

# Methoden moderner Röntgenphysik I + II: Struktur und Dynamik kondensierter Materie

Vorlesung zum Haupt/Masterstudiengang Physik SS 2011  
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# Materials Science

6. 5. Martin v. Zimmermann

10. 5. Martin v. Zimmermann

12. 5. Hermann Franz

correlated electron  
materials –  
structural properties  
correlated electron  
materials –  
magnetic properties  
glasses

# correlated electron materials: overview

- phase transitions
- structural phase transition of  $\text{SrTiO}_3$
- x-ray diffraction to investigate phase transitions
- structural aspects of transition metal oxides
- orbital and charge order in  $\text{La}_{1-x}\text{Ca}_x\text{MnO}_3$
- resonant scattering to study orbital/charge order
  
- magnetic interactions in transition metal oxides
- Mott insulator
- colossal magneto resistance (CMR) effect
- magnetic x-ray scattering

# exchange interactions

combination of Coulomb interaction and Pauli principle

$$J \sim - \int \Psi_x^*(\mathbf{r}_1) \Psi_y(\mathbf{r}_1) (e^2/r_{12}) \Psi_y^*(\mathbf{r}_2) \Psi_x(\mathbf{r}_2)$$

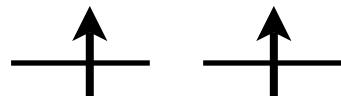
one-band Hubbard model:

$$\begin{aligned} H &= -\sum t_{ij} (c_{i\sigma}^\dagger c_{j\sigma}) + U \sum n_{i\uparrow} n_{i\downarrow} \\ &= H_{\text{kin}} + H_U \end{aligned}$$

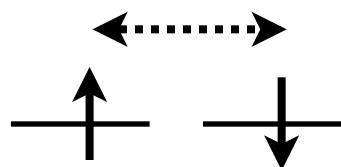
$t_{ij}$  hopping amplitude between nn sites  $\langle ij \rangle$   
 $c_{i\sigma}^\dagger$  creates an electron with spin  $\sigma$  at lattice site  $i$   
 $U$  Coulomb repulsion  
 $n_{i\sigma}$  number of electrons at site  $i$  with spin  $\sigma$

$t \gg U$  : metallic system

$t \ll U$  : insulator with one electron per site



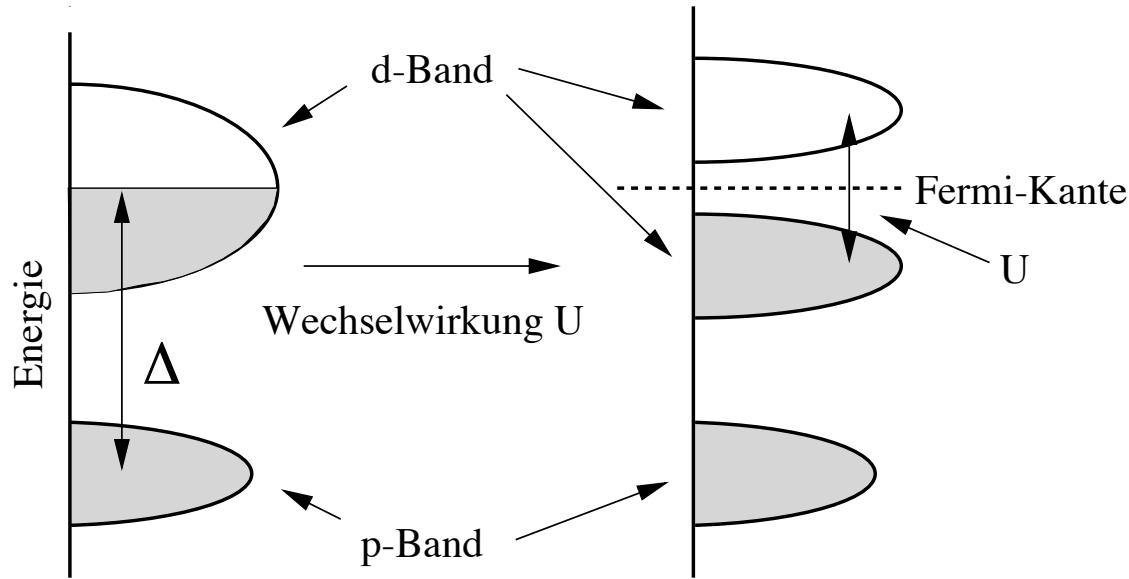
$$\Delta E = 0$$



$$\Delta E = -2t^2/U$$

superexchange:  
antiferromagnetic

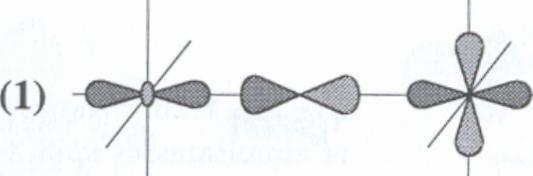
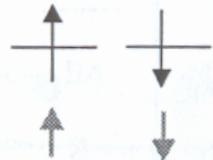
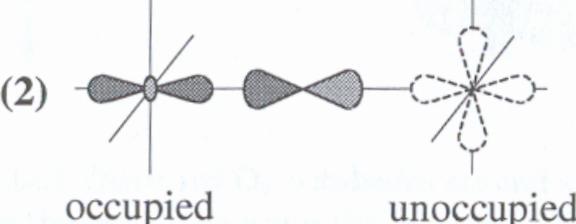
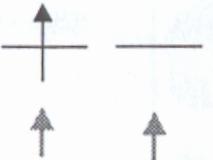
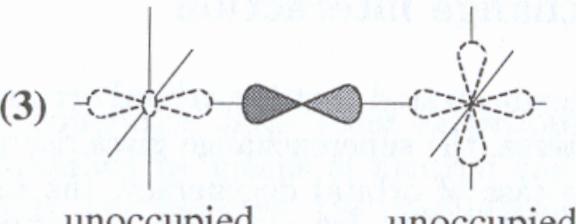
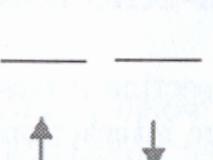
# Mott insulator



strongly correlated electron systems: transition metal oxides  
high-T<sub>c</sub> superconductors  
CMR-manganites ...

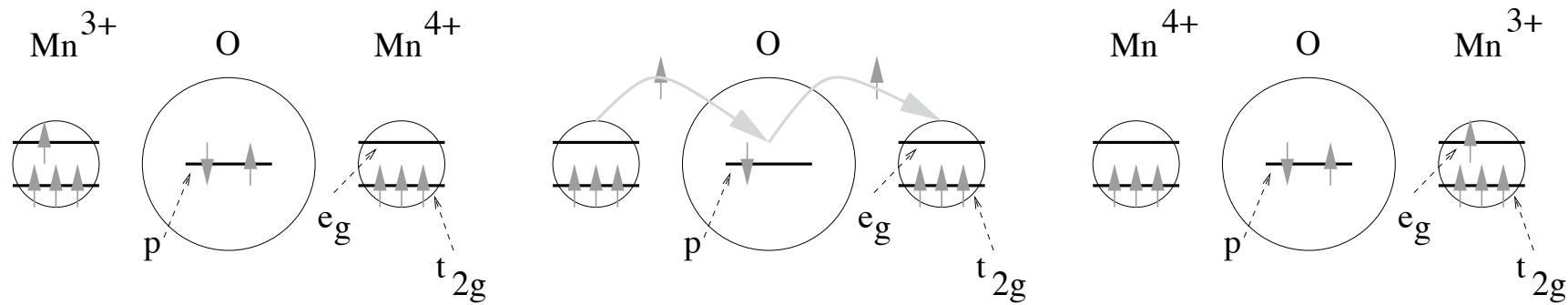
# GKA-rules (Goodenough-Kanamori-Andersen)

orbital dependent exchange interaction

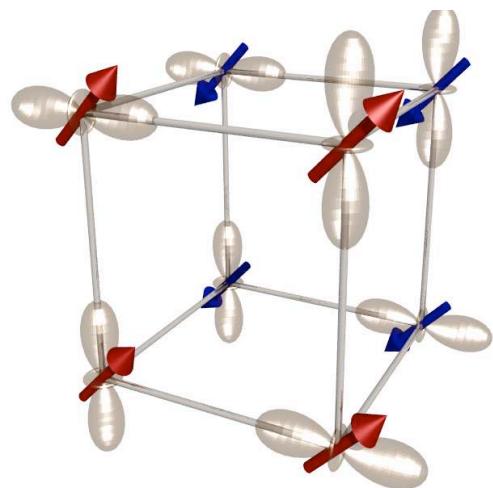
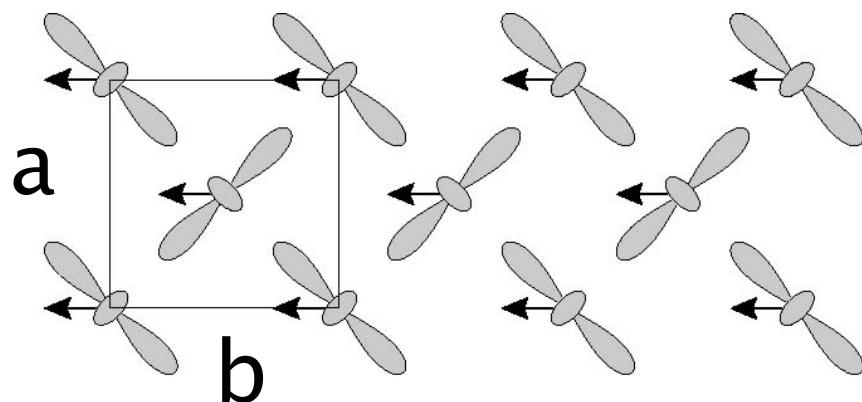
Configuration example	Exchange coupling
(1) 	 antiferromagnetic
(2) 	 ferromagnetic
(3) 	 antiferromagnetic

# double exchange interaction

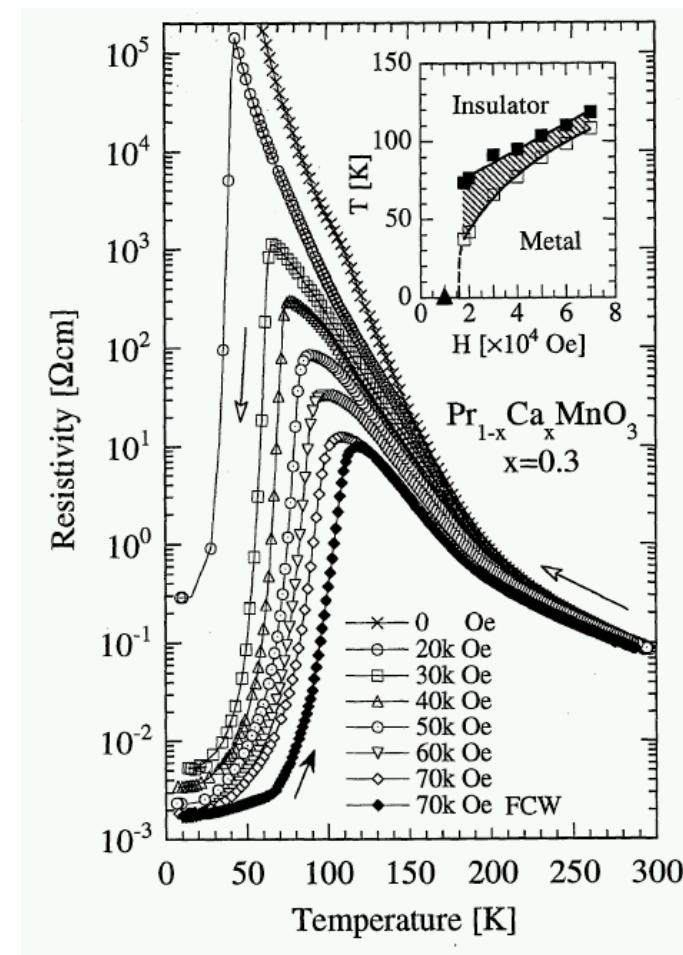
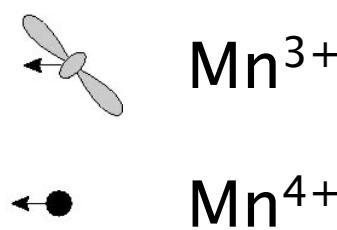
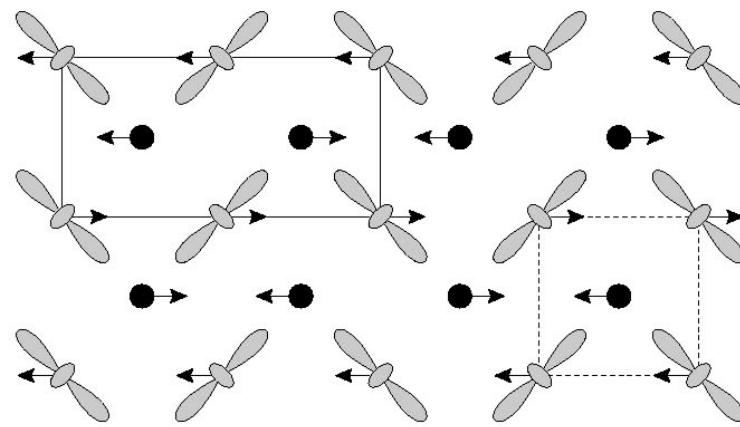
ferromagnetic interaction between different ions due to Hund's coupling



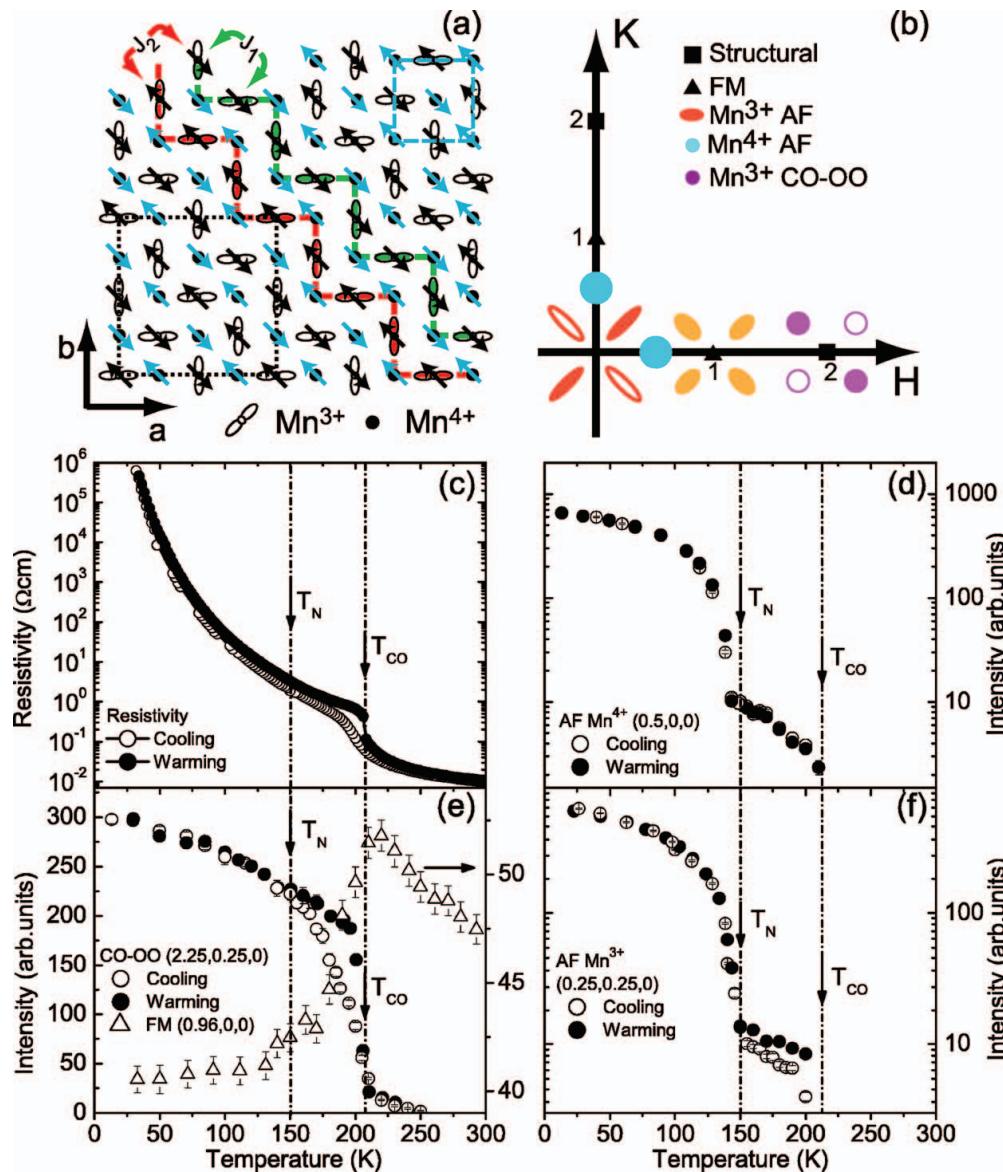
# magnetism of LaMnO<sub>3</sub>



# magnetism of $\text{La}_{0.5}\text{Ca}_{0.5}\text{MnO}_3$ and colossal magneto resistance (CMR) effect



# magnetism of manganites



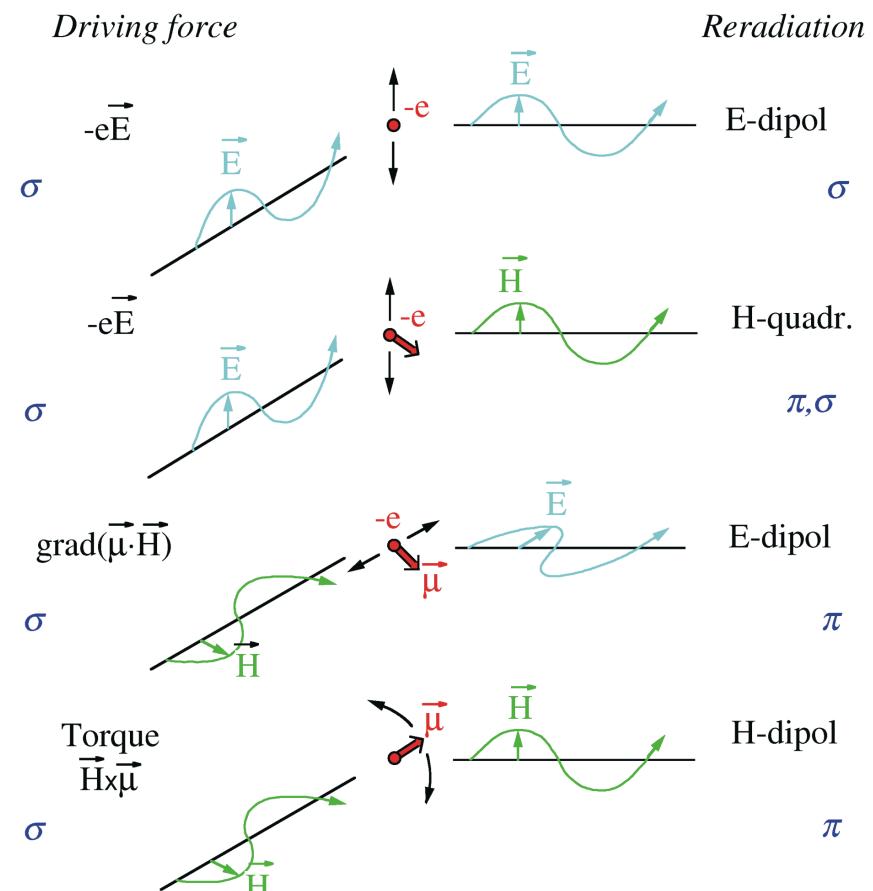
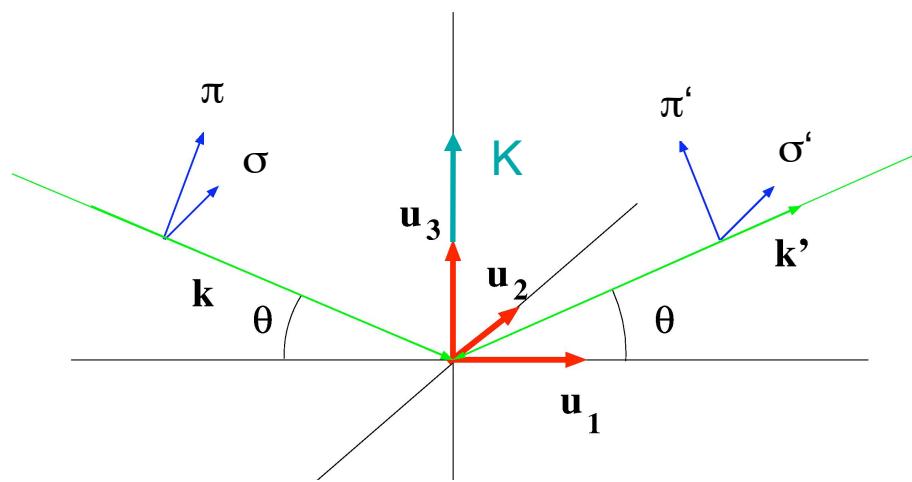
F. Ye et al.  
Phys. Rev. B 72, 212404 (2005)

# magnetic x-ray scattering

Synchrotronstrahlung linear polarisiert in Ringebene

Streugeometrie vertikal

→  $\sigma$  – polarisierte einfallende Strahlung



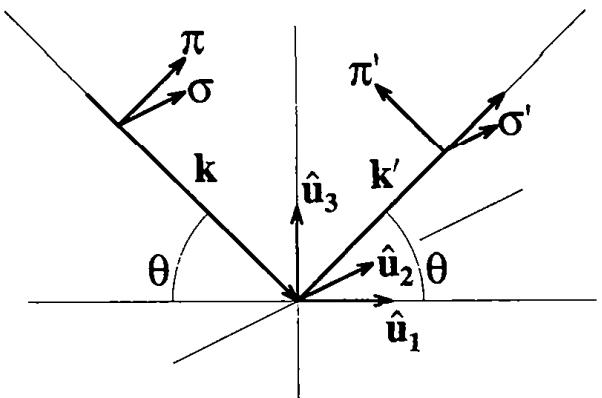
# magnetic x-ray scattering

$$\frac{d\sigma}{d\Omega} \Big|_{\varepsilon \rightarrow \varepsilon'} = [e^2/mc^2]^2 \left| \langle M_C \rangle_{\varepsilon' \varepsilon} + i(\lambda_C/d) \langle M_M \rangle_{\varepsilon' \varepsilon} \right|^2$$

$$\lambda_c = h/mc = 0.024 \text{ \AA} \text{ electron Compton length}$$

	$\sigma$	$\pi$
$\sigma'$	$S_2 \cos \theta$	$[(L_1 + S_1) \cos \theta + S_3 \sin \theta] \sin \theta$
$\pi'$	$[-(L_1 + S_1) \cos \theta + S_3 \sin \theta] \sin \theta$	$[2L_2 \sin^2 \theta + S_2] \cos \theta$

	$\sigma$	$\pi$
$\sigma'$	$\rho(\mathbf{Q})$	0
$\pi'$	0	$\rho(\mathbf{Q})(\cos 2\theta)$



spin moment:  $S = S_1 \cdot \hat{\mathbf{u}}_1 + S_2 \cdot \hat{\mathbf{u}}_2 + S_3 \cdot \hat{\mathbf{u}}_3$

orbital monment:  $L = L_1 \cdot \hat{\mathbf{u}}_1 + L_2 \cdot \hat{\mathbf{u}}_2 + L_3 \cdot \hat{\mathbf{u}}_3$

charge density:  $\rho(Q)$

# magnetic x-ray scattering

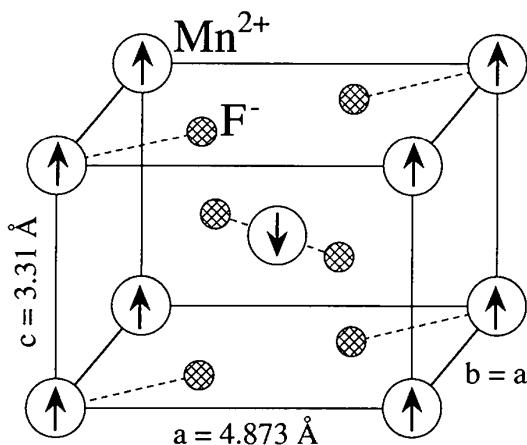
- ratio charge scattering / magnetic scattering =  $(\lambda_c/d)^2 \sim 10^{-6}$
- x-ray diffraction allow to distinguish between orbital and spin contribution by polarization.
- Components S2 and L2 perpendicular to the scattering plane preserve the photon polarization.
- Components in the scattering plane components alter the polarization  $\sigma \leftrightarrow \pi$ .
- high energy x-ray limit (  $\cos(\theta) \rightarrow 0$ ;  $E < 80$  keV )

$$d\sigma/d\Omega|_{\varepsilon \rightarrow \varepsilon'} = r_0^2 | \langle M_C \rangle_{\varepsilon \varepsilon'} + i(\lambda_C/d) \langle M_M \rangle_{\varepsilon \varepsilon'} |^2.$$

$$\langle M_M \rangle = \begin{array}{c|cc} & \sigma & \pi \\ \hline \sigma' & S_2 & 0 \\ \pi' & 0 & S_2 \end{array}.$$

$$(d\sigma/d\Omega)_{\text{magnetic}} = r_0^2 (\lambda_C/d)^2 |S_2|^2.$$

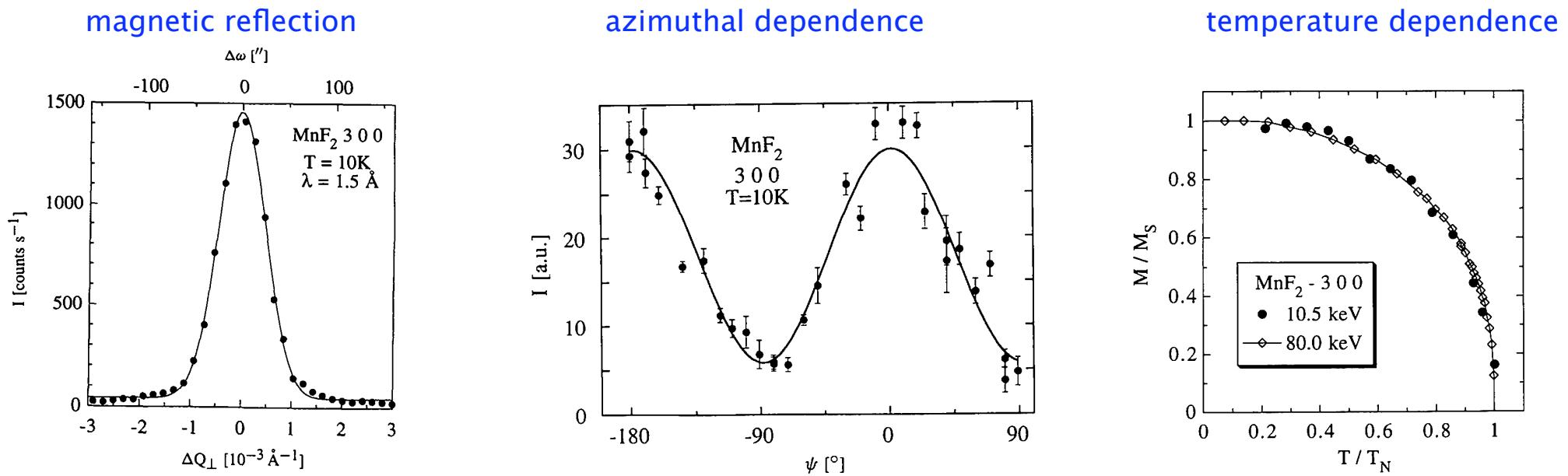
# magnetic x-ray scattering: example MnF<sub>2</sub>



magnetic ordering wave vector: (1, 0, 0)

moment direction: || c-axis

T. Brückel et al.  
Acta Cryst. (1996) A52, 427



# Scattering scheme with polarization analysis

Non-resonant magnetic scattering amplitude [Blume & Gibbs]

$$f^{mag} = -i \frac{\hbar\omega}{mc^2} \begin{pmatrix} f^{\sigma\sigma'} & f^{\sigma\pi'} \\ f^{\pi\sigma'} & f^{\pi\pi'} \end{pmatrix}$$

$$= -i \frac{\hbar\omega}{mc^2} \begin{pmatrix} S_2 \sin 2\theta & -2 \sin^2 \theta [\cos \theta (L_1 + S_1) - S_3 \sin \theta] \\ 2 \sin^2 \theta [\cos \theta (L_1 + S_1) + S_3 \sin \theta] & \sin 2\theta [2L_2 \sin^2 \theta + S_2] \end{pmatrix}$$

Determination of L/S ratio  
Magnetic structure determination

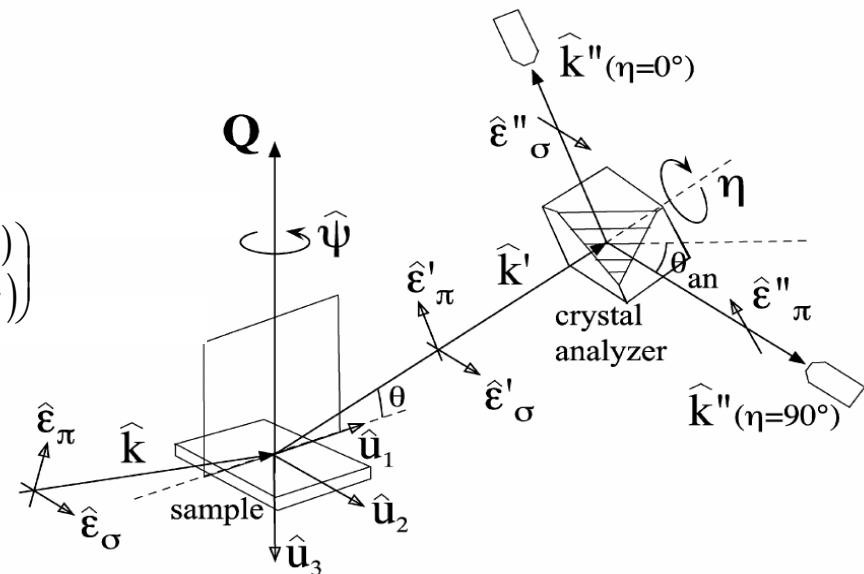
Resonant magnetic scattering amplitude (dipole transitions) [Hill & McMorrow]

$$f_{E1}^{res-mag} = \begin{pmatrix} f^{\sigma\sigma'} & f^{\sigma\pi'} \\ f^{\pi\sigma'} & f^{\pi\pi'} \end{pmatrix}$$

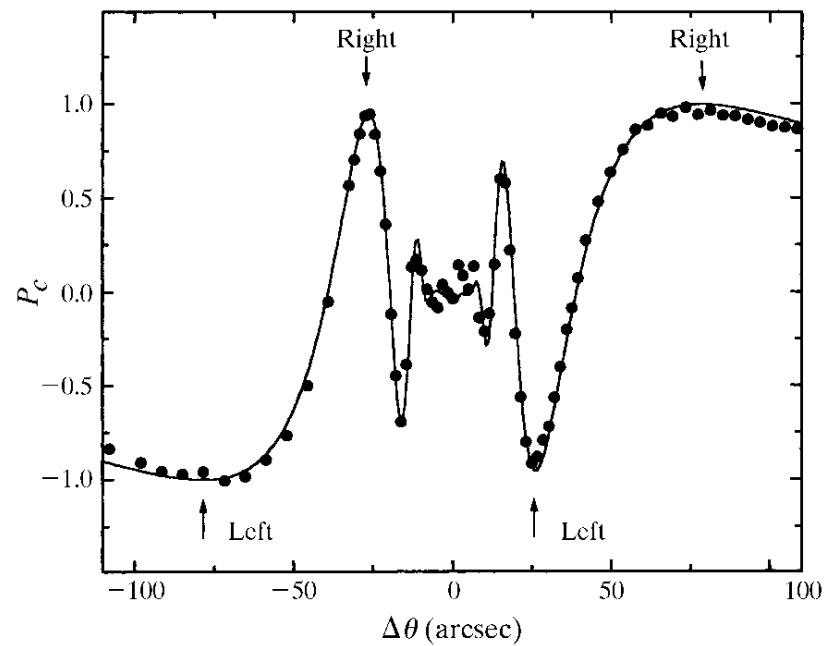
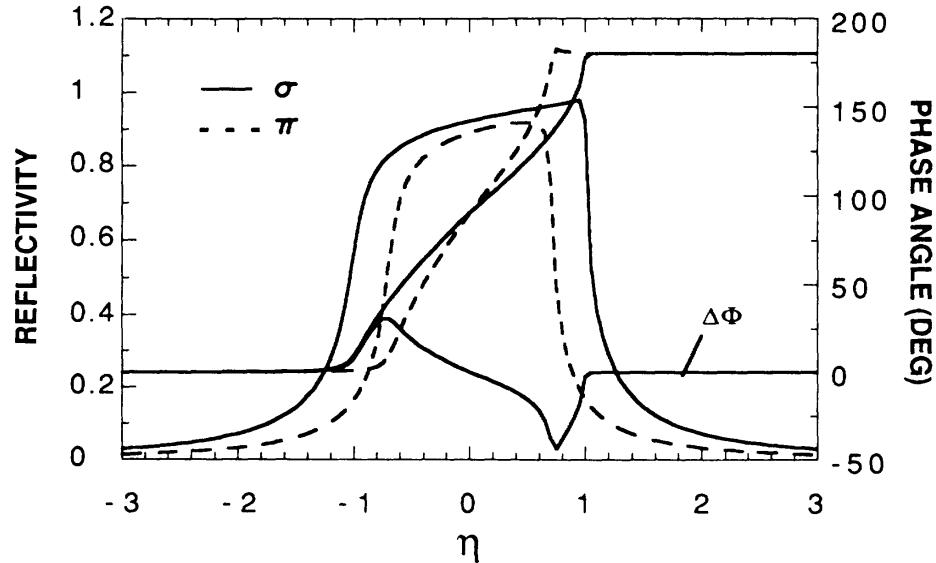
$$= F^0 - iF^1 \begin{pmatrix} 0 & m_1 \cos \theta + m_3 \sin \theta \\ m_3 \sin \theta - m_1 \cos \theta & -m_2 \sin 2\theta \end{pmatrix}$$

$$+ F^2 \begin{pmatrix} m_2^2 & m_2(m_1 \sin \theta - m_3 \cos \theta) \\ m_2(m_1 \sin \theta + m_3 \cos \theta) & -\cos^2 \theta (m_1^2 \tan \theta + m_3^2) \end{pmatrix}$$

Strong intensities due to resonance enhancement  
Element sensitivity at absorption edges  
Magnetic structure determination

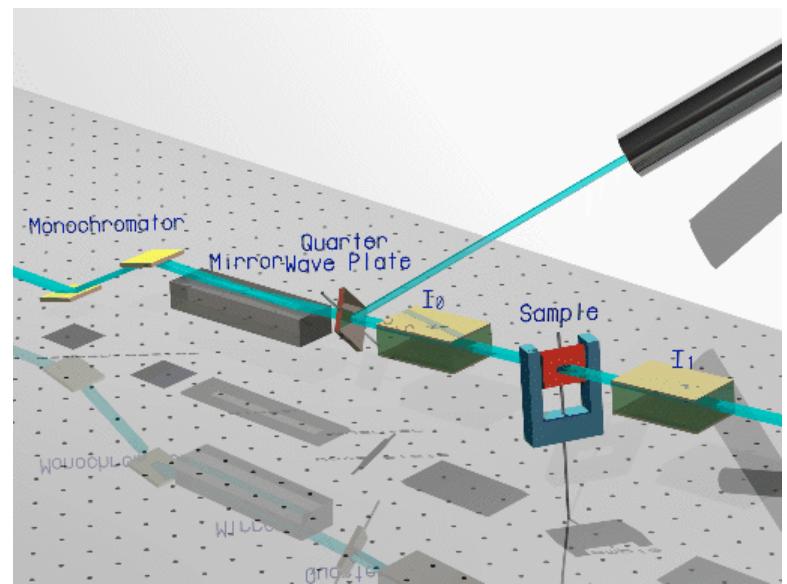


# quarter wave phase plate – circular polarization

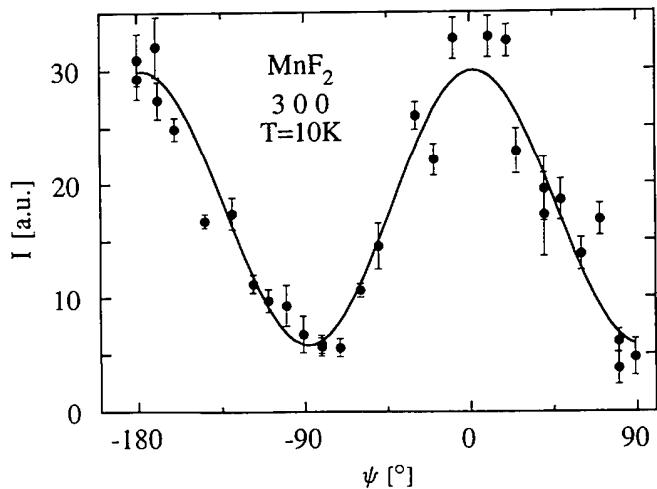


control of incident polarization:  
circular: left/right  
linear:  $\sigma$  /  $\pi$

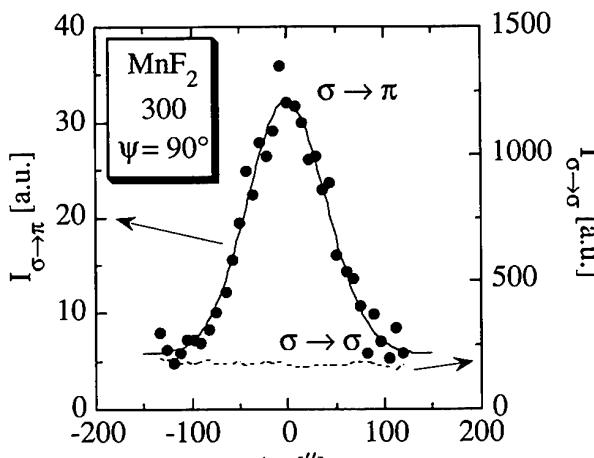
Battermann  
Phys. Rev. B 45, 12677 (1992)



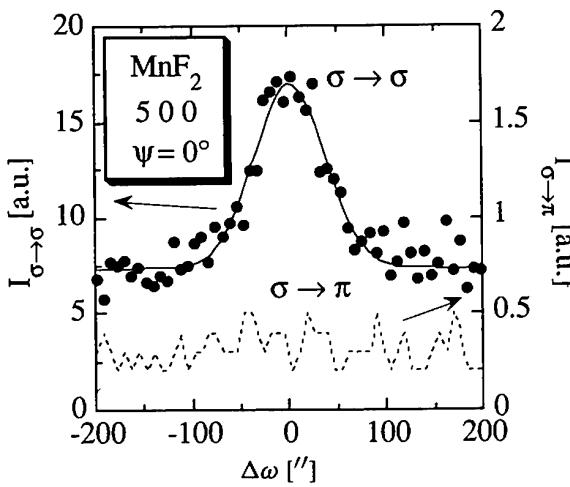
# polarization resolved magnetic scattering



T. Brückel et al.  
Acta Cryst. (1996) A52, 427



(a)



# summary

- magnetic interactions in transition metal oxides
- Mott insulator
- colossal magneto resistance (CMR) effect
- magnetic x-ray scattering

# exercises

Is it possible to observe resonant scattering from orbital order (magnetic order) in LaMnO<sub>3</sub> (lattice parameter 5.4 Angstroem) at the Mn L-edge?

At which position of (h,k,l) can magnetic scattering and scattering from orbital order be measured in LaMnO<sub>3</sub> and La<sub>0.5</sub>Ca<sub>0.5</sub>MnO<sub>3</sub>?

What does Erna need to do, if she wants to do polarization resolved x-ray diffraction on her rotating anode source.