



# Master Kurs im SS 2011

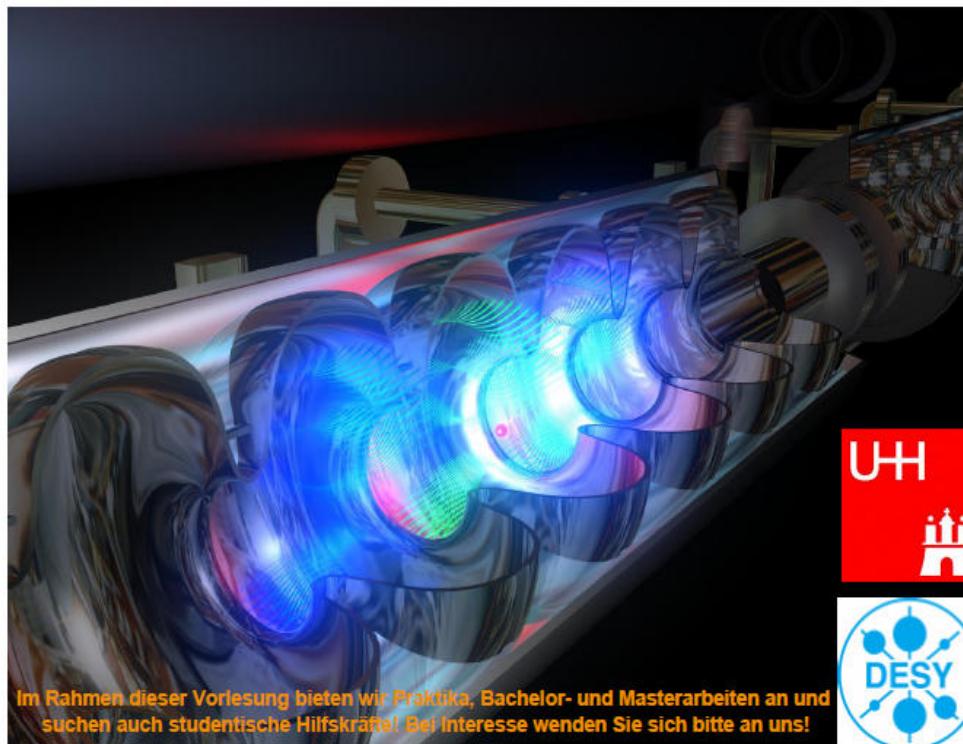
G. Grübel, M. Martins, W. Wurth, E. Weckert

## Methoden moderner Röntgenphysik II

Vierstündige Vorlesung mit Übungen und Proseminar  
(Seminar Raum 3)

Di 14:00 – 15:30, Do 10:15 – 11:45

Beginn: 05.04.2011, 14:00



# Methoden moderner Röntgenphysik II

Vorlesungszeit: 4.4. – 16.7.

Ferien: 13.6 – 24.6.

66-360: Methoden moderner Roentgenphysik II

Di: 14:00-15:30 SemRm 3

Do: 10.15-11.45 „

Beginn: 5.4.

66-361: Uebungen

Di: 16:00-17.30 SemRm3 ab ????.

66-505: ProSeminar (for Batchelor students)

Vorbesprechung 5.4. 15:30 SemRm 3

# Methoden moderner Röntgenphysik II

- 5.4. - 19.4. 2011 Wiederholung + Kohärenz Christian Gutt
- 21.4. - 3.5. 2011 Weiche Materie Stephan Roth
- 5. 5. 2011 Glass Physik Hermann Franz
- 10.5. -12.5.2011 Magnetismus Martin v. Zimmermann
- 17.5.- 14.7.2011 Festkörperspektroskopie Wilfried Wurth
- Im obigen Block Inelastische Röntgenstreuung Wolfgang Caliebe und Wolfgang Drube

# Literature

Basic concepts: [Elements of Modern X-Ray Physics](#)

J. A. Nielsen and D. McMorrow, J. Wiley&Sons (2001)

[X-Ray Diffraction](#)

B.E. Warren, DOVER Publications Inc., New York

[Principles of Optics](#)

M.Born and E. Wolf, Cambridge University Press, 7<sup>th</sup>. ed.

[Soft X-rays and Extreme Ultraviolet Radiation](#)

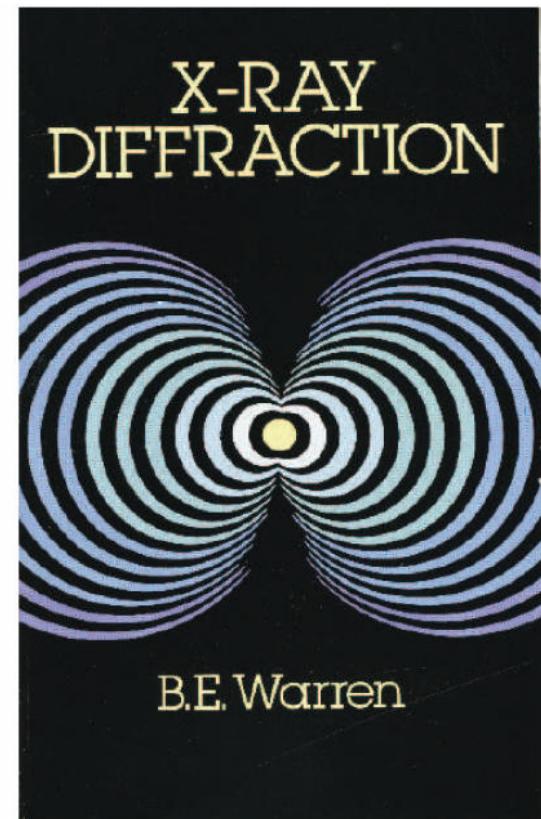
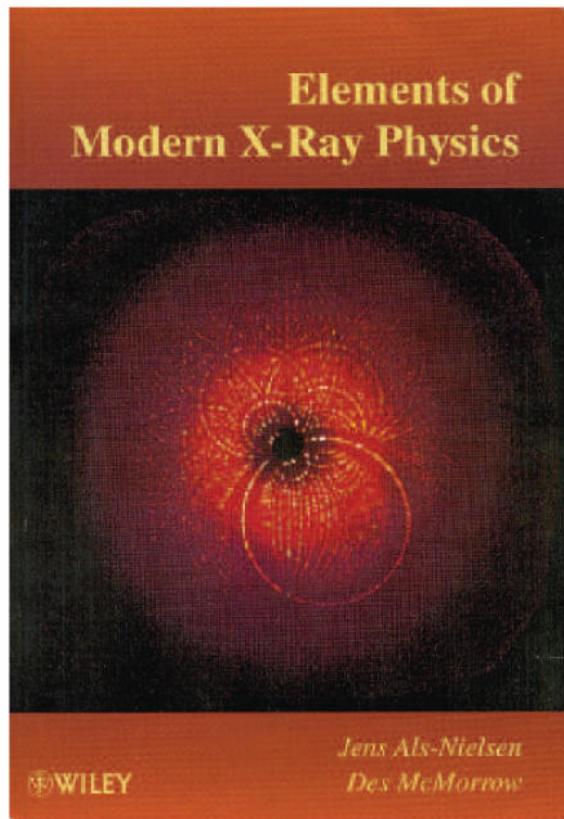
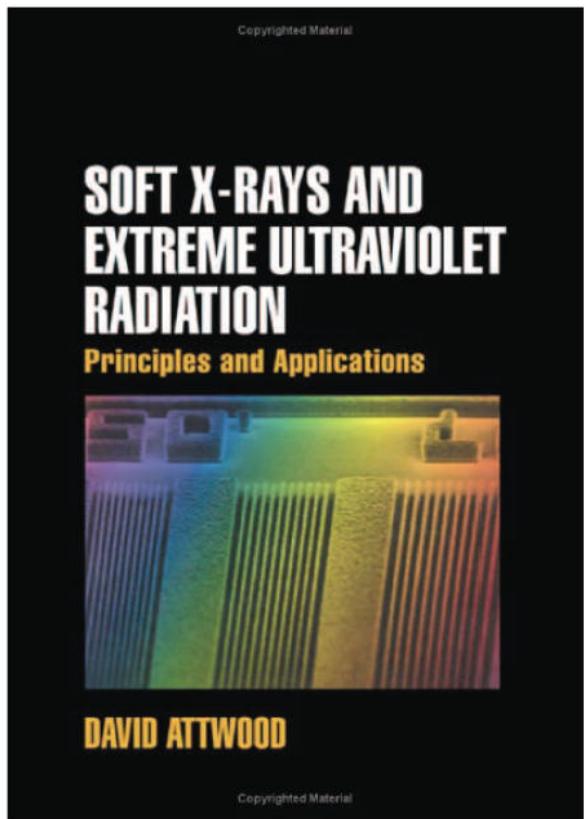
D. Attwood, Cambridge University Press (2000)

<http://www.coe.berkeley.edu/AST/sxreuv/>)

[Physik der Teilchenbeschleuniger und](#)

[Synchrotronstrahlungsquellen](#)

K. Wille, Teubner Studienbücher 1996



[http://hasylab.desy.de/science/studentsteaching/lectures/index\\_eng.html](http://hasylab.desy.de/science/studentsteaching/lectures/index_eng.html)

 **PHOTON SCIENCE** 

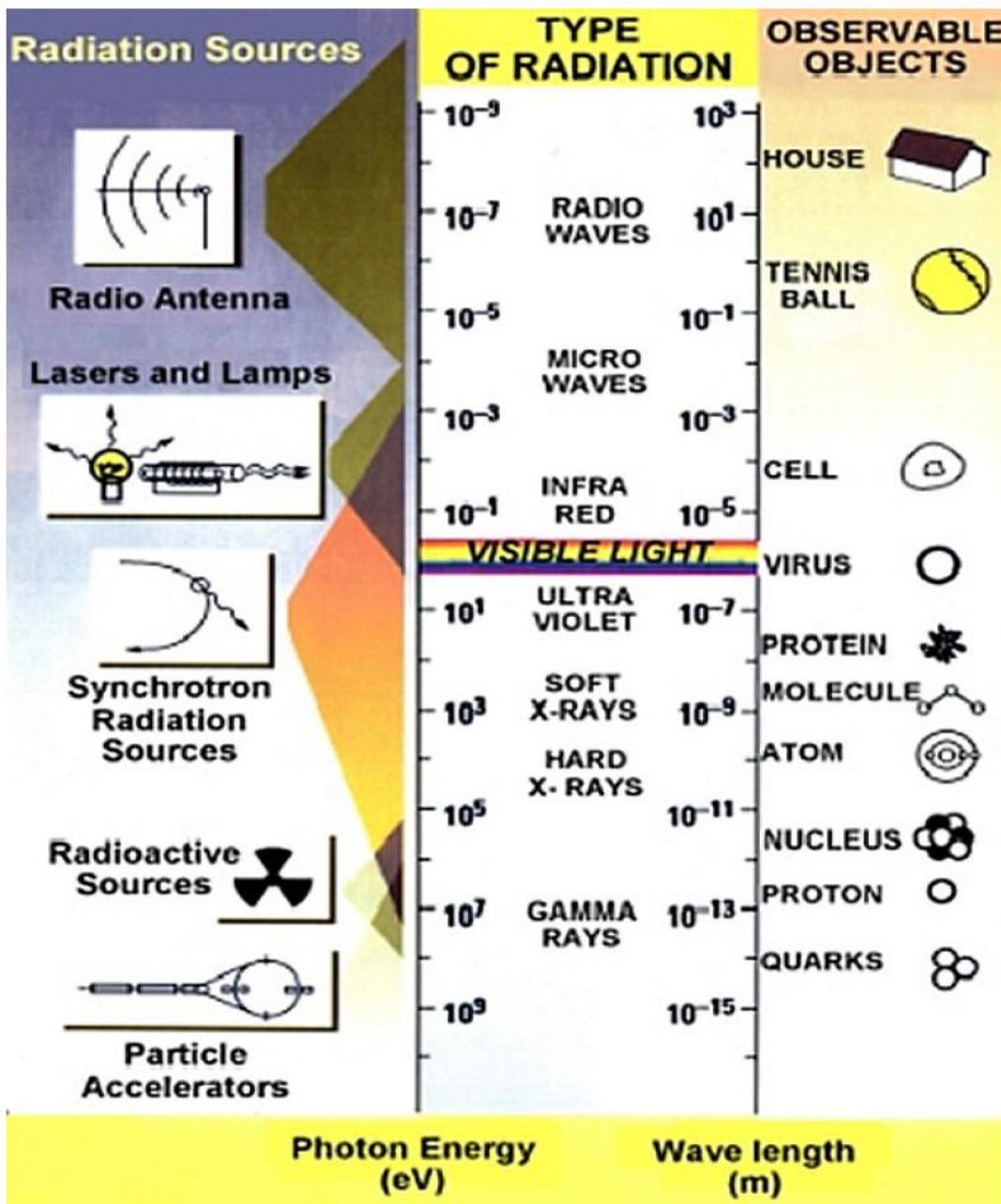
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Welcome to the student portal for Photon Science at DESY!

Inside you will find all the information you need about the light sources themselves and your opportunities to take part in this booming area of research.

<p><b>Primer</b></p> <p>In this section, you can find out more about the facilities themselves and about the theory that is behind the generation of synchrotron light at a storage ring and the actual experiments.</p> 	<p><b>Primers</b></p> <p><i>In this section, you can find out more about the facilities themselves and about the theory that is behind the generation of synchrotron light at a storage ring and the actual experiments.</i></p>
<p><b>Opportunities</b></p> <p><i>Click here to find more about the opportunities that DESY has in store for your academic career in photon science.</i></p> 	
	<p><b>Graduate Schools</b></p> <p><i>Graduate schools offer special programmes for participating PhD students. This includes lectures, colloquia, and workshops with experts from university and DESY.</i></p>
<p><b>Open Positions</b></p> <p><i>Several groups at HASYLAB / DESY are seeking bachelor/ diploma / master / PhD students for photon science research projects. The supervision of the theses will be done in cooperation with the University of Hamburg.</i></p> 	



X-rays  
 =  
 electromagnetic radiation  
 =  
 Wavelength  
 $(\lambda[\text{\AA}] = 12.398/\text{E[keV]})$   
 =  
 Object Size  
 =  
 Angstroms  
 for Condensed Matter Research

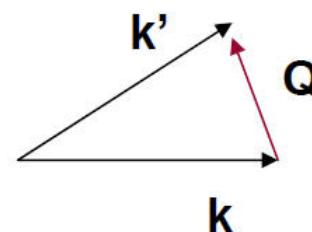
# Scattering of X-rays

consider a monochromatic plane (electromagnetic) wave with wavevector  $\mathbf{k}$ :

$$\mathbf{E}(\mathbf{r}, t) = \epsilon E_0 \exp\{i(\mathbf{k}\mathbf{r} - \omega t)\} \quad \text{with } |\mathbf{k}| = 2\pi/\lambda$$

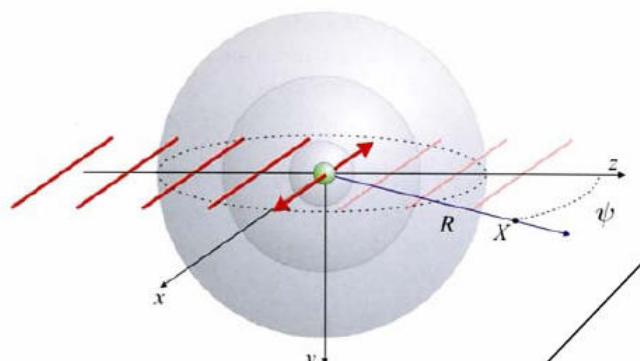
elastic scattering:

$$\hbar \mathbf{k}' = \hbar \mathbf{k} + \hbar \mathbf{Q}$$



## Scattering by a single electron:

$$E_{\text{rad}}(R, t)/E_{\text{in}} =$$



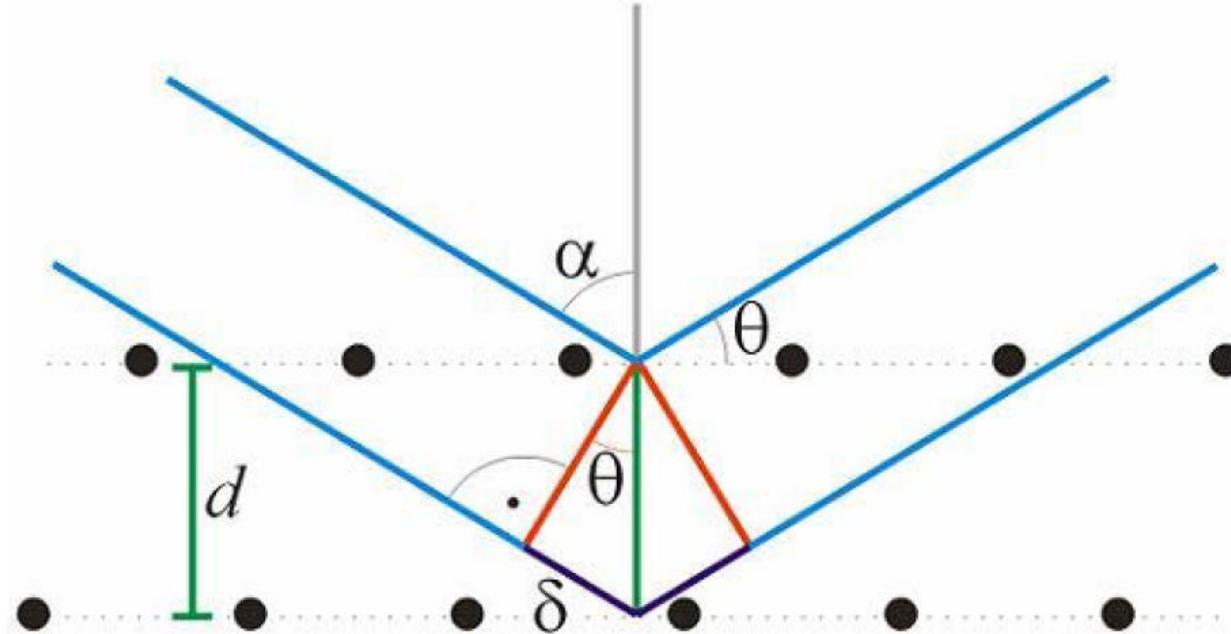
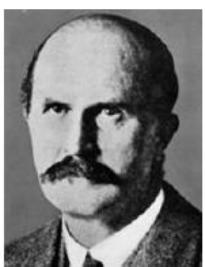
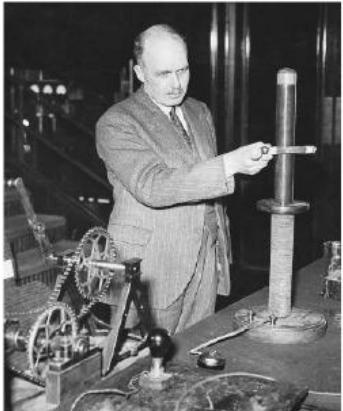
$$-(e^2/4\pi\epsilon_0 mc^2) \exp(i\mathbf{k}\mathbf{R})/R \cos\psi$$

spherical wave

thomson scattering length  $r_0$   
 $(=2.82 \times 10^{-5} \text{ \AA})$

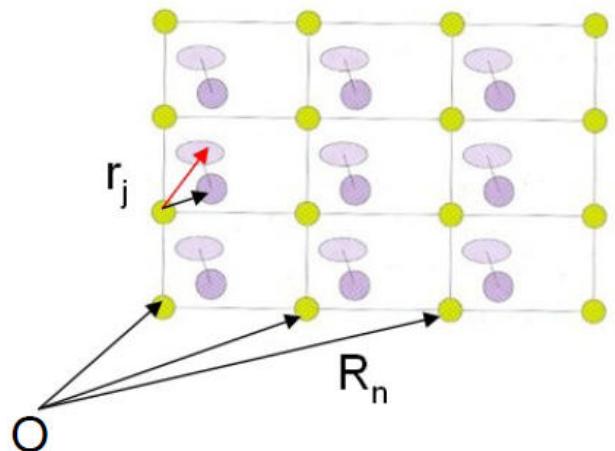
phase shift of  $\pi$  btw. incident and radiated field

# Bragg's Law



scattering intensity only if:  $n\lambda = 2d \sin(\Theta)$

## scattering by a crystal:



$$r_j = R_n + r_j$$

lattice vector + atomic position in lattice

$$F^{\text{crystal}}(Q) = \frac{\sum_{r_j} f_j(Q) \exp(iQr_j)}{\text{unit cell structure factor}} \frac{\sum_{R_n} \exp(iQR_n)}{\text{lattice sum}}$$

$$I_s = r_o^2 F(Q) F^*(Q) P$$

lattice sum  $\equiv$  phase factor of order unity or  $N$  (number of unit cells) if

$$Q \bullet R_n = 2\pi \times \text{integer} \text{ and } Q = G$$

# ▪ Reciprocal Lattice

1-D: defined by (iiia):  $a_i \bullet a_j^* = 2\pi \delta_{ij}$

2-D and 3-D:

$$a_1^* = (2\pi/v_c) a_2 \times a_3$$

$$a_2^* = (2\pi/v_c) a_3 \times a_1$$

$$a_3^* = (2\pi/v_c) a_1 \times a_2$$

with  $v_c = a_1 \bullet (a_2 \times a_3)$

note: in 2-D  $a_3$  is chosen to be a unit vector normal to the 2-D plane spanned by  $a_1$  and  $a_2$ .

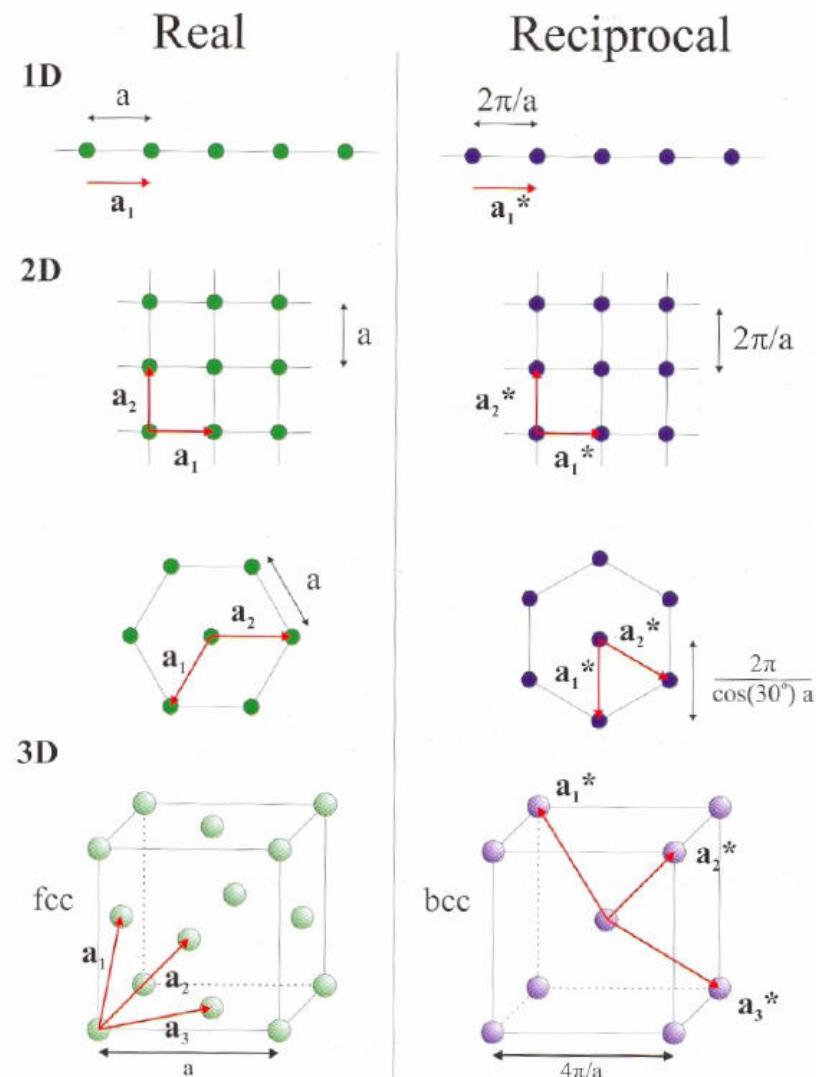
Example: fcc lattice

$$a_1 = (a/2)(y'+z'), a_2 = (a/2)(z'+x'), a_3 = (a/2)(x'+y')$$

$$a_1^* = (4\pi/a) (y/2 + z/2 - x/2)$$

$$a_2^* = (4\pi/a) (z/2 + x/2 - y/2)$$

$$a_3^* = (4\pi/a) (x/2 + z/2 - y/2)$$



## • The Ewald shere

Visualisation of diffraction effects in reciprocal space (a).

Laue condition requires  $\mathbf{Q} = \mathbf{G} = h\mathbf{a}_1^* + k\mathbf{a}_2^*$

Design sphere with radius  $k$  pointing to origin (b).

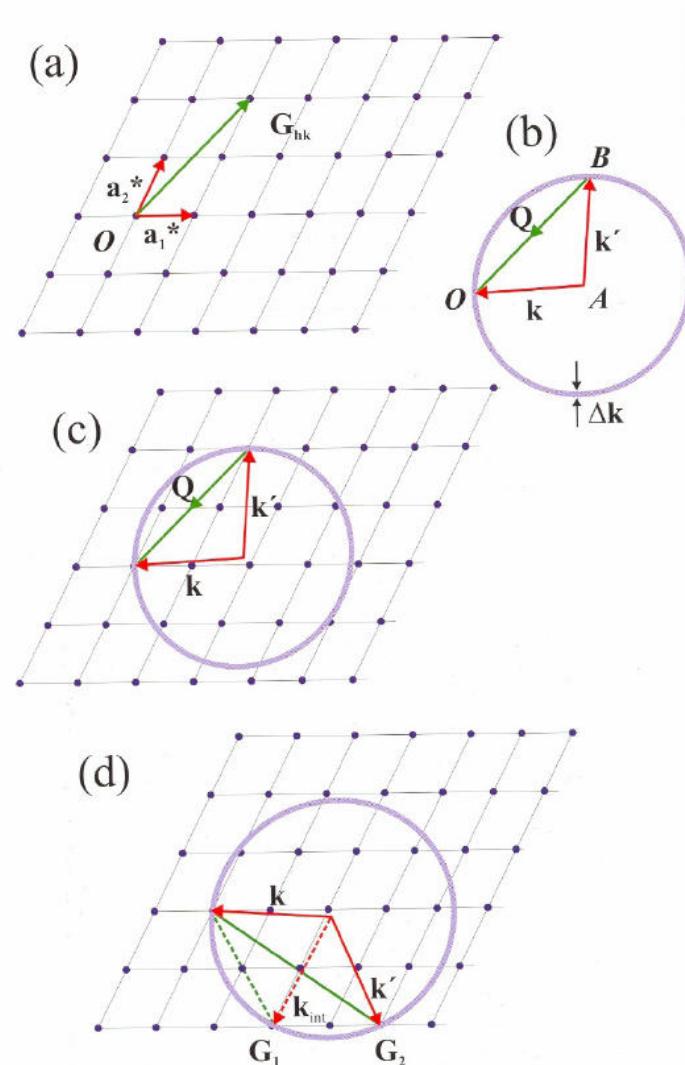
If any reciprocal lattice point falls on the circle then the Laue conditions is fulfilled (c).

Intensity is observed if the detector is placed in the direction of  $\mathbf{k}'$  (c).

A rotation about O corresponds to a rotation of the crystal.

Note: More than one reciprocal lattice point can lie on the sphere  $\equiv$  multiple scattering.

If the beam is not monochromatic the sphere adopts the corresponding width. In the white beam case all spots are ultimately detected.



unit cell structure factor:

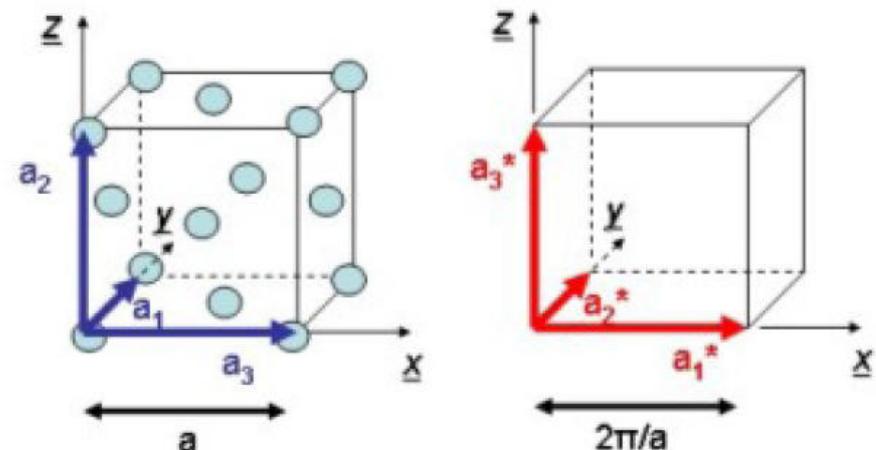
$$\sum_{r_j} f_j(Q) \exp(iQr_j)$$

e.g. fcc lattice:  $r_1 = 0$

$$r_2 = \frac{1}{2} (a_1 + a_2)$$

$$r_3 = \frac{1}{2} (a_2 + a_3)$$

$$r_4 = \frac{1}{2} (a_3 + a_1)$$



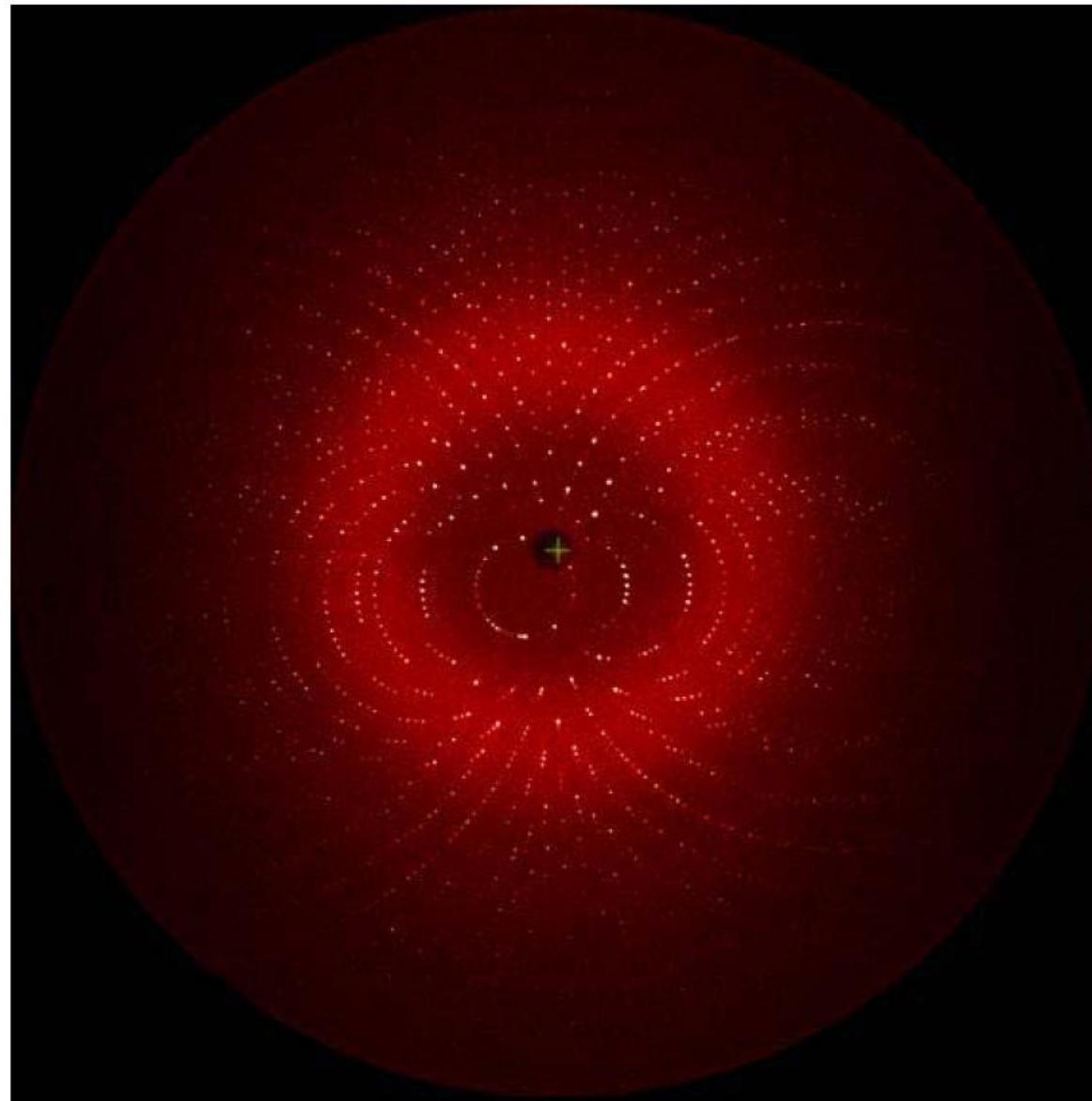
$$a_1 = a\underline{x}; a_2 = a\underline{y}; a_3 = a\underline{z}; V_c = a^3; a_1^* = (2\pi/a)\underline{x}; a_2^* = (2\pi/a)\underline{y}; a_3^* = (2\pi/a)\underline{z}$$

$$F_{hkl}^{fcc} = f(Q) \sum \exp(iQr_j) \quad \text{with } Q = G = h a_1^* + k a_2^* + l a_3^*$$

$$= f(Q) \{1 + e^{i\pi(h+k)} + e^{i\pi(k+l)} + e^{i\pi(l+h)}\} \quad (\mathcal{E})$$

$$= f(Q) \times \begin{cases} 4 & \text{if } h, k, l \text{ are all even or odd} \\ 0 & \text{otherwise} \end{cases}$$

# Modern Protein Crystallography

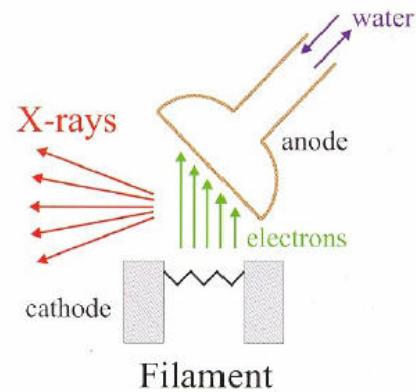


# Sources of X-Rays

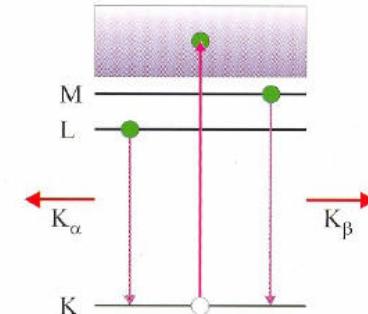
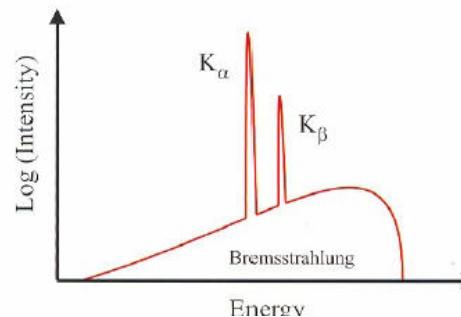
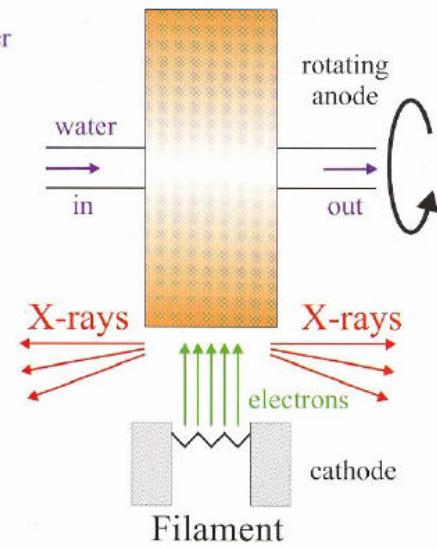
- 1895 discovered by W.C. Röntgen
- 1912 First diffraction experiment (v. Laue)
- 1912 Coolidge tube (W.D. Coolidge, GE)
- 1946 Radiation from electrons in a synchrotron, GE, Physical Review, 71,829(1947)



Coolidge Tube



Rotating Anode



## HochleistungsRöntgenröhren

- Einfach zu handhaben
- Einsetzbar in fast jedem Labor
- Typisch nur zwei Anregungsenergien:  
 $Mg\ K\alpha$  (1.2 keV) und  $Al\ K\alpha$  (1.4 keV)
- Nicht durchstimmbar
- geringe Leistung
- schlechte Auflösung;  $\Delta E$  1-2 eV (natürliche Linienbreite der atomaren Übergänge)

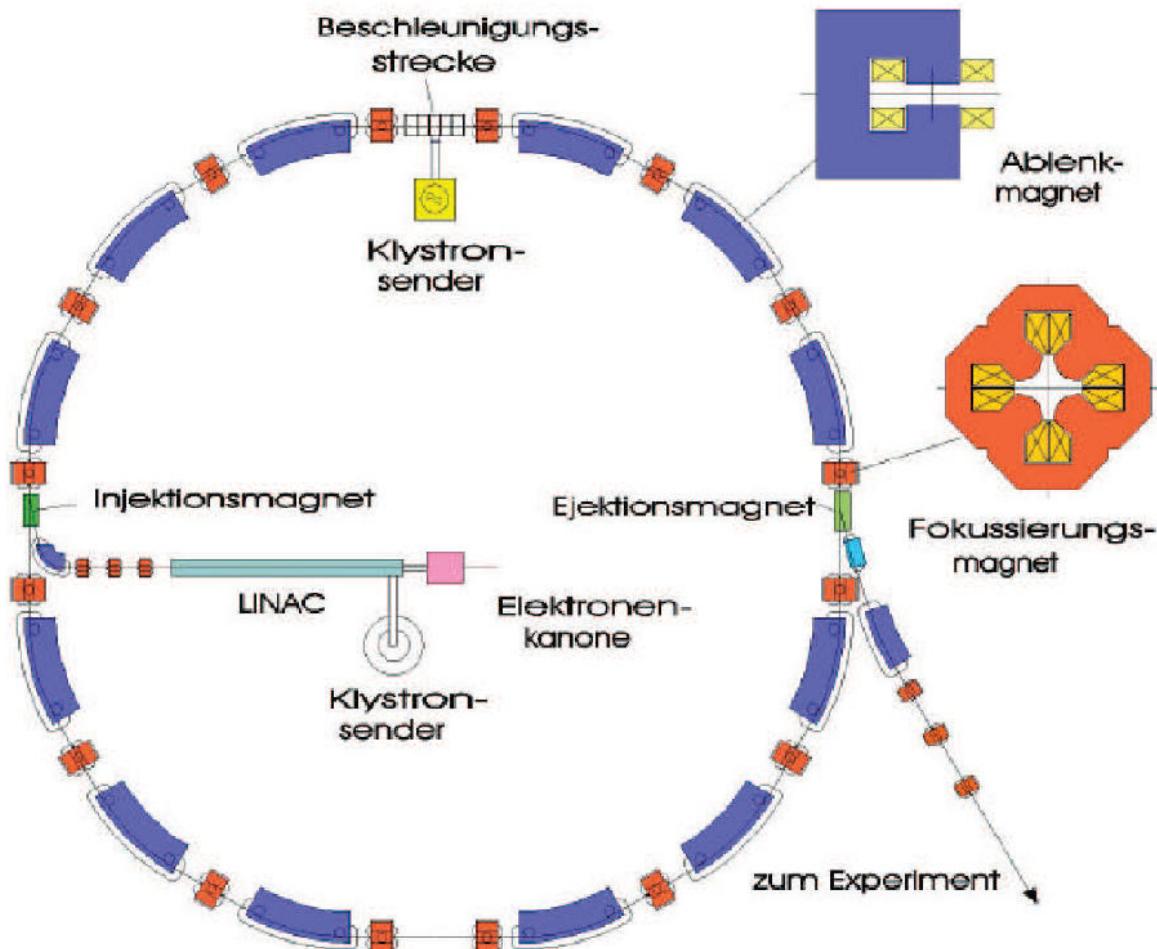
## Synchrotronstrahlung

- Photonenenergie *frei* wählbar zwischen dem Infraroten (THz Strahlung) und harter Röntgenstrahlung ( $>100$  keV)
- Sehr hohe Photonenzahlen
- Polarisation der Strahlung frei wählbar
- Großgerät

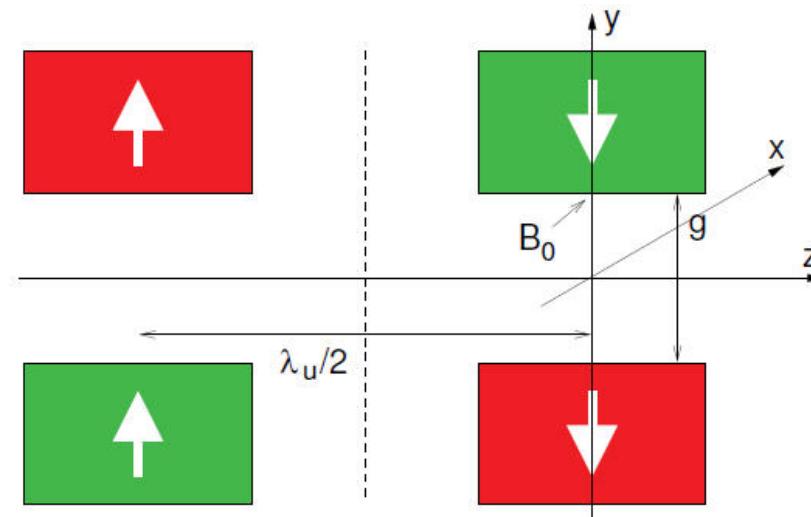
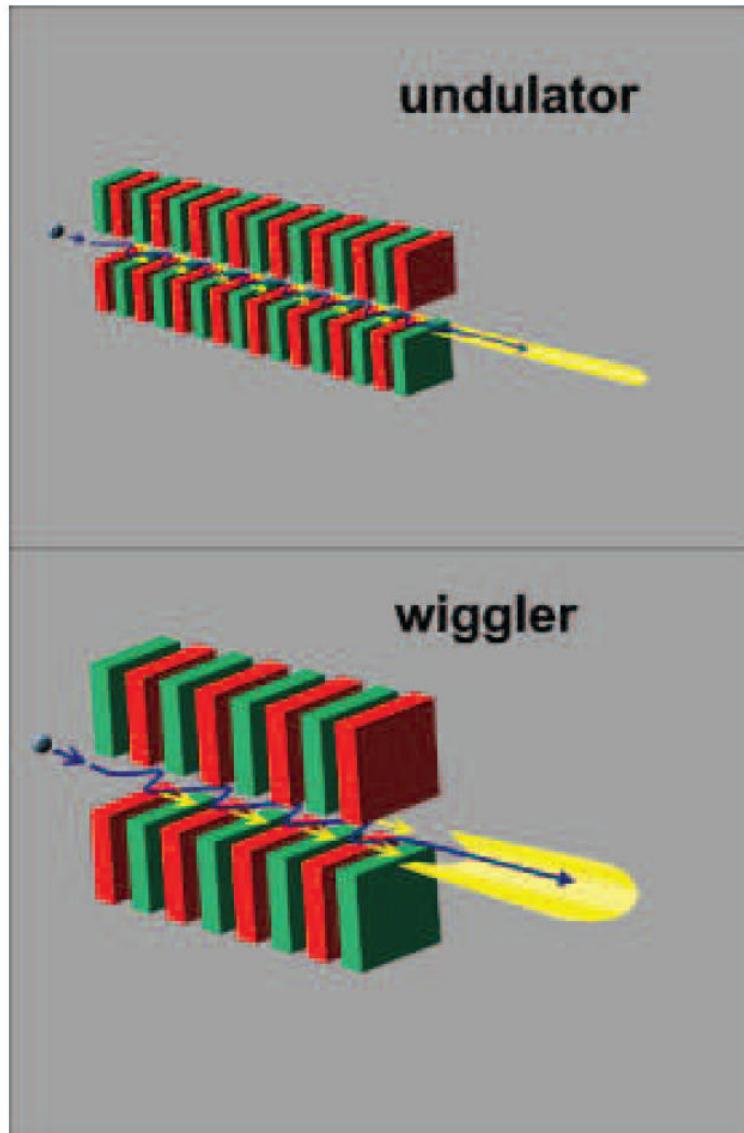
## Freie Elektronen Laser (FEL)

- Laserstrahlung im Röntgenbereich
- Extrem hohe Photonendichten
- Sehr kurze Lichtpulse (einige 10 fs)
- Photonenenergien in der Zukunft bis zu 14 keV

# Aufbau eines Synchrotrons



# Insertion Devices (IDs)



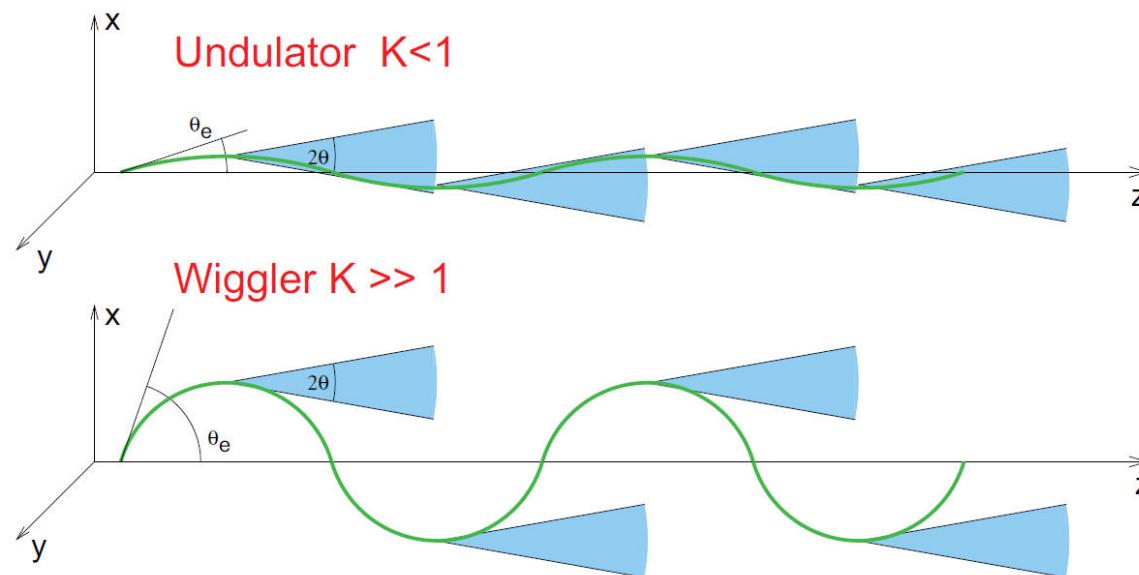
$$\bar{B} = \frac{B_0}{\cosh \pi \frac{g}{\lambda_u}}$$

$$B_y(z) = \bar{B} \cos \frac{2\pi}{\lambda_u} z$$

$$v_x = \frac{Kc}{\gamma} \sin \frac{2\pi}{\lambda_u} z$$

mit  $K := \frac{e\bar{B}\lambda_u}{2\pi m_0 c}$

$$|\theta_{e,max}| \approx \frac{K}{\gamma} \quad \gamma = \left(1 - \frac{v^2}{c^2}\right)^{-1/2}$$



# Undulator Parameter

Charakteristischer Abstrahlwinkel der SR:  $\theta = 1/\gamma$ ,  $\theta_e = K/\gamma$

$K \leq 1$  Undulator

Abstrahlkegel der einzelnen Magnetpole überlappen → kohärente Überlagerung → Interferenzeffekte

$K \gg 1$  Wiggler

Abstrahlkegel der einzelnen Magnetpole überlappen nicht → Nicht kohärente Überlagerung → Emittierte Strahlung entspricht weitgehend der eines Dipols, aber mit  $2 \cdot N$  facher Intensität.

Wellenlänge  $\lambda$  der Undulatorstrahlung:

$$\lambda = \frac{\lambda_u}{2\gamma^{*2}}(1 + \gamma^{*2}\theta^2) = \frac{\lambda_u}{2\gamma^2} \left(1 + \frac{K^2}{2} + \gamma^2\theta^2\right) \quad (5)$$

Vergleich der verschiedenen Quellen

Dipol:  $P$

Wiggler:  $N \cdot P$

Undulator:  $N^2 \cdot P$

Beim FEL werden wir sehen, daß für diesen dann

$$N^2 \cdot N_e^2$$

gilt

- Eine wichtige Größe zur Charakterisierung von Synchrotronstrahlung ist die Brillanz

$$B := \frac{\Delta P}{\Delta A \cdot \Delta \Omega}$$

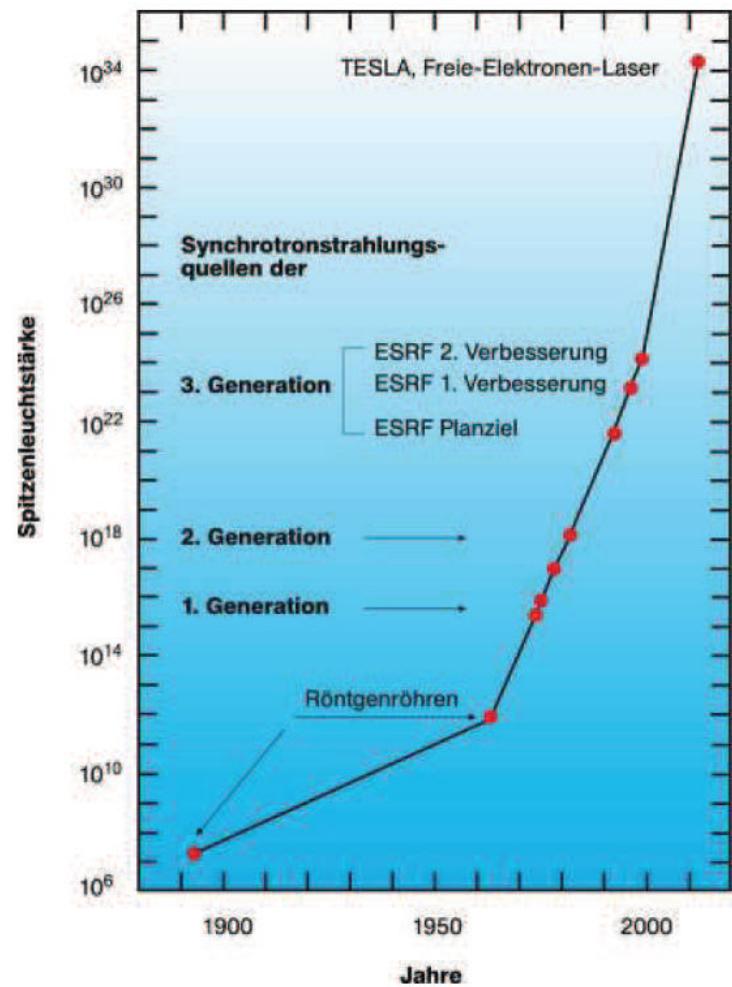
Spektrale Brillanz

$$B_{\Delta\omega/\omega} := \frac{\Delta P}{\Delta A \cdot \Delta \Omega \cdot \Delta\omega/\omega}$$

- Dichte der Photonen im transversalen Phasenraum
- Um eine möglichst hohe Photonendichte am Ort des Experimentes zu erreichen, muß die Brillanz so groß wie möglich sein
- Größtmöglich Brillanz → Laser
- Einheit

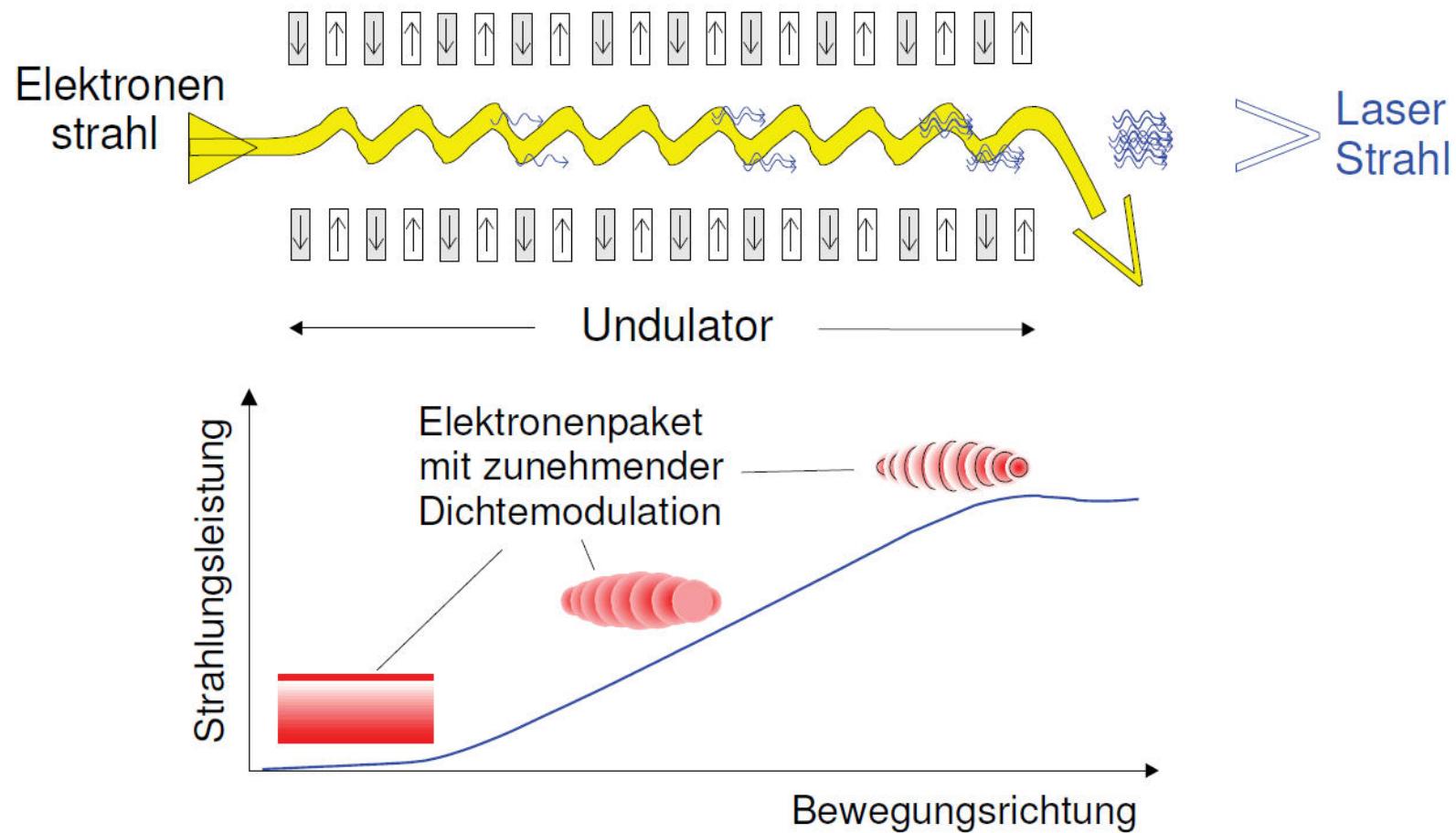
$$[B_{\Delta\omega/\omega}] = \frac{\text{Photonen}}{\text{s} \cdot \text{mm}^2 \cdot \text{mrad}^2 \cdot 0.1\% \text{BW}}$$

# Brillanz



- Entwicklung der Brillanz verschiedener Röntgenquellen mit der Zeit

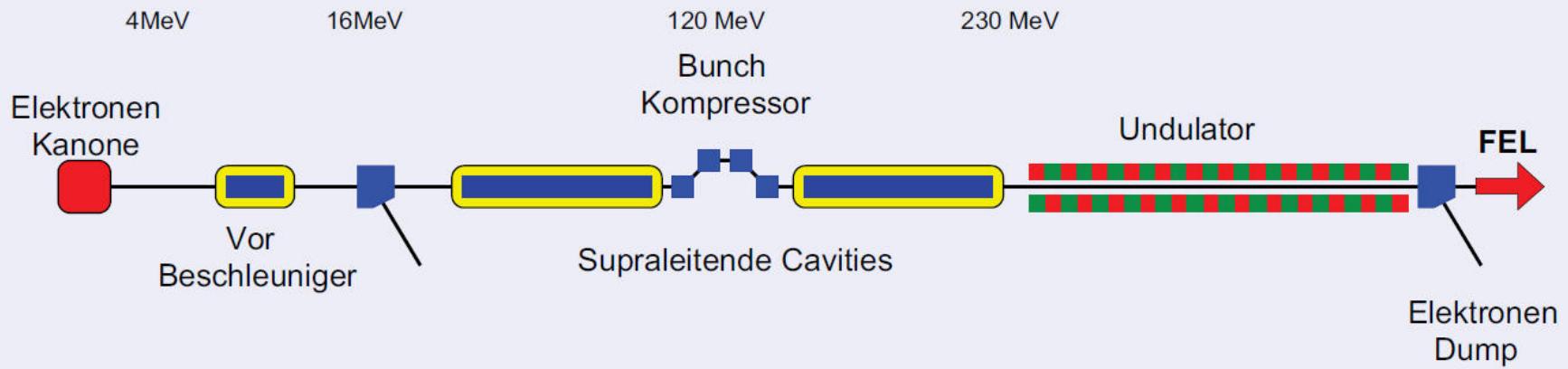
# Das FEL Prinzip



# Aufbau eines FEL

- Elektronenquelle: Erzeugung eines Elektronenbunches
- Beschleuniger: Beschleunigung auf relativistische Energien
- Magnetstruktur: Erzeugung der Röntgenstrahlung – Synchrotronstrahlung
- Röntgenoptik: Transport der FEL-Strahlung zum Experiment

## Experiment



# Realisierung eines FEL

## Erster VUV-FEL

FLASH am Hasylab/DESY

## Eigenschaften XFEL

- Typische Länge des Beschleunigers: 30-2000 m
- Länge der Magnetstruktur: 30-300 m
- Photonenergiebereich 10 eV - 10 keV
- Pulslängen 10 – 100 fs (jetzt)



- Zahl der Photonen, die man an aktuellen Synchrotronquellen in 1 s bekommt, erzeugt ein FEL in 50 fs !

