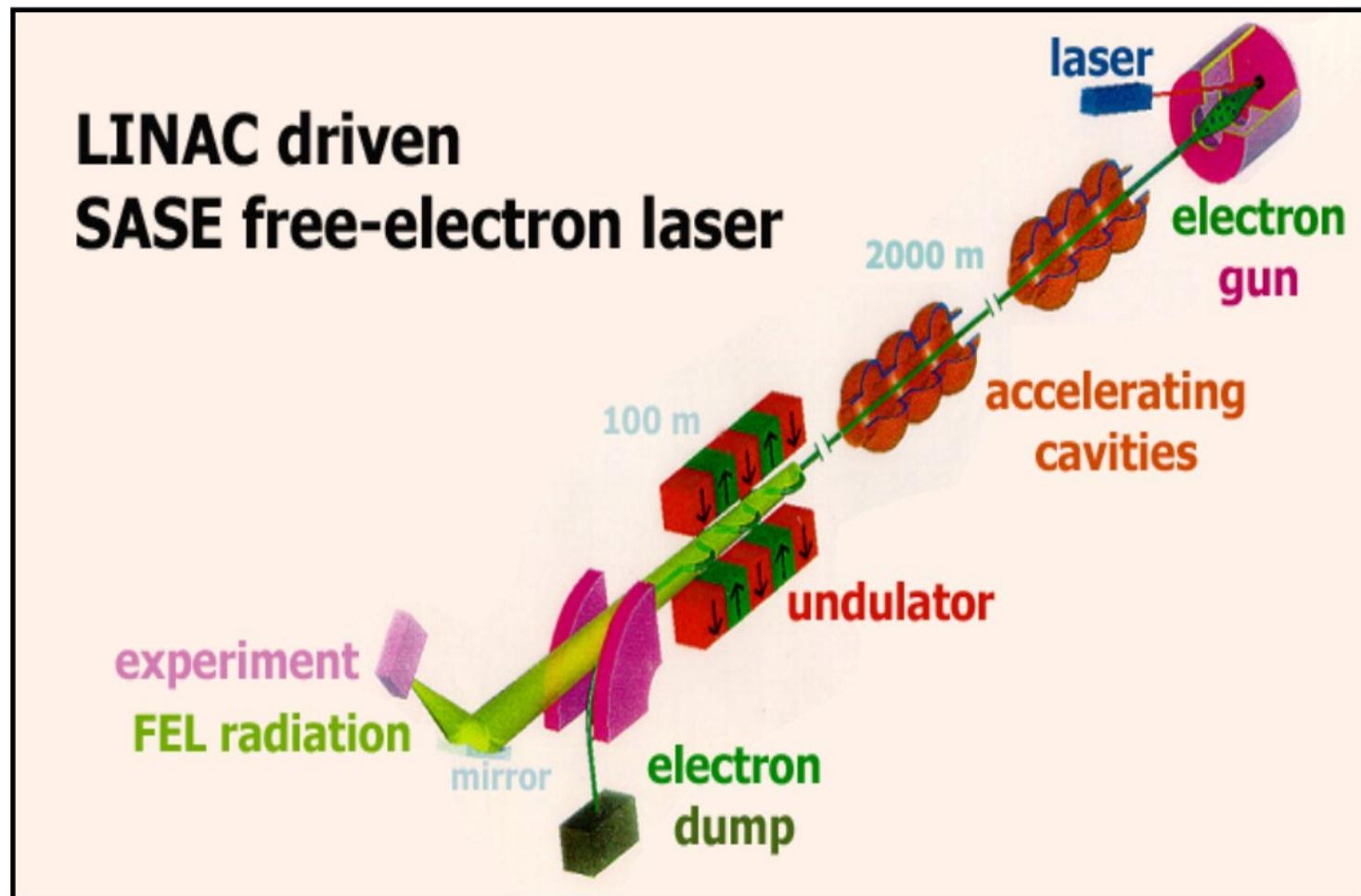
bandwidth: $\frac{\Delta\lambda}{\lambda} \sim \frac{1}{nN}$



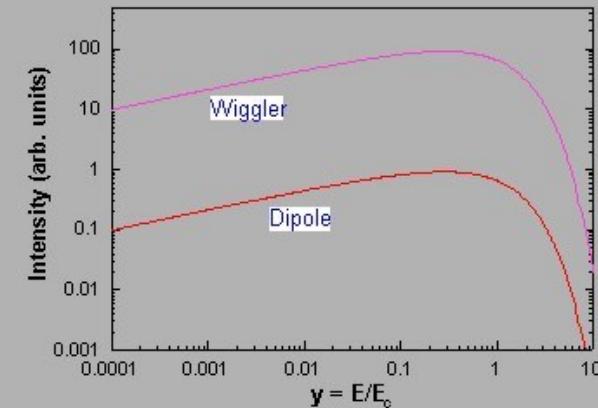
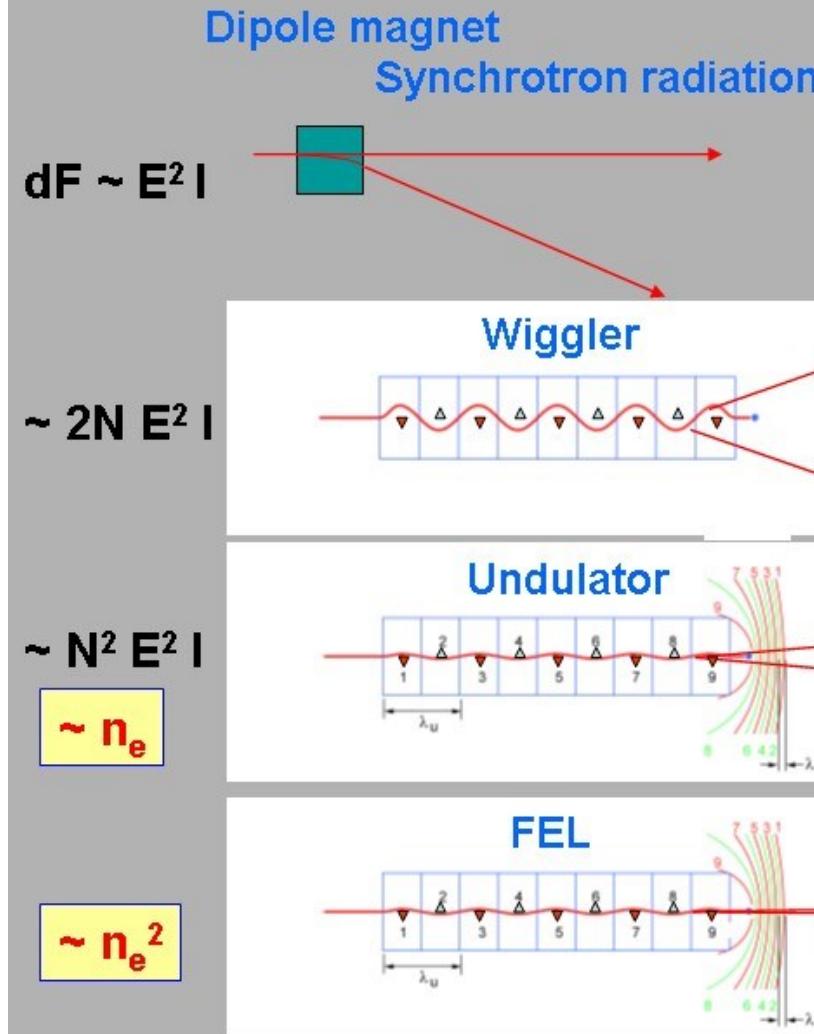
Towards Diffraction Limited Light Sources: MAX IV (Lund)



Free Electron Lasers (FELs)



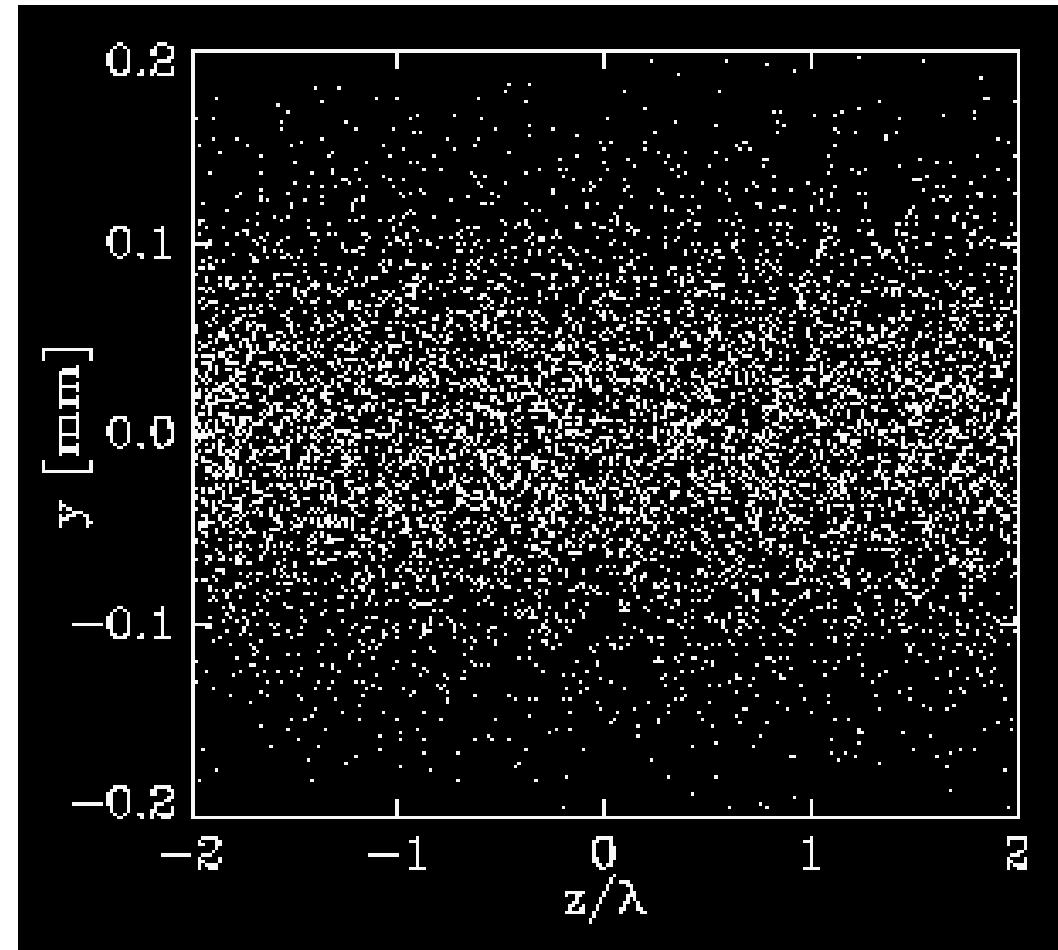
Synchrotron and FEL Sources



The radiation emitted by a single electron in subsequent oscillations in an undulator is in phase. Radiation from different electrons is NOT (positional disorder in bunch).

"Phasing" is achieved via positional order in the bunch (micro-bunching) with a period equal to the x-ray wavelength.

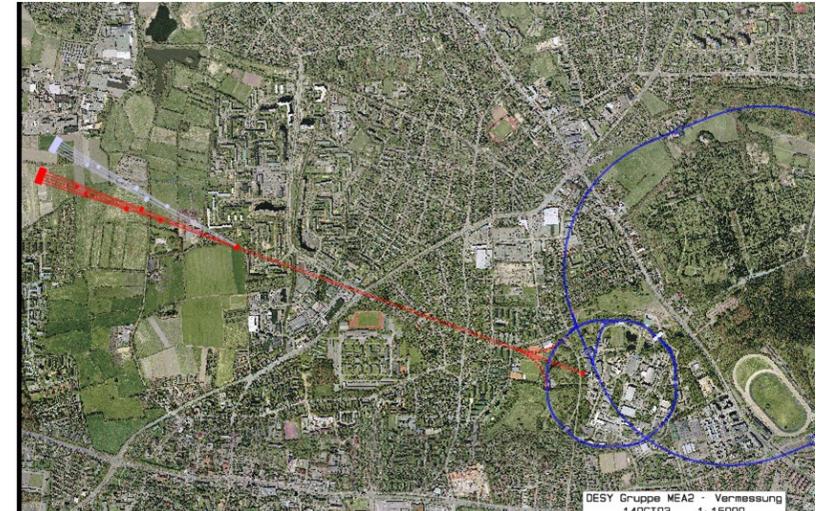
Electron Bunching



GENESIS – simulation for TTF parameters

Courtesy Sven Reiche
(UCLA)

VUV and X-Ray FELs



Brilliance

$$B = \frac{\text{photons}}{\text{s mm}^2 \text{ mrad}^2 0.1\% \text{ BW}}$$

