#### Methoden moderner Röntgenphysik I + II: Struktur und Dynamik kondensierter Materie

Vorlesung zum Haupt/Masterstudiengang Physik SS 2012 M. v. Zimmermann

#### <u>martin.v.zimmermann@desy.de</u> HASYLAB at DESY building 25b, room 222, phone 8998 2698

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### Materials Science

- 10.5. correlated electron systems structural properties
- 15. 5. correlated electron systems magnetic properties
- 22.5. high–Tc superconductors
- 24.5. charge density waves

#### correlated electron materials: overview

- phase transitions
- structural phase transition of SrTiO<sub>3</sub>
- x-ray diffraction to investigate phase transitions
- structural aspects of transition metal oxides
- orbital and charge order in La<sub>1-x</sub>Ca<sub>x</sub>MnO<sub>3</sub>
- resonant scattering to study orbital/charge order
- magnetic properties of transition metal oxides
- magnetic scattering
- resonant magnetic scattering

### Phase transitions

examples:

- solid liquid gas
- structural phase transition (SrTiO<sub>3</sub>)
- magnetic phase transition
- Mott-metal-insulator transition
- macroscopic quantum phenomena (superconductivity, suprafluidity)
- quantum phase transitions (at zero temperature, driven by pressure, magnetic field)
- glass transitions (amorphous solids, spin-glasses, quasi-crystals) (non-equilibrium states)

# classification of phase transitions

Ehrenfest classification:

smoothness of the chemical potential  $\mu$ First order if the entropy s =  $-\partial \mu / \partial T$  is discontinuous at the transition.

Problem: derivatives of  $\mu$  can diverge as a transition is approached.

Modern classification:

Fist order transitions have non-zero latent heat. Are also called discontinuous.

All other transitions are continuous phase transitions.

#### structural phase transition of SrTiO<sub>3</sub>

- phase transition breaking of symmetry
- stable structure at temperature T determined by minimum of the free energy  $F = U T \cdot S$
- Orderparameter Q

Q=0 in the disordered phase

Q=1 in the completely ordered phase

- Phase transition at temperature T<sub>c</sub>
- For continuous phase transitions, ordered and disordered regions form at  $T_c$  with out energy cost critical fluctuations



#### Landau theory

#### phenomenological description of phase transitions

 $F(Q,T) = 1/2aQ^2 \ + \ 1/3bQ^3 \ + \ 1/4cQ^4 \ + \ \dots$ 

$$\left. \frac{\partial F}{\partial Q} \right|_{Q_o} = 0 \text{ und } \left. \frac{\partial^2 F}{\partial^2 Q} \right|_{Q_o} > 0$$

$$a > 0$$
 :  $a = a'(T - T_c)$   $b=0$ 

$$F(Q,T) = 1/2a'(T-T_c)Q^2 + 1/4cQ^4$$

$$Q_o^2(T) = \begin{cases} 0 & \forall T > T_c \\ \frac{a'}{c}(T_c - T) & \forall T < T_c \end{cases}$$
$$\implies \quad Q_o(T) \sim (T_c - T)^\beta \text{ mit } \beta = 0.5$$

#### β critical exponent

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#### Susceptibility - correlation function

$$\mathcal{F} = \frac{\partial F}{\partial Q}\Big|_{T} \qquad \qquad \chi(T) = \frac{\partial Q}{\partial \mathcal{F}}\Big|_{\mathcal{F}=0}$$
$$\chi(T) = \begin{cases} \frac{1}{a'(T-T_{c})} & \forall T > T_{c} \\ \frac{1}{2a'(T_{c}-T)} & \forall T < T_{c} \end{cases}$$
$$\implies \chi(T) \sim |T_{c} - T|^{-\gamma} \quad \text{mit } \gamma = 1$$

 $G(\vec{x},T) = \langle Q(\vec{x},T)Q(0,T) \rangle - \langle Q(T) \rangle^{2} = k_{B}T\chi(\vec{x},T)$ 

$$\chi(\vec{q},T) = \int d\vec{x} \, \exp(-i\vec{q}\vec{x}) \, \chi(\vec{x},T) \sim \int d\vec{x} \, \exp(-i\vec{q}\vec{x}) \, G(\vec{x})$$
  
mit  $G(\vec{x},T) \sim \frac{e^{-|\vec{x}|/\zeta}}{|\vec{x}|} \implies \chi(\vec{q},T) \sim \frac{1}{\kappa^2 + q^2}.$ 

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# Landau theory and beyond

- Landau theory is independent of the dimension of the system and dimension of the orderparameter, fails to describe fluctuations around  $T_c$ , good approximation for  $T \neq T_c$
- Landau-Ginzburg theory takes position dependent fields into account and describes behavior around  $T_{\rm c}$
- Renormalizing Group theory most complete theory to describe phase transitions. Results in proper values for critical exponents and could predict the scaling laws, the relation between different critical exponents.
- Predicts also the universality hypothesis, that the behavior at a phase transition is given only by the dimension of the system and the dimension of the orderparameter, but not the specific interactions.

#### example: structural phase transition in SrTiO3

perovskite structure: Pm3m (#221) lattice parameter a<sub>c</sub> below 105 K: I4/mcm (#140)  $a_t = \sqrt{2} a_c$ ,  $c_t$ orderprameter: spontaneous strain  $\phi^2 = c_t(T)/a_0(T) - 1$  $a_0(T) = 2/3 a(T) + 1/3 c(T)$ 



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# investigation of structural phase transitions by x-ray diffraction

Ist approach: determination of lattice parameters

2nd approach: determinations of intensity of high-temperature phase "forbidden" reflections. determination of the space group



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#### 3-axis diffractometer



#### diffractometer



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# investigation of structural phase transitions by x-ray diffraction

$$I_{Bragg} \sim |F_{hkl}|^2 \sim Q_o^2 \sim (T_c - T)^{2\beta}$$
$$I_{Fl}(\vec{q}, T) \sim \chi(\vec{q}, T) \sim \frac{1}{\kappa^2 + q^2}$$



#### soft mode transition

phonon energy: inelastic neutron scattering



static lattice distortion: x-ray diffraction

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#### correlated electron materials: transition metal oxides

- physical properties determined by interplay of charge, orbital, spin and lattice degrees of freedom
- high Tc superconductivity
- colossal magnetoresistance
- multiferroic behavior

H <sup>1</sup>	Periodic Table of the Elements															2 He	
Li 3	Be	4 ■ hydrogen ■ alkali metals						<ul> <li>poor metals</li> <li>nonmetals</li> <li>poble gases</li> </ul>					C 6	N <sup>7</sup>	08	۶ F	10 Ne
11 Na	12 Mg	<ul> <li>area in earth metals</li> <li>transition metals</li> </ul>						<ul> <li>none gases</li> <li>rare earth metals</li> </ul>					14 Si	15 P	16 S	17 Cl	18 Ar
19 K	Ca <sup>20</sup>	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr
37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53	54 Xe
55 Cs	56 Ba	57 La	72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Ti	82 Pb	83 Bi	84 Po	85 At	86 Rn
87 Fr	88 Ra	89 Ac	104 Unq	105 Unp	106 Unh	107 Uns	108 Uno	109 Une	110 Unn								
			58	59 Dr	60 Nd	61 Dm	62	63	64	65	66	67	68	69	70	71	
			Ce 00			F111	500	Eu 05	Gu	10	Dy	00	100	101	102	102	
			Th	Pa	U 92	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No	Lr	

#### correlated electron materials: transition metal oxides

3d electronic Eigenstates:  $R_n * Y_m^2(\Theta, \varphi)$ quantum numbers: n=3 (radial) l=2 (angular momentum)  $m=-2 \dots +2$  magentic (5-fold degenerate)

perovskite structure

in a cubic crystal field: e.g. LaMnO<sub>3</sub>

 $V(r) = \sum Z_i e^2/|r - R_i|$  Madelung Potential

in rectangular coordinates:  $V_4(r) = 5/2 V_{40} (x^4 + y^4 + z^4 - 3/5r^4)$ 



# cubic crystal field



crystal field splitting:



# Hund's rules

electrons occupy orbitals such that the gound state is characterized by:

- 1. the maximum value of the total spin S allowed by the exclusion principle
- 2. the maximum value of orbital angular momentum L consistent with S
- 3. Spin-orbit interaction:
  - J = |L + S| for more that half filled shell
  - J = |L S| for less than half filled shell



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# Jahn-Teller distortion



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#### cooperative Jahn-Teller distortion - orbital order



#### no change in lattice parameters

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#### resonant x-ray scattering



at Mn K-edge: |i>=1s|n>=4p



#### resonant x-ray scattering





at the absorption edge the atom form factor depends on the incident and scattered polarization:

$$f = f0 + \Delta f(\omega)$$
  

$$\Delta f(\omega) = \mathbf{e}^{t_{f}} \cdot f'(\omega) \cdot \mathbf{e}_{i}$$
  

$$f' = (f'_{\alpha,\beta}) = r_{0}/m \sum_{j} \frac{\langle Is \mid P_{\beta} \mid 4p_{j} \rangle \quad \langle 4p_{j} \mid P_{\alpha} \mid Is \rangle}{E(4p_{j}) - E(Is) - h\omega - i\Gamma/2}$$

$$f_{||} = \frac{r_0}{m} \frac{|\mathsf{D}|^2}{h(\omega - \omega_0) + 2\Delta - i\Gamma/2}$$

$$f_{\perp} = \frac{r_0}{m} \frac{|\mathsf{D}|^2}{h(\omega - \omega_0) - \Delta - i\Gamma/2}$$

with  $\langle Is | P_{\alpha} | 4p_j \rangle = D \delta_{\alpha_j}$ 

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# (3 0 0) Intensity

$$I(\mathbf{Q}) = I_0 \cdot |F(\mathbf{Q})|^2 = I_0 \cdot |\sum_l o_l f_l e^{i\mathbf{Q}.\mathbf{b}_l} e^{-\mathbf{Q}^t.U_l.\mathbf{Q}}|^2$$
  

$$F(300) = f_1(\omega, \mathbf{e}_i, \mathbf{e}_f) - f_2(\omega, \mathbf{e}_i, \mathbf{e}_f)$$
  

$$= \mathbf{e}_f^t.[\hat{f}_1(\omega) - \hat{f}_2(\omega)].\mathbf{e}_i$$
  

$$\doteq \mathbf{e}_f^t.\hat{F}(300).\mathbf{e}_i \quad ,$$

$$\hat{F}(300) = \hat{f}_1 - \hat{f}_2 = \begin{pmatrix} f_{\perp} - f_{\parallel} & 0 & 0\\ 0 & f_{\parallel} - f_{\perp} & 0\\ 0 & 0 & 0 \end{pmatrix}.$$

$$I = I_0 \cdot \left| \mathbf{e}_f \cdot (U \hat{F}(300) U^t) \cdot \mathbf{e}_i \right|^2, \text{ where}$$
$$U \hat{F}(300) U^t = \begin{pmatrix} 0 & f_{||} - f_{\perp} & 0\\ f_{||} - f_{\perp} & 0 & 0\\ 0 & 0 & 0 \end{pmatrix}.$$

#### azimuthal dependence



#### resonant scattering at transition metal L-edges

- direct sensitivity for d-electrons, thus orbital order is probed directly, not the Jahn-Teller distortion as for k-edge
- large resonant enhancement for magnetic order
- small momentum transfers achievable, (100) of LaMnO3 out of reach
- surface sensitive
- ultra high vacuum conditions necessary

# doping – charge order



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#### charge/orbital order resonant diffraction



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#### domains - correlation length



1.2

Bragg

• charge orbital

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ΦΦ

Φ\_Φ

0.008

DDDD DDDDD

#### summary

solids state phase transitions order parameter power laws with critical exponents correlation length superlattice reflection

transition metal oxides symmetry of d-electrons in cubic crystal field Jahn-Teller effect resonant x-ray scattering

#### literature

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#### exercises

Is it possitble to measure orbital order (magnetic order) in LCMO at the Mn L-edge? At which position of (h,k,l) can magnetic scattering be measured?