

# Vorlesung zum Haupt/Masterstudiengang Physik

## Methoden Moderner Röntgenphysik II: Struktur und Dynamik Kondensierter Materie

Surfaces

(OHS)

Applications in Soft Matter

(MMAK / SVR)

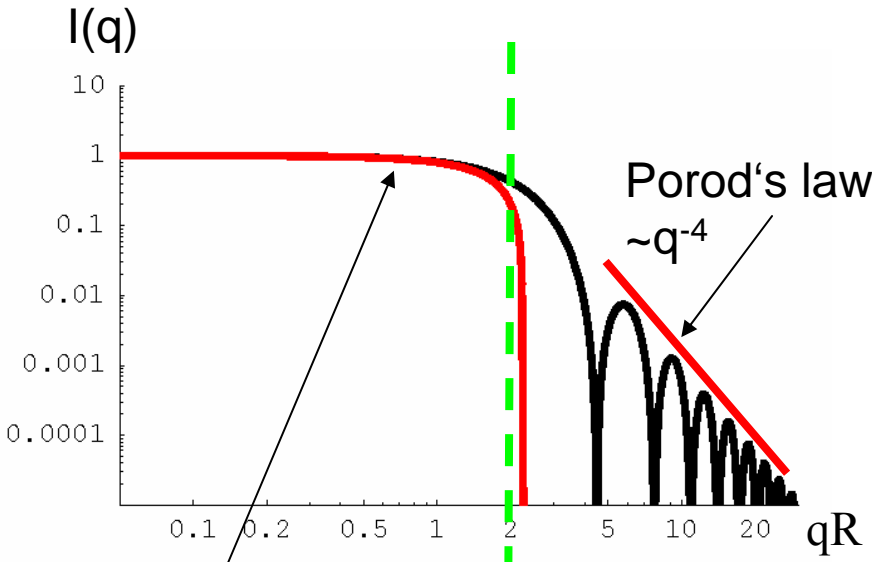
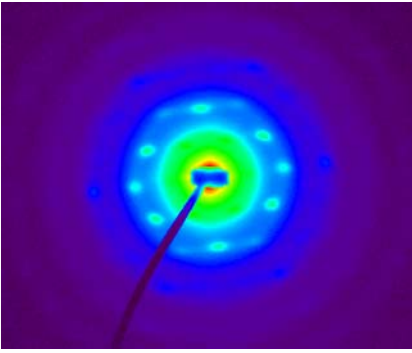
Mottakin M. Abul Kashem / Stephan V. Roth (SVR)

# Applications in Soft Matter

- 20.04.2010 An Introduction to Polymer Physics
- 22.04.2010 Small-Angle X-ray Scattering and its Applications
- 27.04.2010 [Polymer, Colloidal and Nanocomposite Surfaces I](#)
- 29.04.2010 Polymer, Colloidal and Nanocomposite Surfaces II

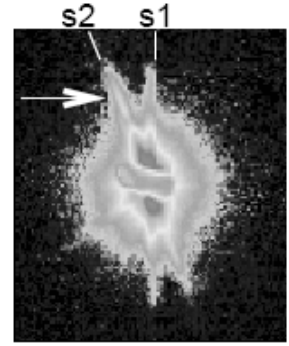
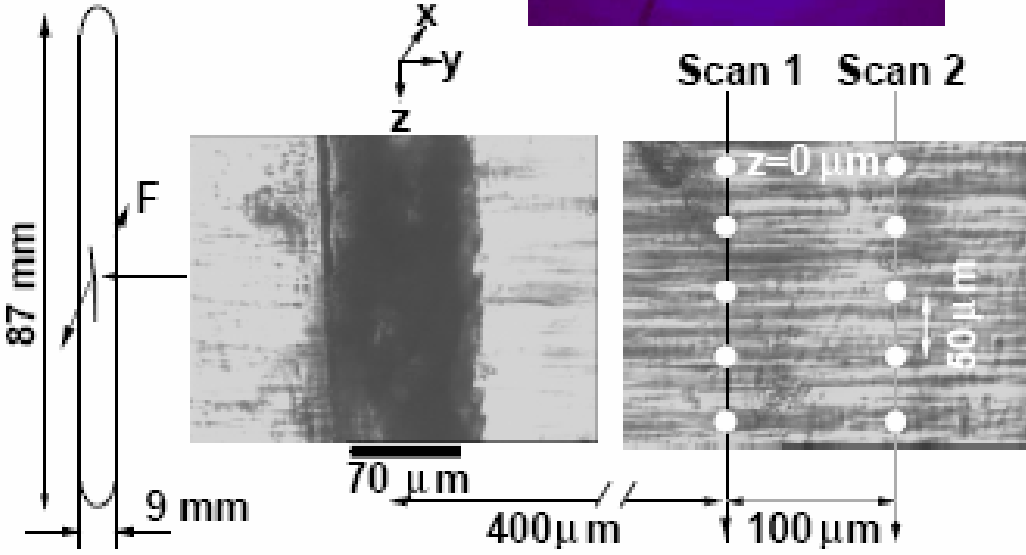
# Summary last lecture

- Approximations for Form factor:
  - Very useful to get first-hand information about multiple length scales
- Influence of form factor (concentrated samples)
- Examples:
  - Colloidal crystals
  - Cracks & crazes



Guinier

$$I(q) = I(0) \cdot \exp\left(-\frac{1}{3} R_G^2 q^2\right)$$



$q = 0.79 \text{ nm}^{-1}$

**Questions?**

# Outline

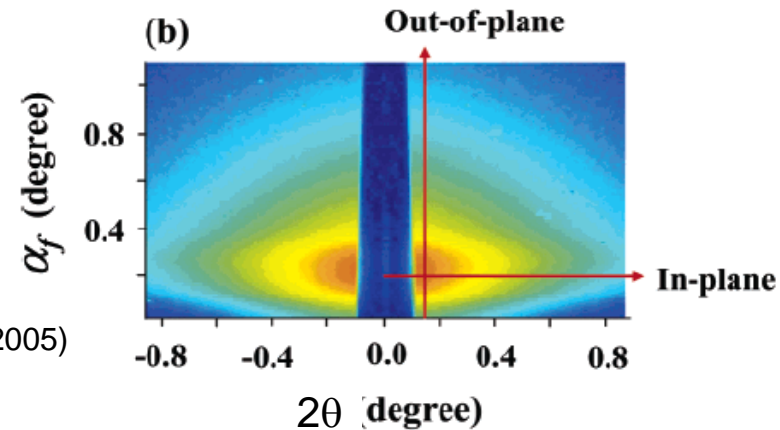
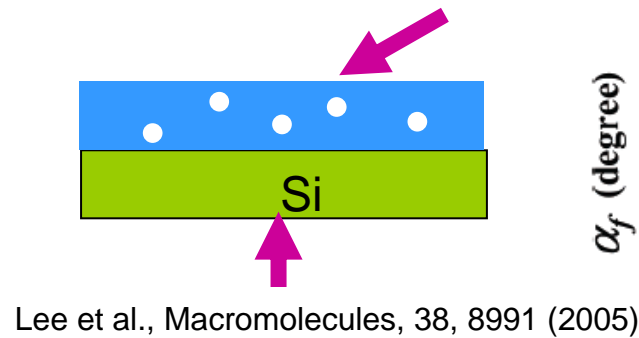
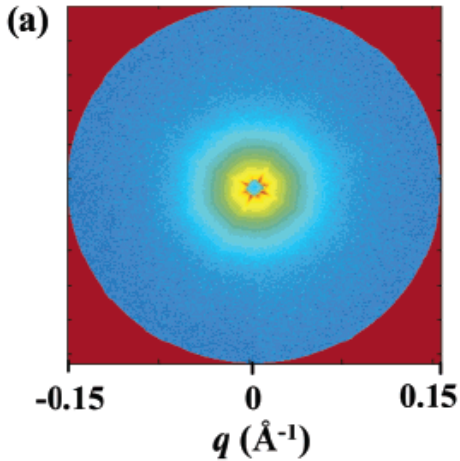
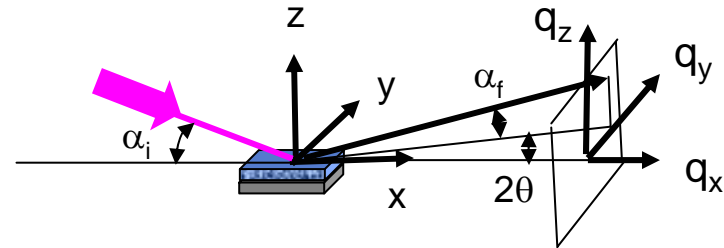
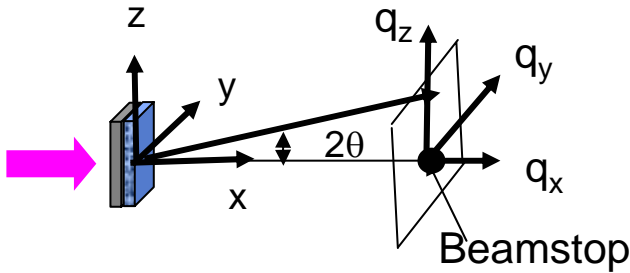


- SAXS versus GISAXS
- GISAXS – theory
- Instrumentation
- Application examples:
  - Gold on glass
  - in-situ growth of colloidal crystals
  - Polymer nanochannels

**Au on glass!**

**It is important to understand the basic features of the different GISAXS pattern and cuts.**

# T-SAXS vs. GISAXS

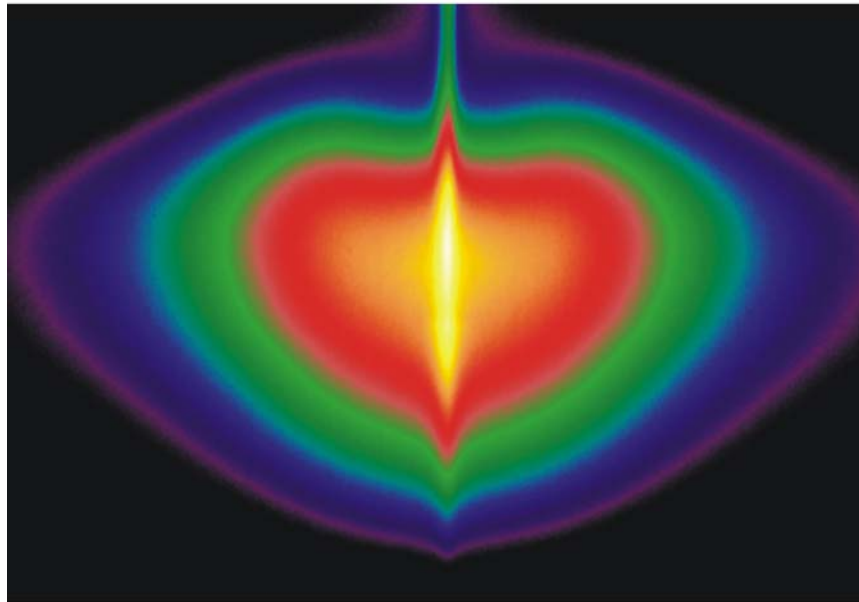


- Easy measurement
- Easy analysis
- In-plane information ( $q_y, q_z$ )
- Any possible scattering from substrate
- Transparency of substrate
- High energy

- Strong intensity
- Easy preparation of samples
- Full information ( $q_x, q_y, q_z$ )
- Scattering from surface / internal structure
- Scattering from reflected AND transmitted beam
- Refraction effects (DWBA)
- Special setup

# History

- 1963 Yoneda – anomalous Scattering below  $\alpha_i$
- 1988 Sinha – rough multilayers
- 1989 Levine – kinetics of gold nanoparticles on glass
- 1996 Müller-Buschbaum – mesoscopic length scales in polymer films
- 2003 Müller-Buschbaum – combination with  $\mu$ focused beams
- Since 2006 „going nano“ ... PETRA III



BW4, CCD  
Au  
d=5nm  
t=3h  
T=300°C

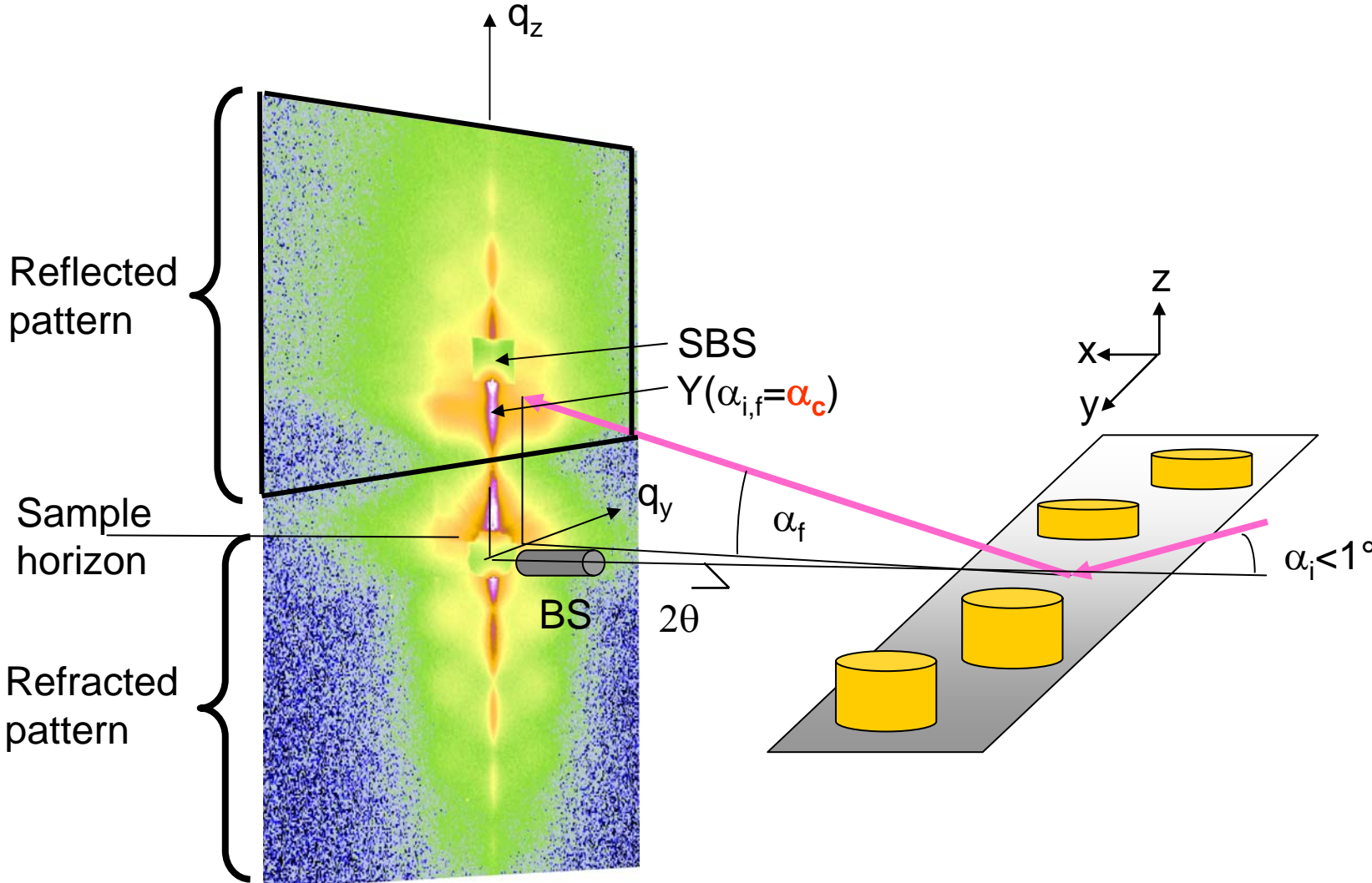
# Outline



- SAXS versus GISAXS
- GISAXS – theory
- Instrumentation
- Application examples:
  - Gold on glass
  - in-situ growth of colloidal crystals
  - Polymer nanochannels

**Au on glass!**

# Grazing incidence small-angle x-ray scattering





# History

- 1963 Yoneda – anomalous Scattering below  $\alpha_i$
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PHYSICAL REVIEW

VOLUME 131, NUMBER 5

1 SEPTEMBER 1963

## Anomalous Surface Reflection of X Rays

Y. YONEDA

*Department of Applied Physics, Faculty of Engineering, Kyushu University, Fukuoka, Japan*

(Received 9 January 1963; revised manuscript received 2 May 1963)

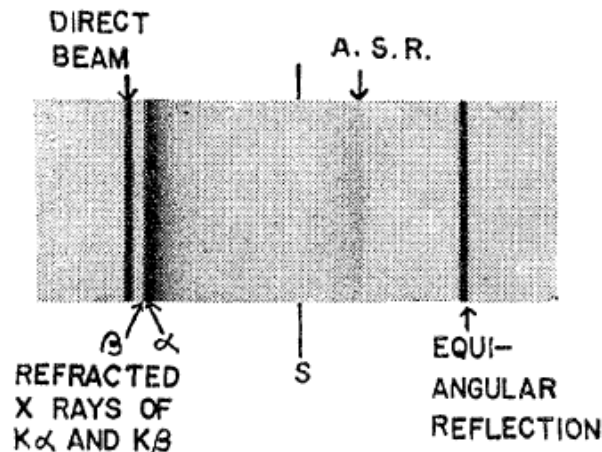


FIG. 2. Photograph of A.S.R. by a glass sample,  $\times 2$ .

# The first successful experiment

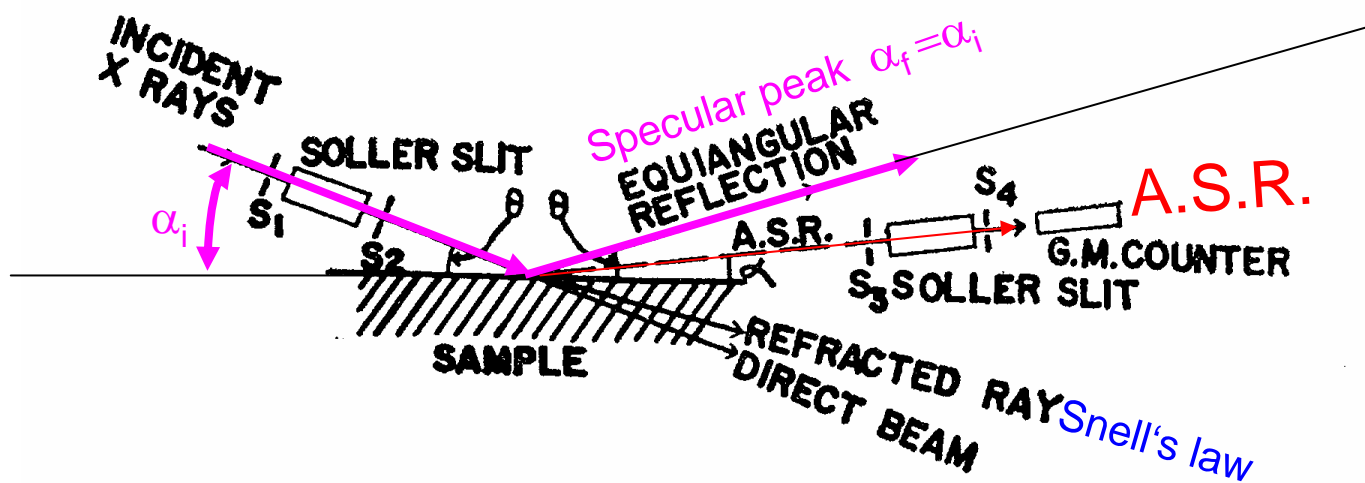


FIG. 1. Schematic view of the experimental arrangement in the incident plane.

Anomalous Surface Reflection  
(diffuse scattering)

Au, 20nm-200nm

Si

Intensity between  $\alpha_f = 0^\circ$  and  $\alpha_f = \alpha_i$  !!!

Why ?

# Refractive index for x-rays

$$n = 1 - \delta + i\beta$$

**real part**

Number density of atoms

Atomic number

$$\delta = \frac{\lambda^2}{2\pi} r_0 \frac{NZ}{\rho_e}$$

**imaginary part**

wavelength

Absorption coefficient

$$\beta = \frac{\lambda}{4\pi} \mu$$

$e^{-\mu x}$   
(Lambert-Beers law)

	$r_0\rho_e [10^{10}\text{cm}^{-2}]$	$\mu_x [\text{cm}^{-1}]$
Vacuum	0	0
PS (C8H8)n	9.5	4
Si	19.7	85
Au	131.5	4170

$$\alpha_c = \sqrt{2\delta}$$

**Critical angle**

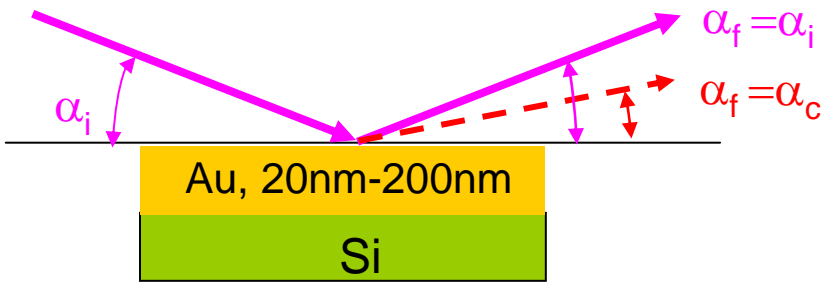
$\alpha_c(\text{Si})=0.2^\circ$   
 $\alpha_c(\text{Au})=0.5^\circ$

$$\lambda \approx 1\text{\AA} \Rightarrow \delta \sim 10^{-7} \dots 10^{-6}$$

Very small!

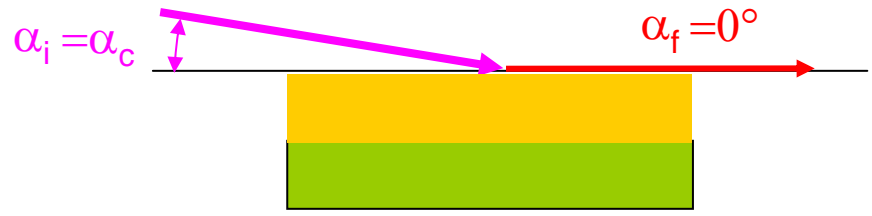
Matter:  $|n(\text{X-rays})| < 1$  optically less dense than vacuum (remember Bragg's law)

# Origin of intensity at $\alpha_c$

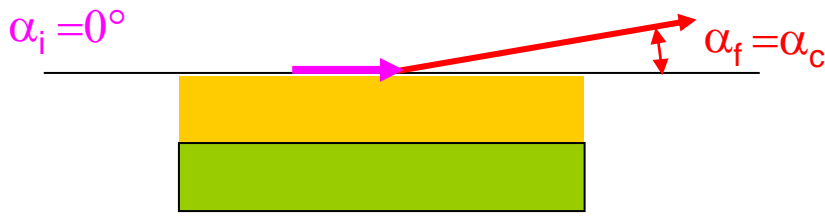


$\alpha_f(\text{Au}) = 0.56^\circ = \alpha_c(\text{Au}, 1.8\text{\AA})$

## Total external reflection

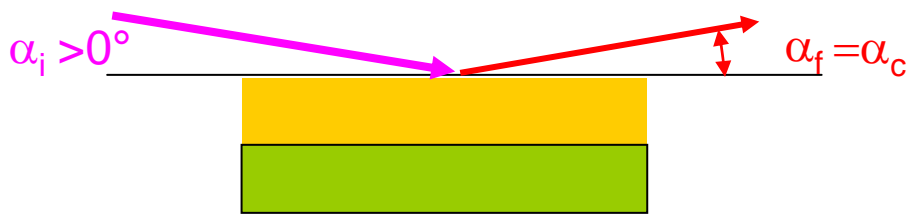


## Reciprocity theorem & critical angle



must stem from wave parallel to surface

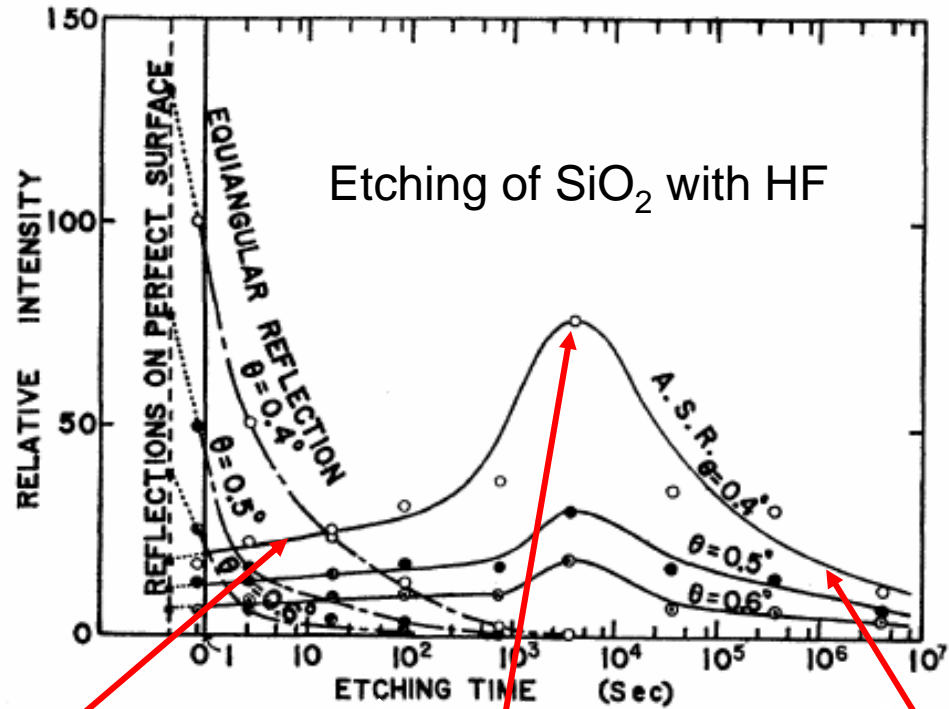
## Yoneda



Yoneda, Phys. Rev. 131, 2010 (1963)

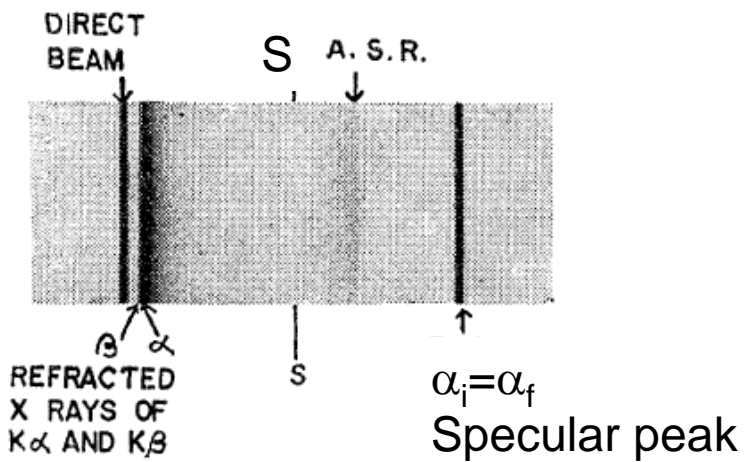
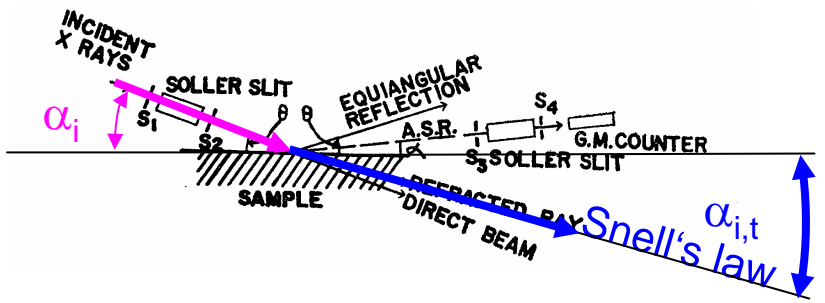
# Hint: Roughness of the sample

**Yoneda peak = Scattering effect!**

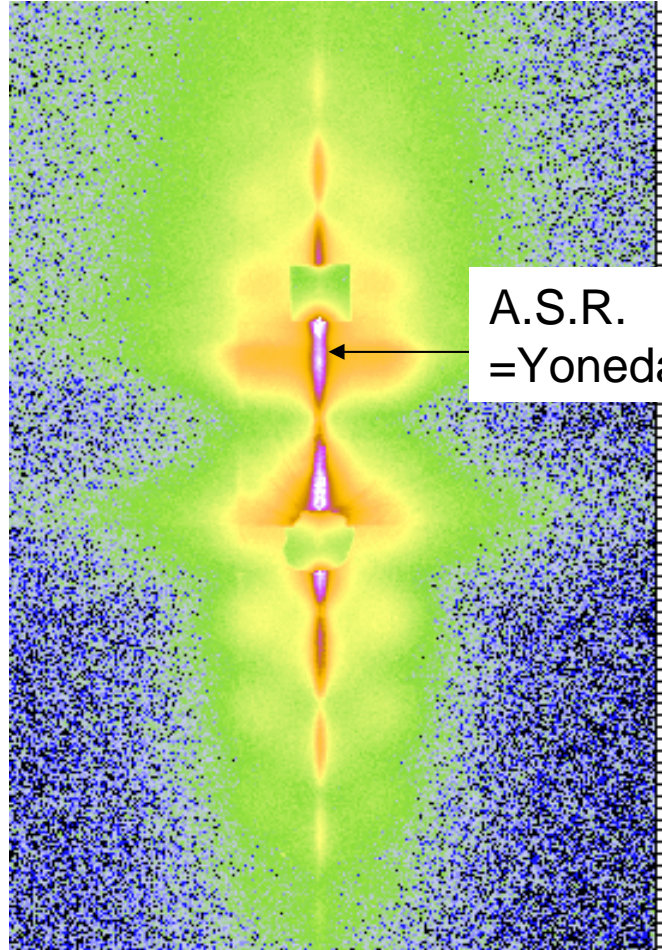


# Basically the same

1963



today



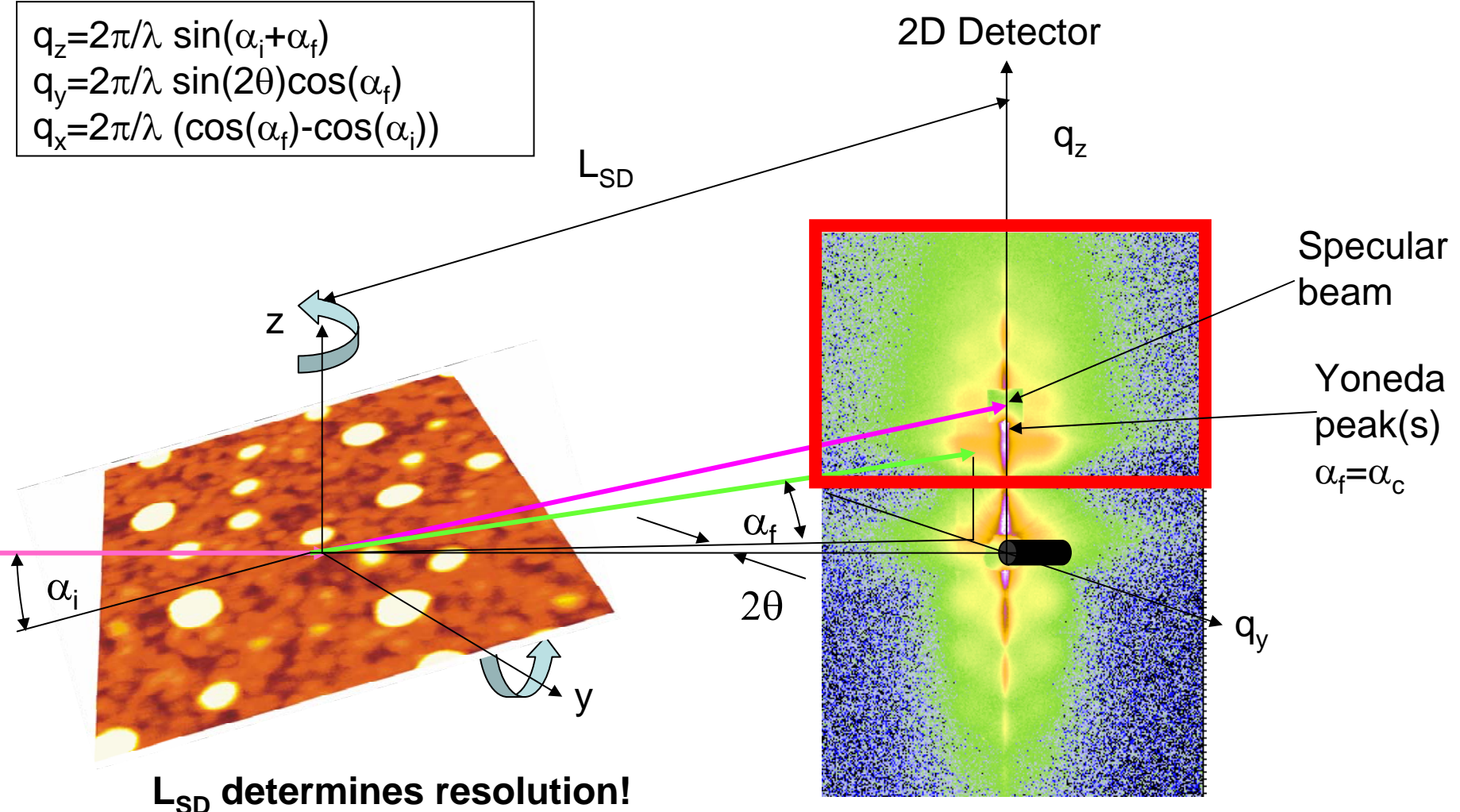
# μGISAXS – more details

## Grazing Incidence Small Angle X-Ray Scattering, GISAXS

$$q_z = 2\pi/\lambda \sin(\alpha_i + \alpha_f)$$

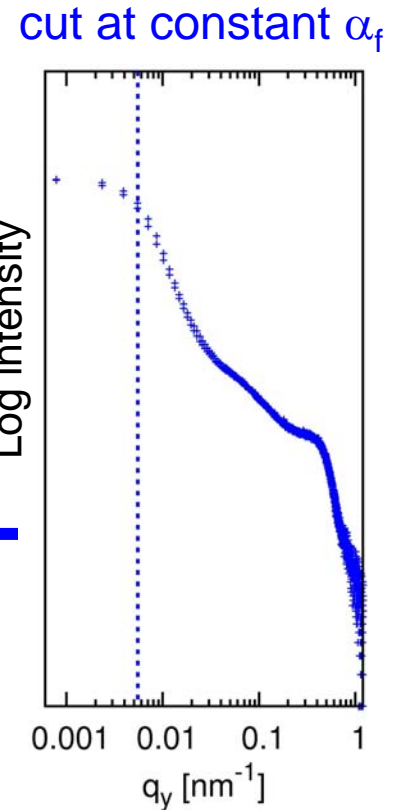
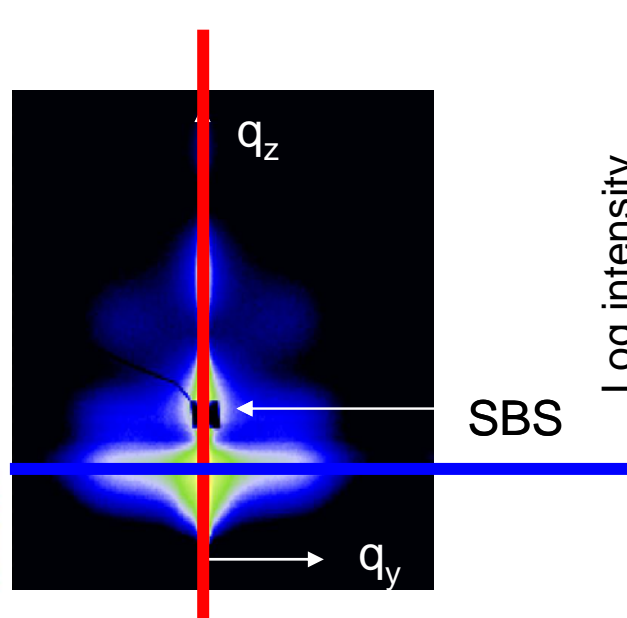
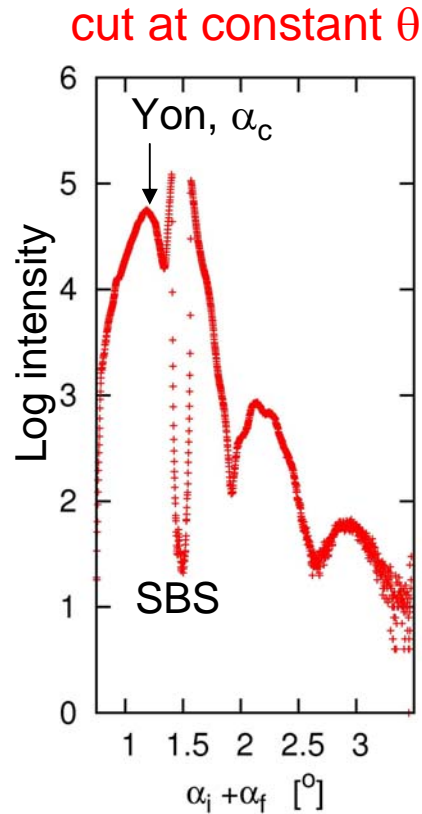
$$q_y = 2\pi/\lambda \sin(2\theta)\cos(\alpha_f)$$

$$q_x = 2\pi/\lambda (\cos(\alpha_f) - \cos(\alpha_i))$$



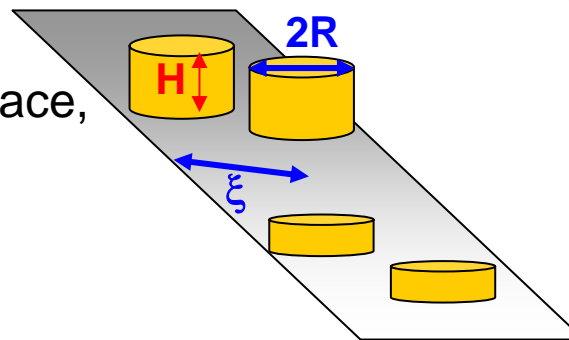
**$L_{SD}$  determines resolution!**

# Grazing incidence small-angle x-ray scattering



Correlation perpendicular to surface, e.g. height of nanoparticles, roughness, layer thickness

Detector-scan



In-plane structures, e.g. distances  $\xi$ , Radius  $R$

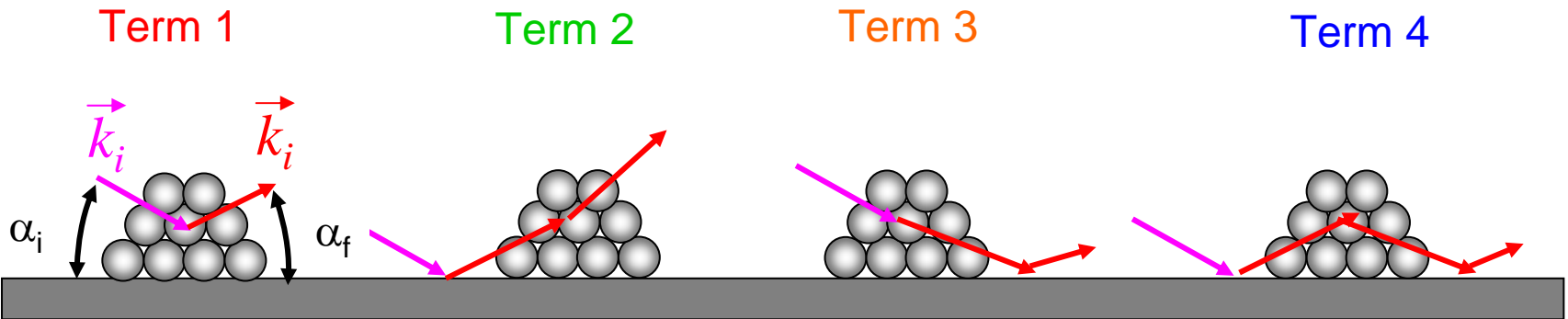
Out-of-plane scan

Salditt et al., Phys.Rev.B **51**, 5617 (1995)  
 Naudon et al., Physica B, **283**, 69 (2000)  
 Renaud et al., Science, **300**, 1416 (2003)  
 Müller-Buschbaum, Anal. Bioanal. Chem **376**, 3 (2003)



# Distorted Wave Born approximation

Form factor: multiple scattering



$$\frac{d\sigma}{d\Omega} \propto \left| \underbrace{P(q_y, k_{fz} - k_{iz})}_{\text{Born term}} + R(\alpha_i)P(q_y, k_{fz} + k_{iz}) + R(\alpha_f)P(q_y, -k_{fz} - k_{iz}) + R(\alpha_i)R(\alpha_f)P(q_y, -k_{fz} + k_{iz}) \right|^2$$

Born term

with  $P(\vec{q}) = \int_V \exp(i\vec{q}\vec{r}) d^3r$

- Coherent interference between four waves along  $\alpha_f$
- Cross section depends on  $q_y$  and  $q_z$
- Weighting with the reflection coefficients in incidence and emergence

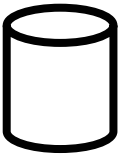
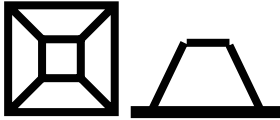
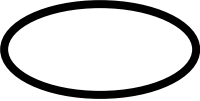
# Now for surfaces (nanoparticles)...

$$I(q_y, q_z) = c |P(q_y, q_z)|^2 \times S(q_y)$$

## Form factor: multiple scattering



## Shape, size and orientation

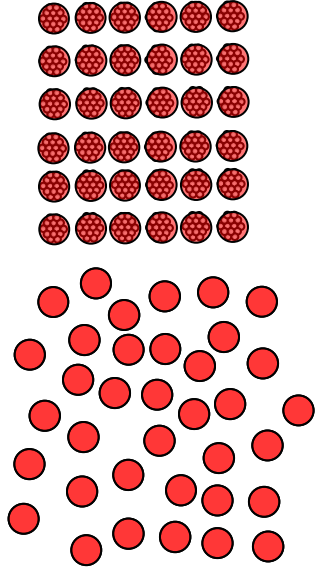
- cylinder 
  - pyramid 
  - ellipsoid 
- + size distributions

## Interference function

$$S(q_y) = \text{FT}(\text{pair correlation function})$$

## Spatial arrangement of the particles

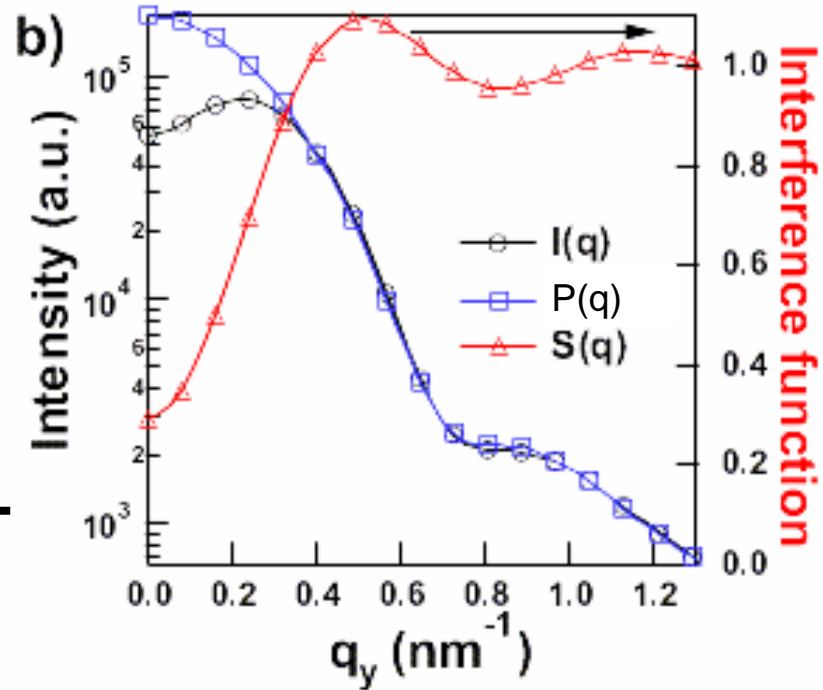
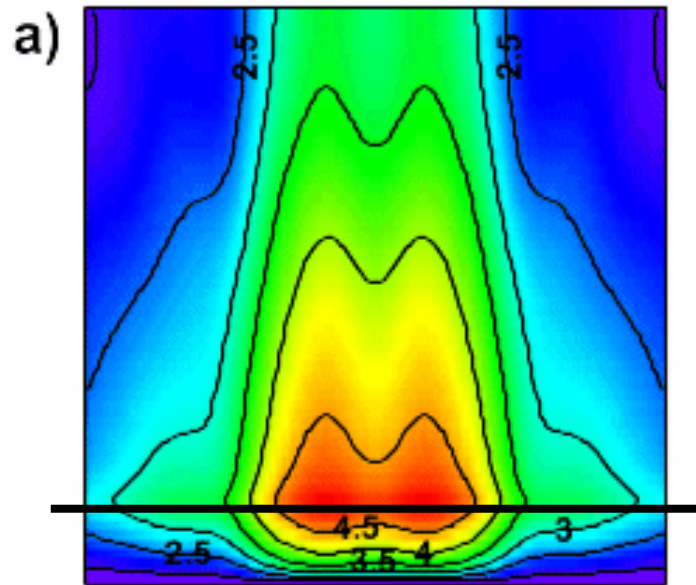
- lattice
- paracrystal



- + mean distance
- + fluctuation of distances

# Simulations: IsGISAXS (R. Lazzari)

$$I(q_y, q_z) = c |P(q_y, q_z)|^2 \times S(q_y)$$



# Outline

➤ SAXS versus GISAXS

➤ GISAXS – theory

➤ Instrumentation

➤ Application examples:

- Gold on glass

- in-situ growth of colloidal crystals

- Polymer nanochannels

**Au on glass!**



# BW4 / HASYLAB (Hamburg, Germany)

for GI(U)SAXS experiments at the BW4 beamline @ HASYLAB (DESY, Hamburg)

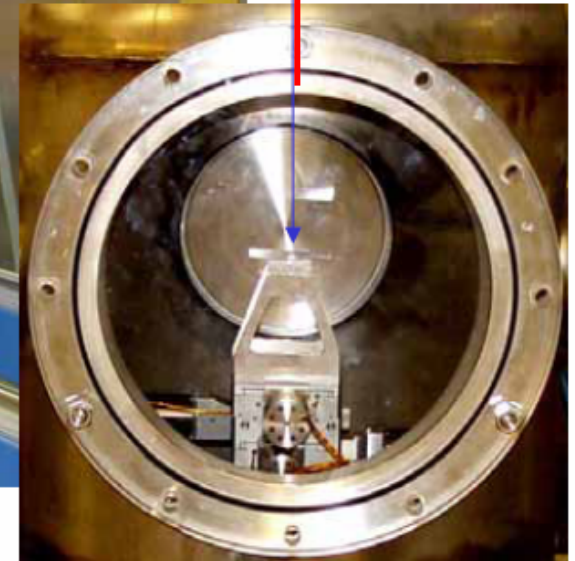
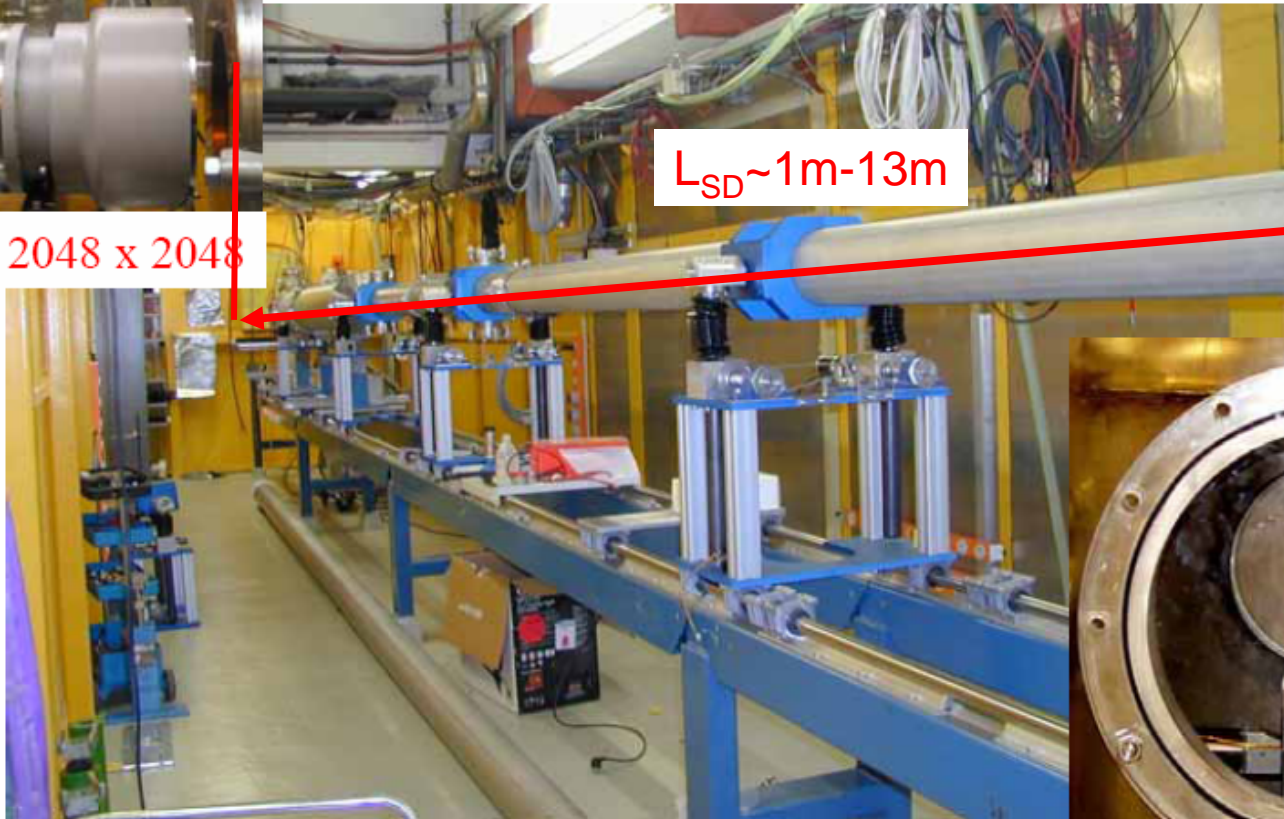


78.1  $\mu\text{m}$ , 2048 x 2048

$L_{SD} \sim 1\text{m}-13\text{m}$



sample

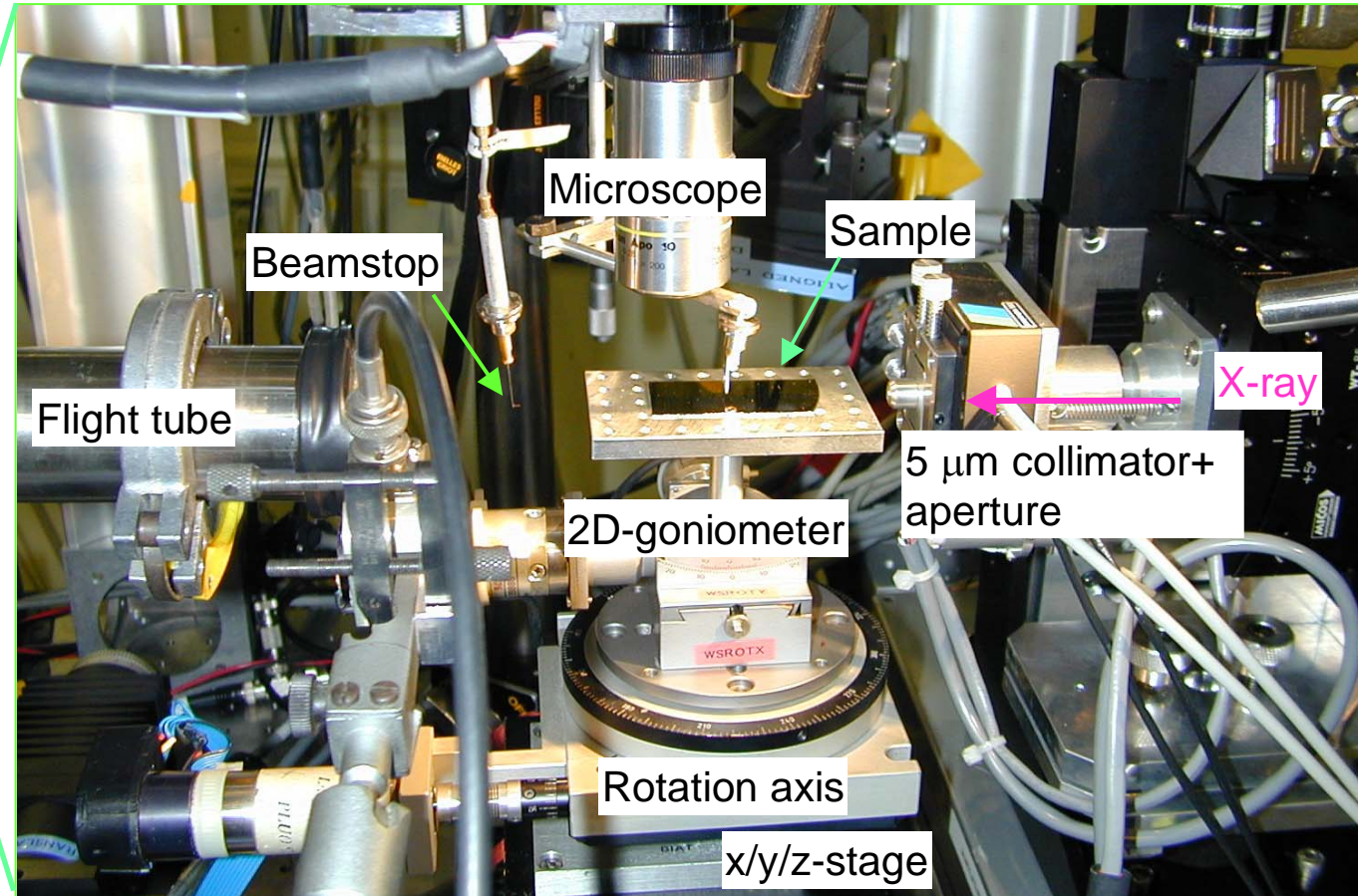
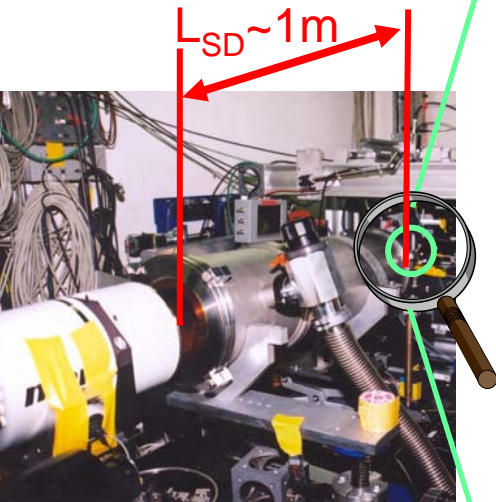


sample – detector distance up to **13 m** possible – optimized conditions for GI(U)SAXS

# ID13 / ESRF (Grenoble, France)

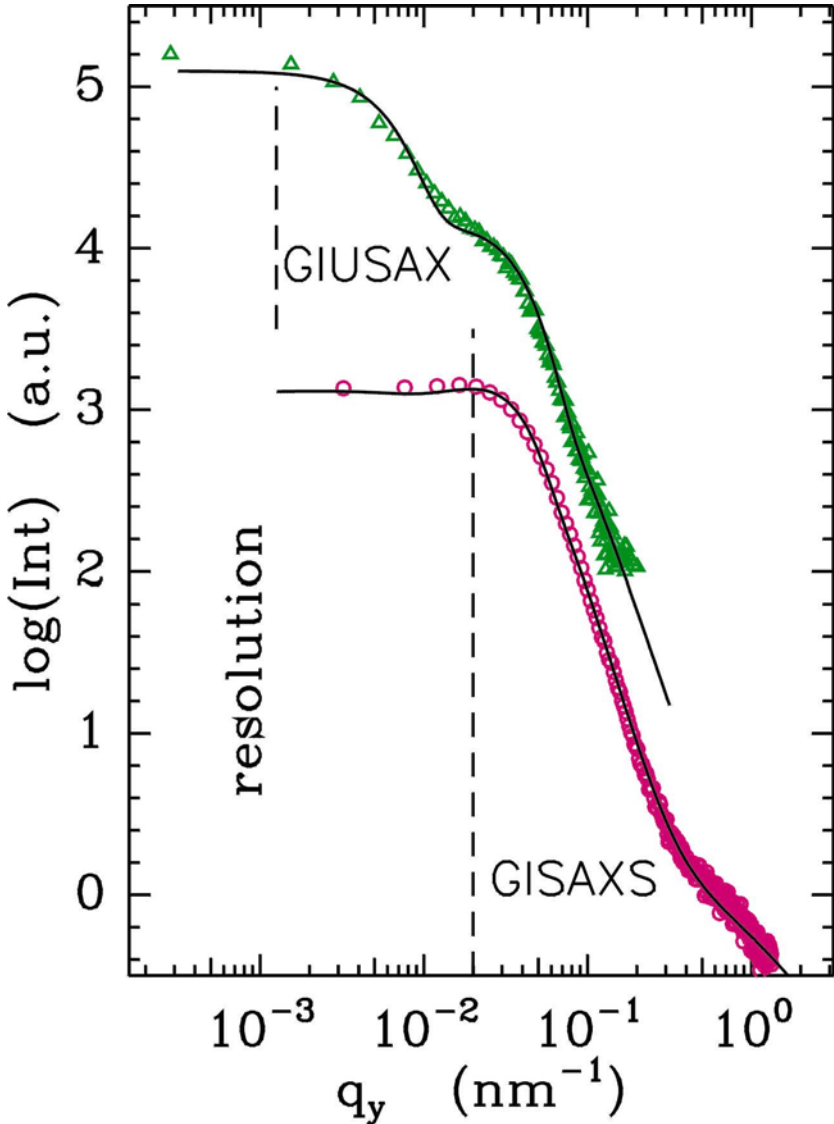
Mean information  $\Leftrightarrow$  local information

Combination of  
GISAXS with  
micro-focus beam



diameter of micro beam GISAXS experiment at ID13 (ESRF)  $5 \mu m$   
footprint (x/y)  $300 \times 5 \mu m^2 \rightarrow$  local information

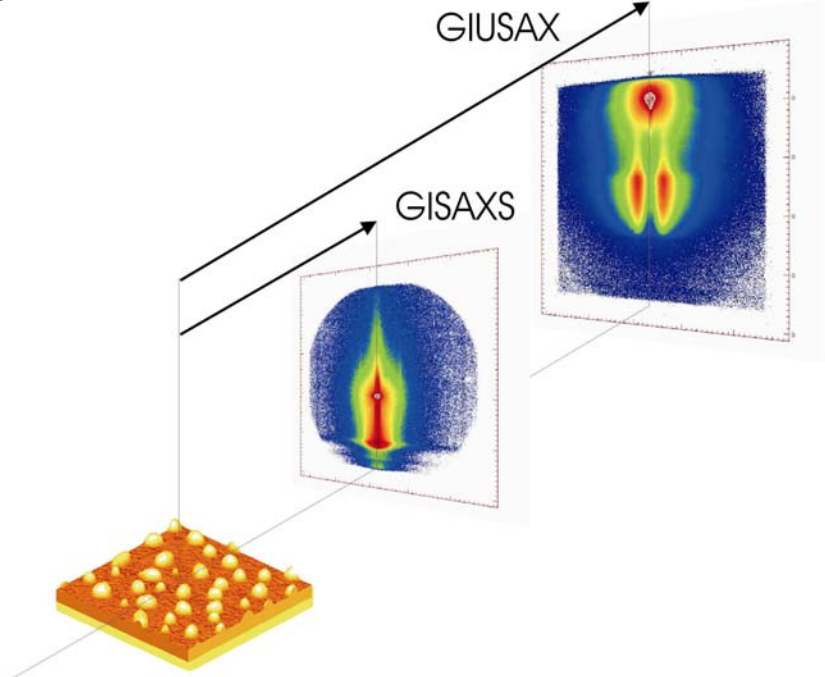
# GISAXS & GIUSAXS



combination of GIUSAXS and GIUSAXS experiment:

GIUSAXS: sample-detector distance 12.8 m

GISAXS: 1.9 m



# Outline

- SAXS versus GISAXS
- GISAXS – theory
- Instrumentation
- Application examples:



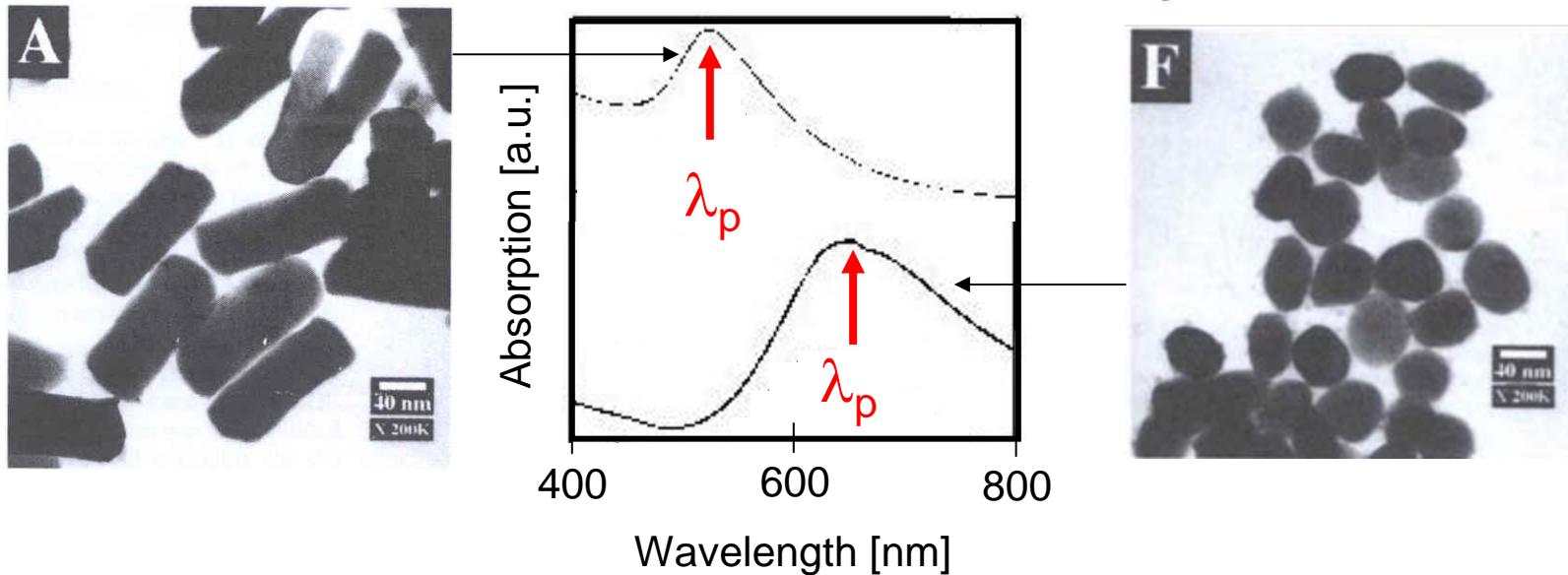
- Gold on glass
- in-situ growth of colloidal crystals
- Polymer nanochannels

**Au on glass!**



# Tempering Au nanoparticles

Optical properties: sharp resonances  $\leftrightarrow$  plasmon resonances  
(visible light) cluster arrangement & shape



J.C. Hulteen et al., J Phys. Chem. B 101, 7727 (1997)

# Annealing

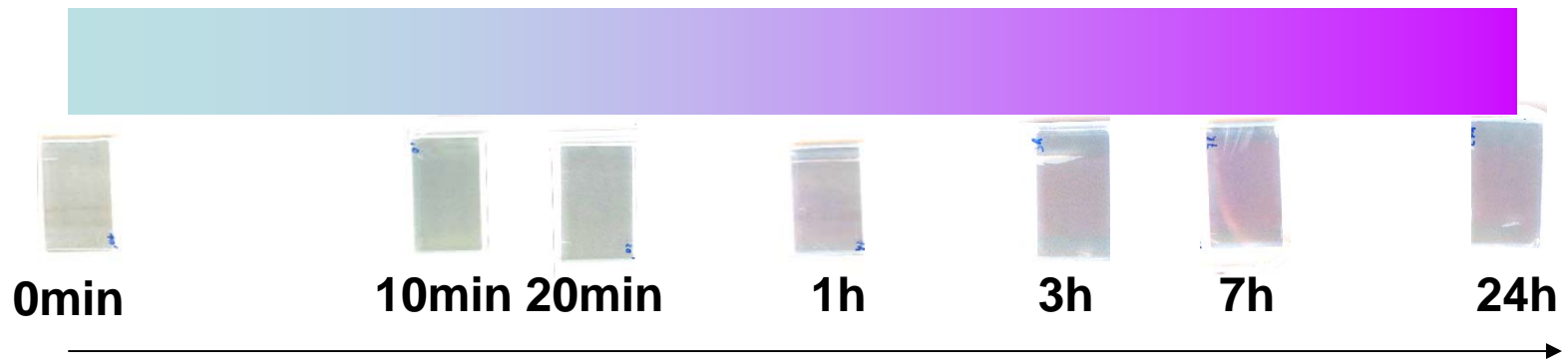
S.V.R., H. Walter (CSEM), R. Domnick (identif) et al., (in preparation)

Au on glass

Parameters: Au layer mass thickness: **3nm , 5nm, 8nm**

**Annealing time**

approaching critical coalescence thickness  
(cluster -> metal character)



0min

10min 20min

1h

3h

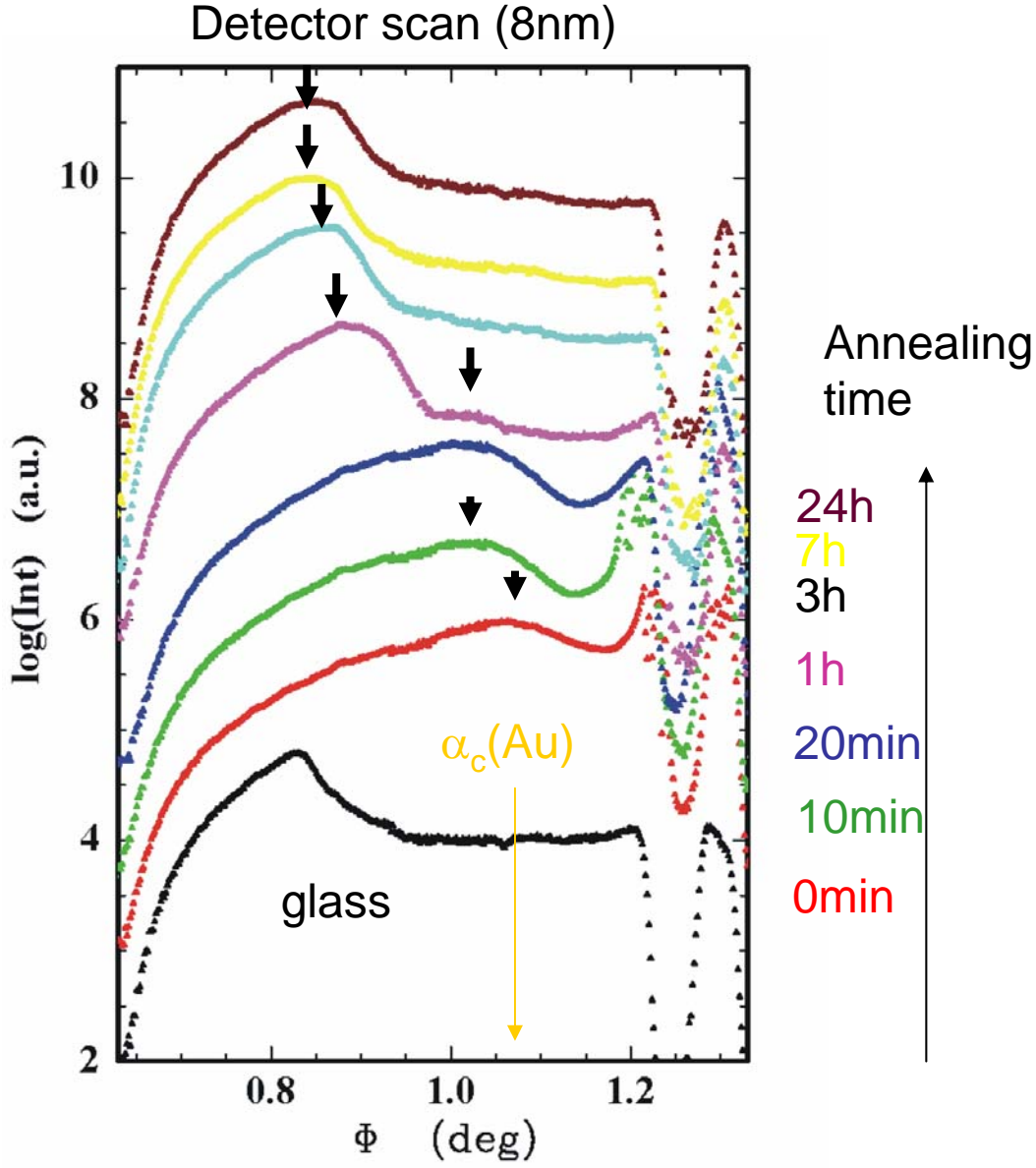
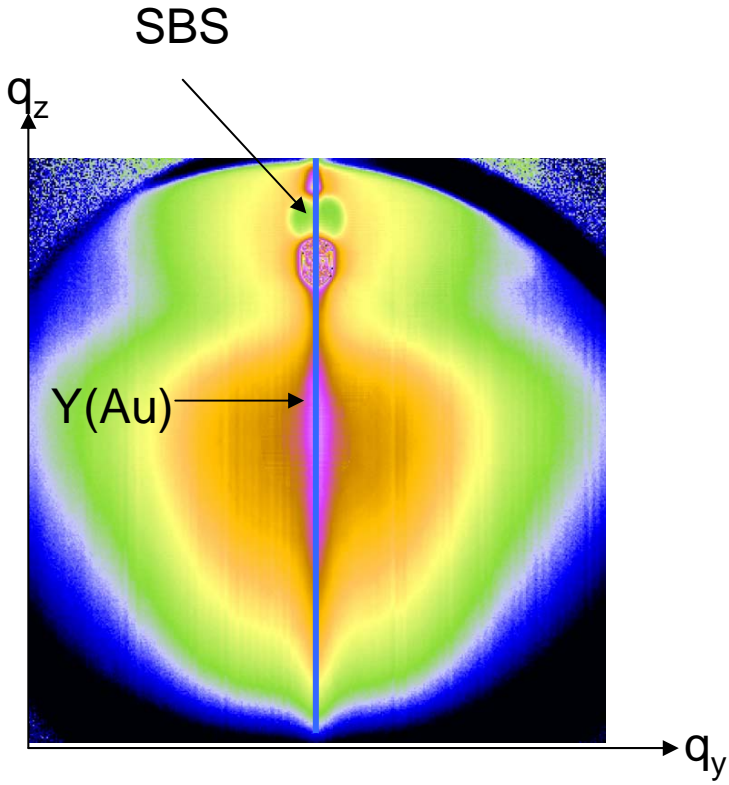
7h

24h

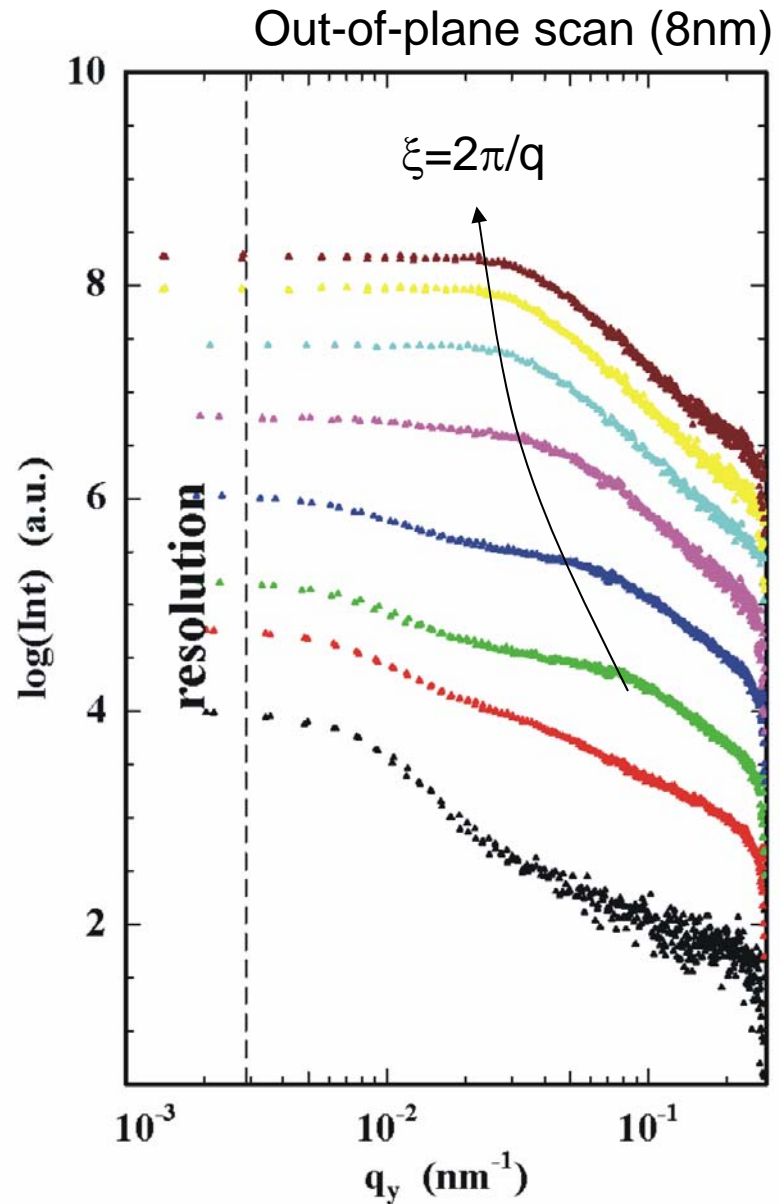
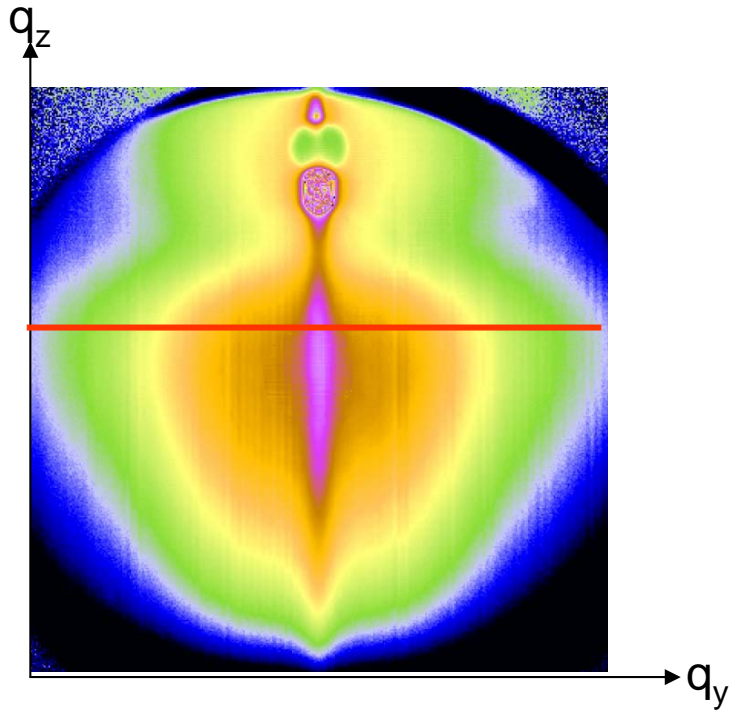
Log (Annealing time)

@  $T_{\text{anneal}} = 300^\circ\text{C} < 1064^\circ\text{C}$  (bulk melting point)

# Surface coverage

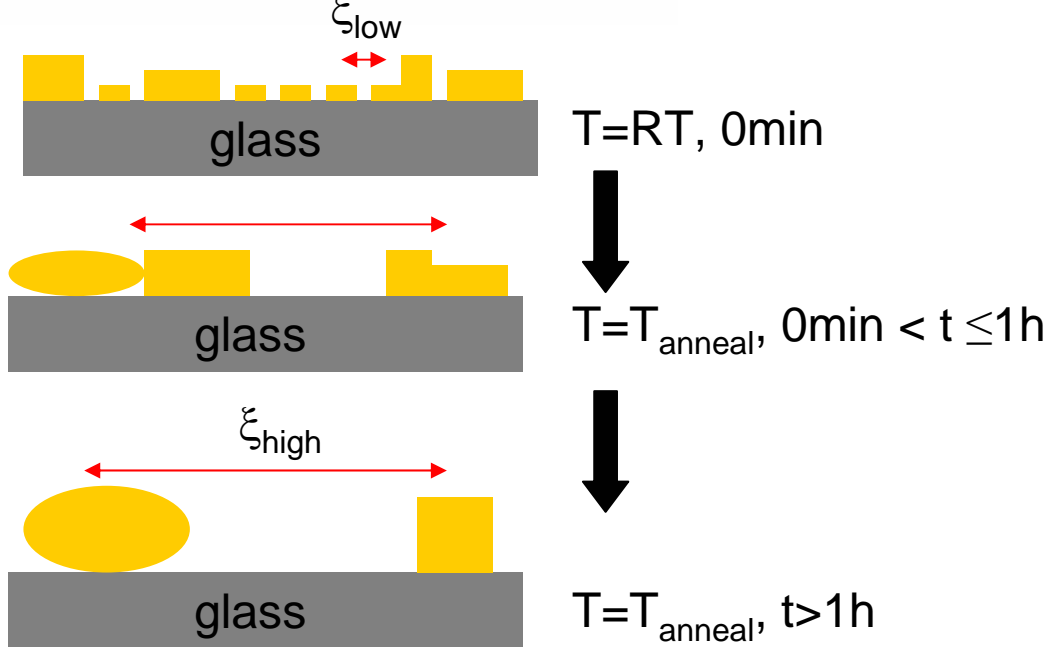
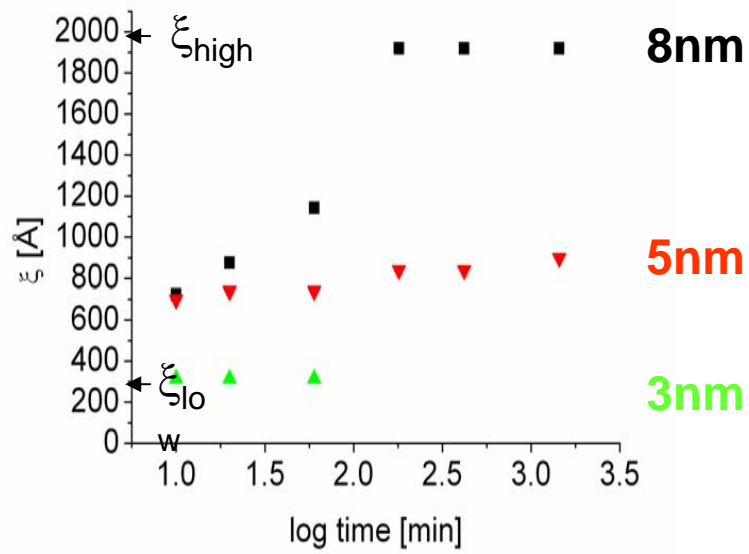
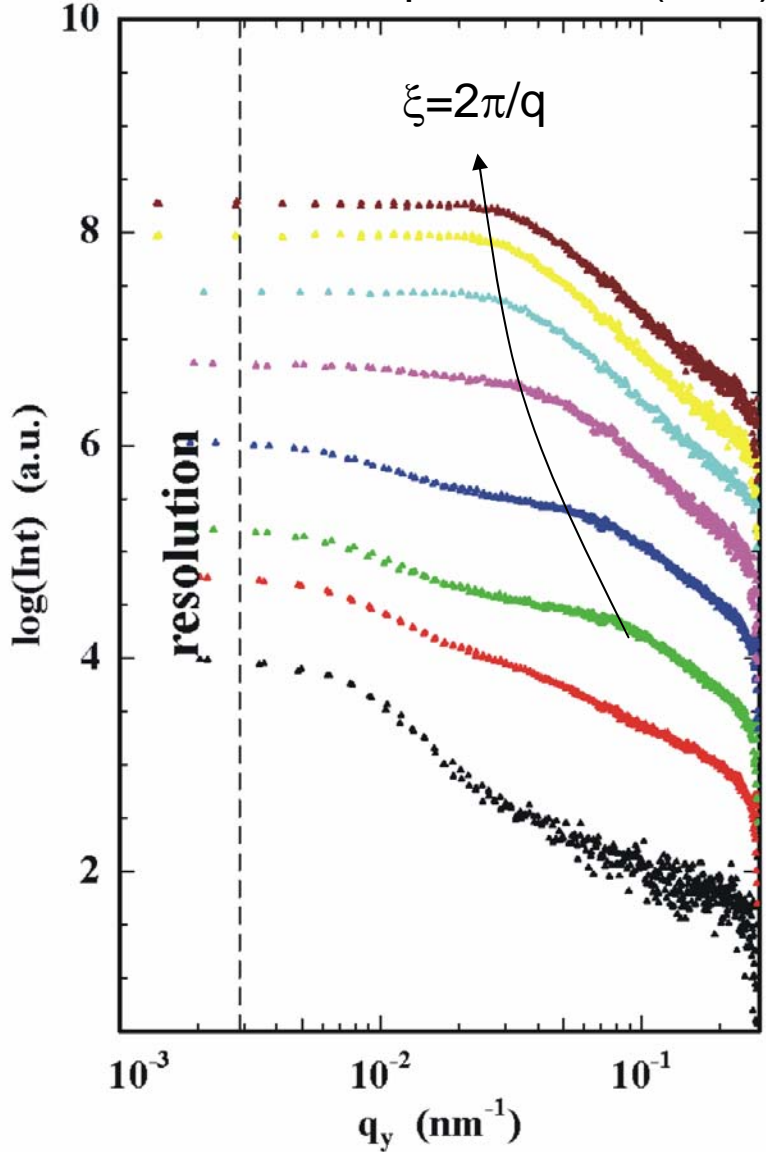


# In-plane ordering



# Lateral length scales

Out-of-plane scan (8nm)



- SAXS versus GISAXS
- GISAXS – theory
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- Application examples:

- Gold on glass



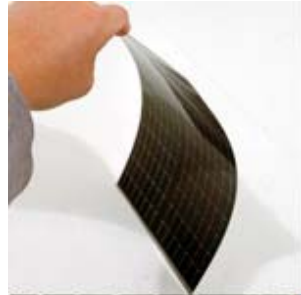
- in-situ growth of colloidal crystals

- Polymer nanochannels

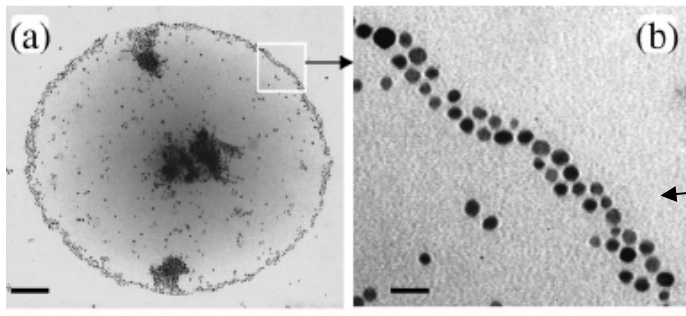
**Au on glass!**

# In-situ nanostructuring from solution

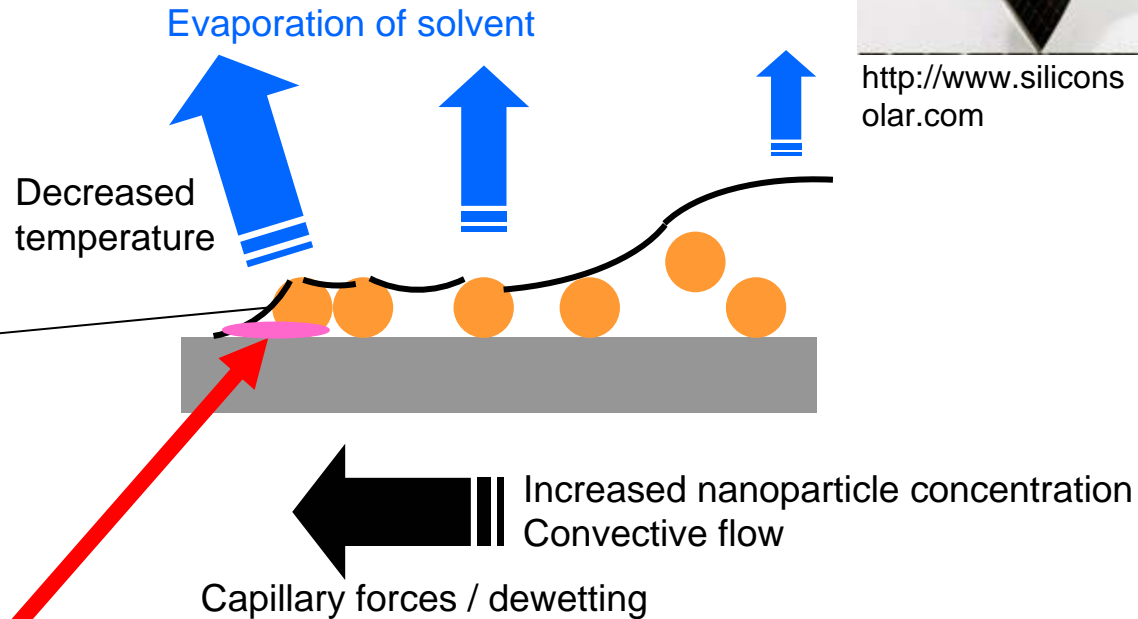
Circuits, solar cells -> printing: electrodes, **cost reduction**



<http://www.siliconsol.com>



Govor et al., PRE **69**, 061609 (2004)



**Control drying-up of colloidal solution layer during inkjet printing**

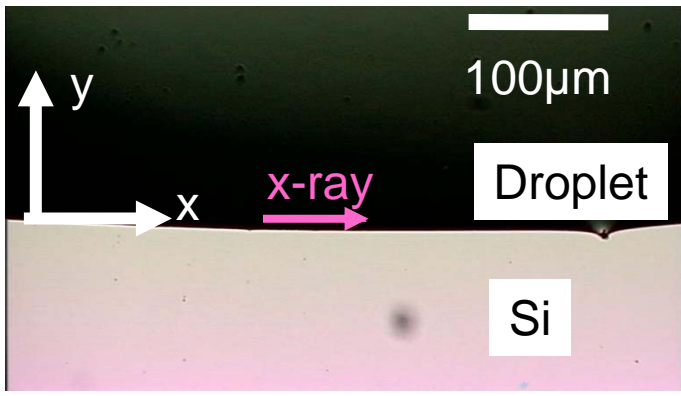
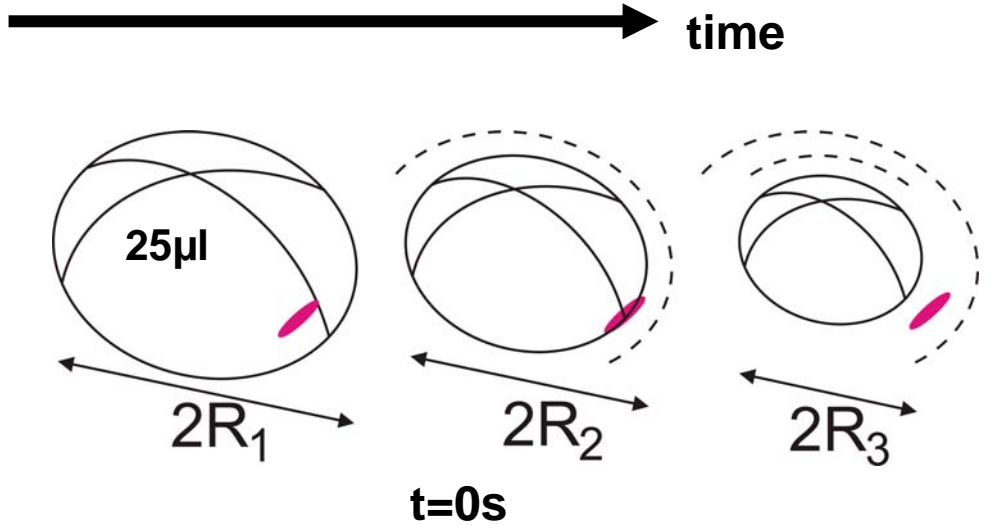
**Critical step: Transfer of order to substrate**

# Real-time results: nanoGISAXS/ ID13 ESRF

2nm Au spheres in water  
Slow evaporation time

300nm beam by Fresnel Zone plates

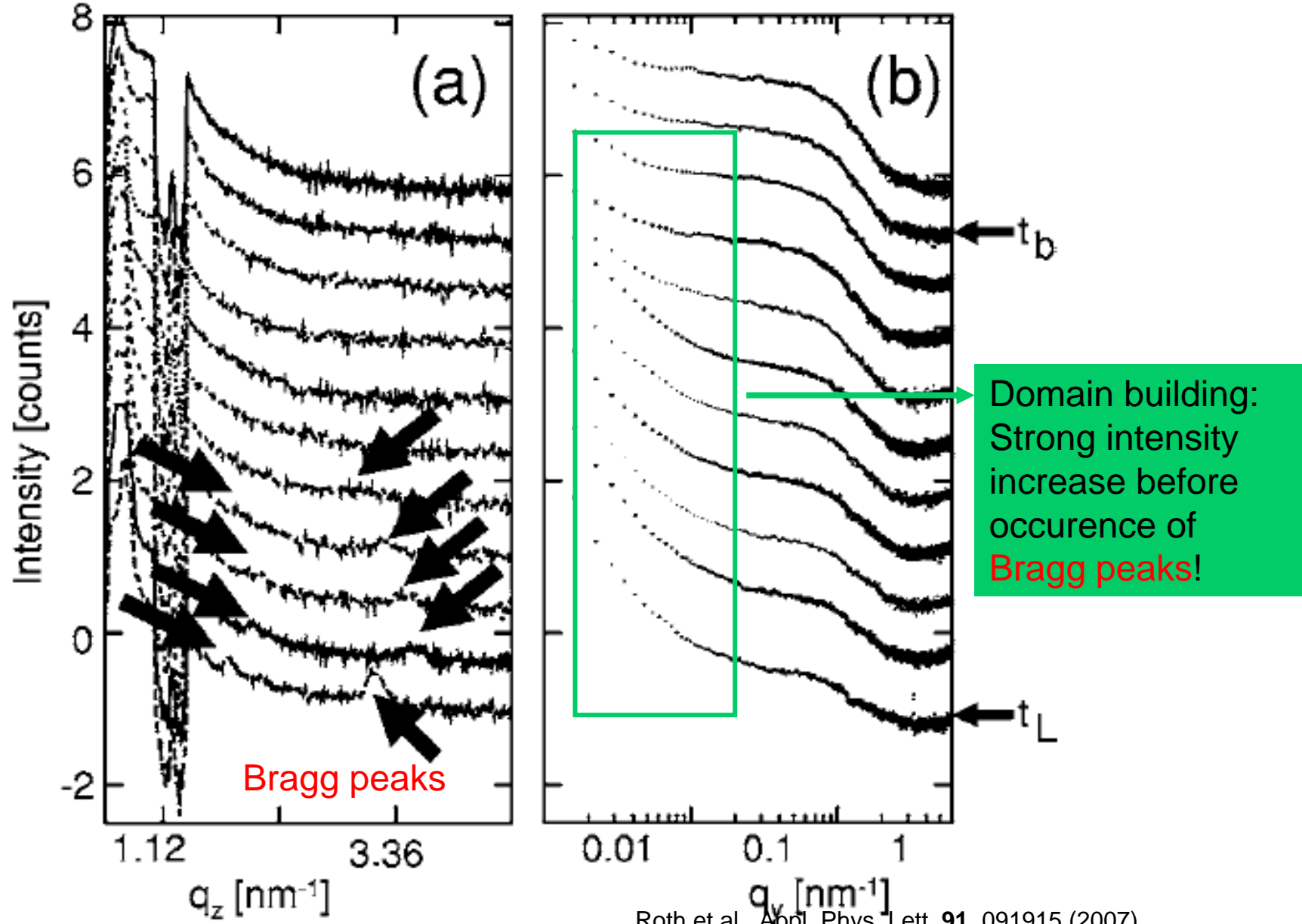
First nanobeam in-situ GISAXS



Roth et al., Appl. Phys. Lett. **91**, 091915 (2007)

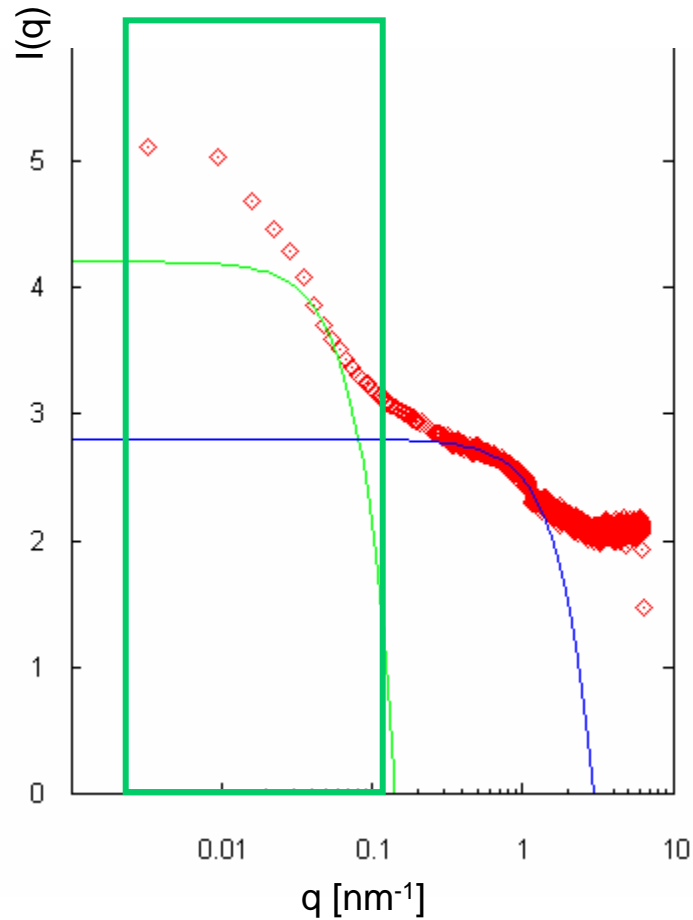


# Real-time results: nanoGISAXS/ ID13 ESRF



Roth et al., Appl. Phys. Lett. **91**, 091915 (2007)

# Guinier Approximation



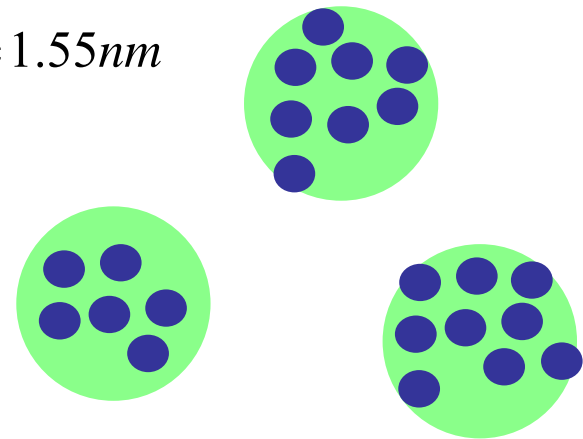
$$\lim_{q \rightarrow 0} I(q) = \Delta\rho^2 \cdot V^2 \cdot \exp\left(-q^2 \cdot \frac{R_g^2}{3}\right)$$

Radius of Gyration  $R_g$

Monodisperse spheres of radius  $R=2\text{nm}$ :

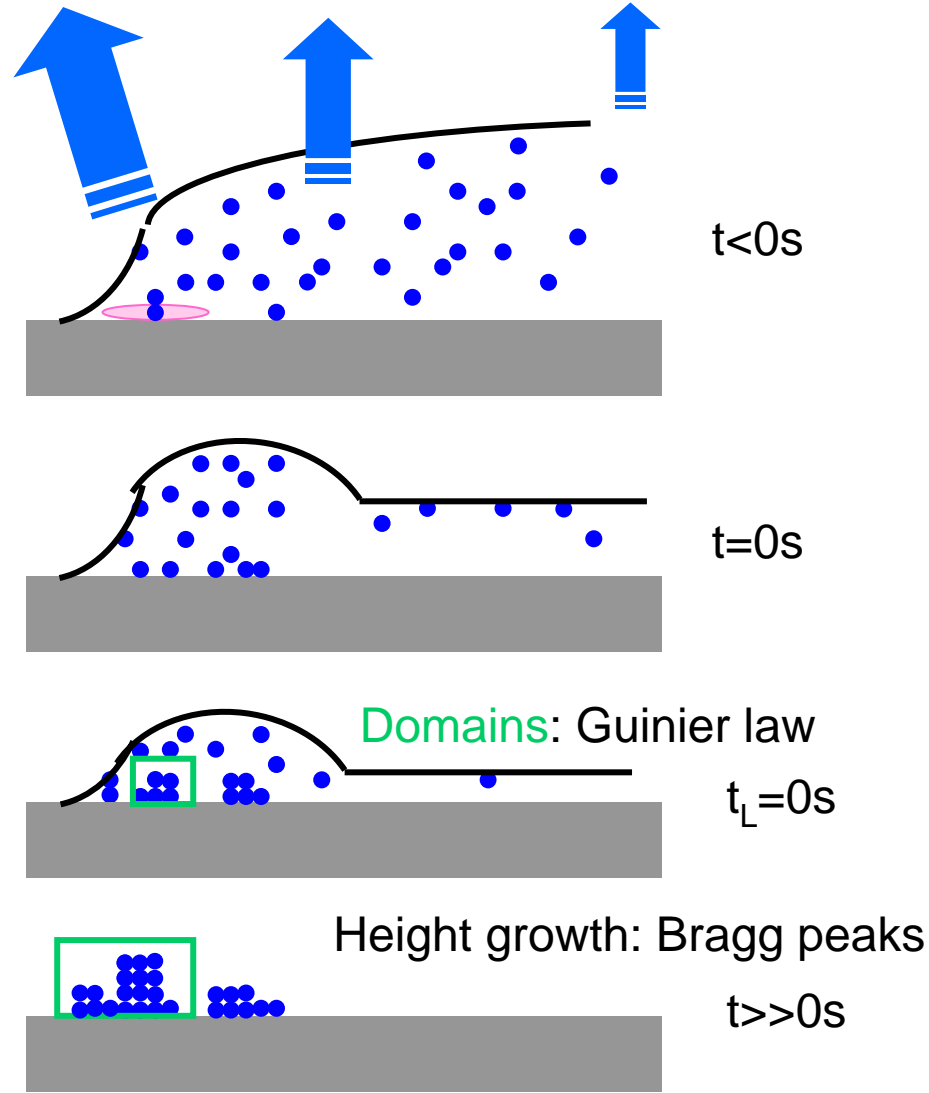
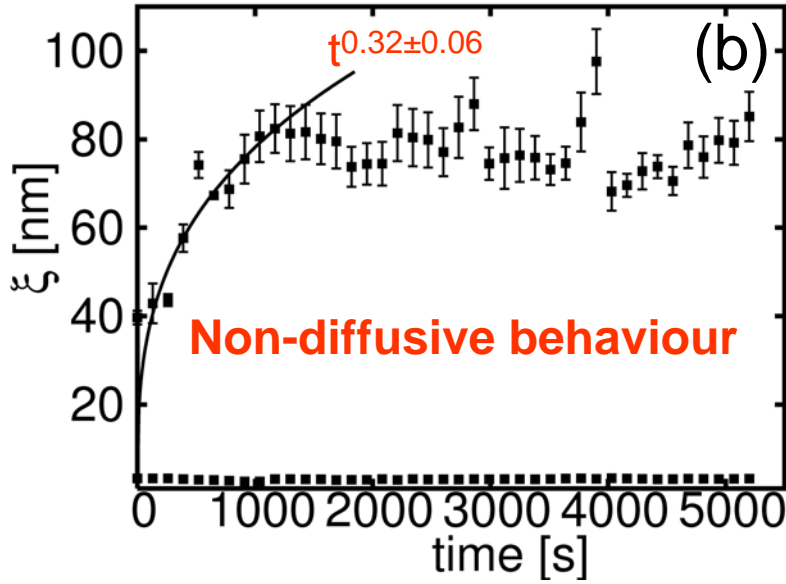
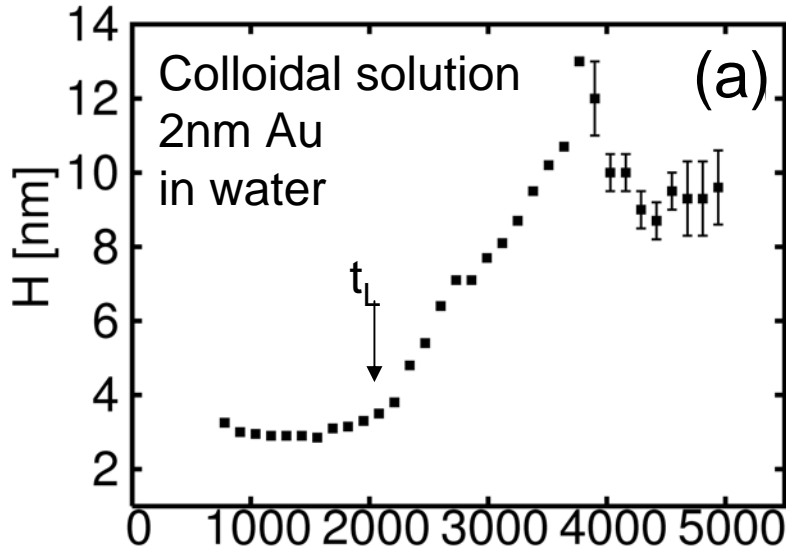
$$R_g = \sqrt{3/5} \cdot R = 1.55\text{nm}$$

**2nm Colloids**  
**domains**



Very useful to get a hand on length scales!  
Sometimes only valid in limited  $q$ -range

# Real-time results: nanoGISAXS/ ID13 ESRF



Roth et al., Appl. Phys. Lett. **91**, 091915 (2007)

- SAXS versus GISAXS
- GISAXS – theory
- Instrumentation
- Application examples:
  - Gold on glass
  - in-situ growth of colloidal crystals
  - Polymer nanochannels

**Au on glass!**

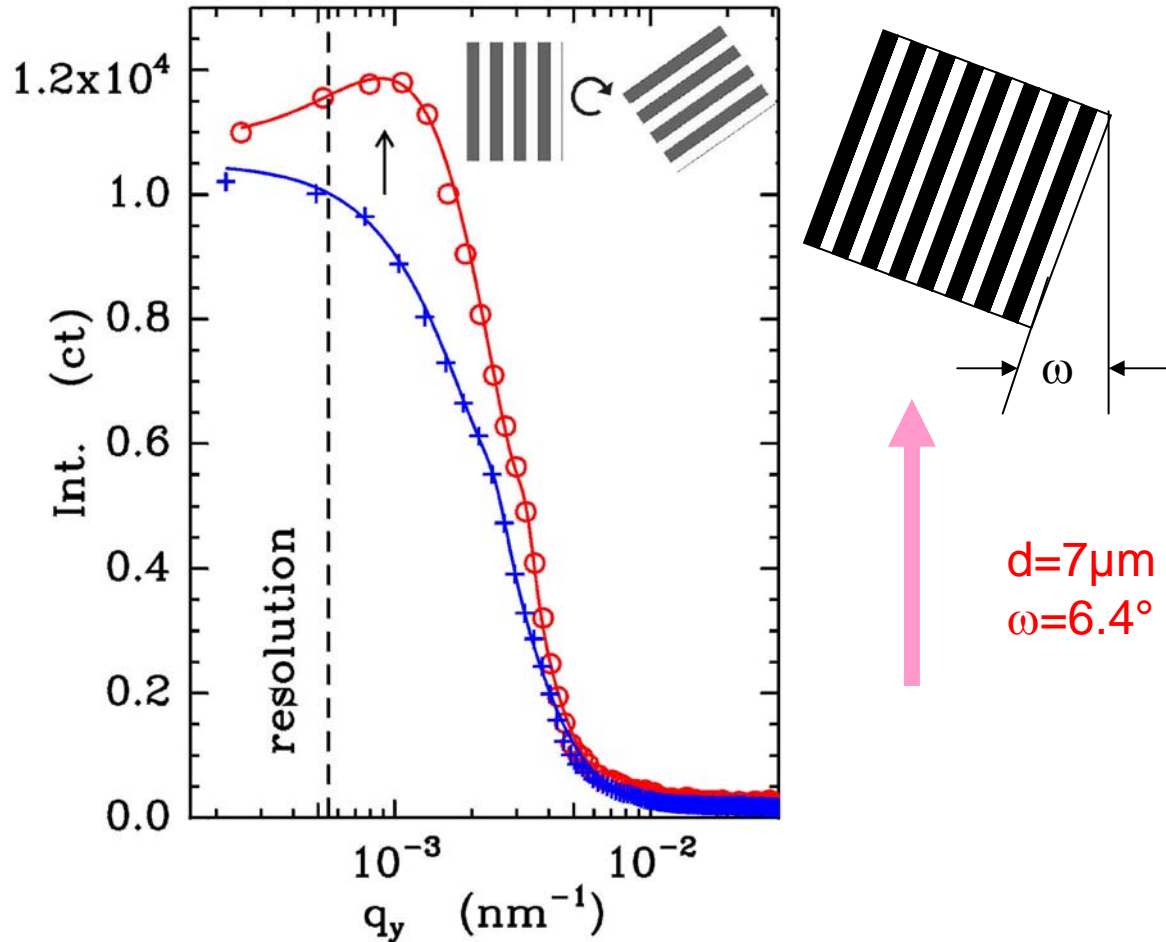
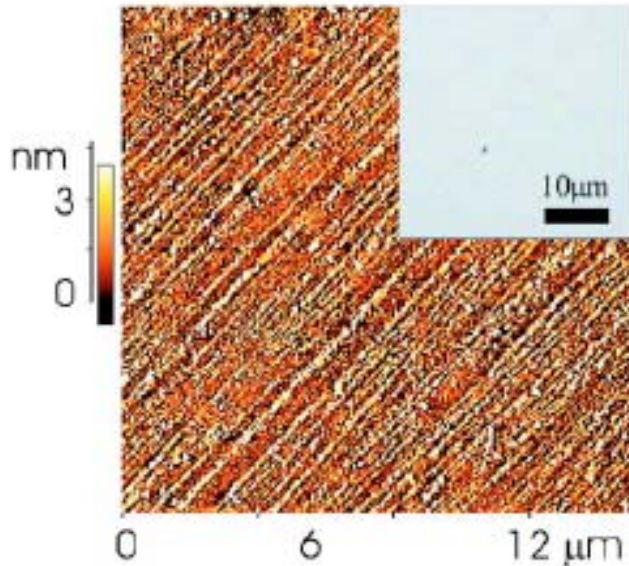


# Route to create large-area ordered polymeric nanochannel arrays

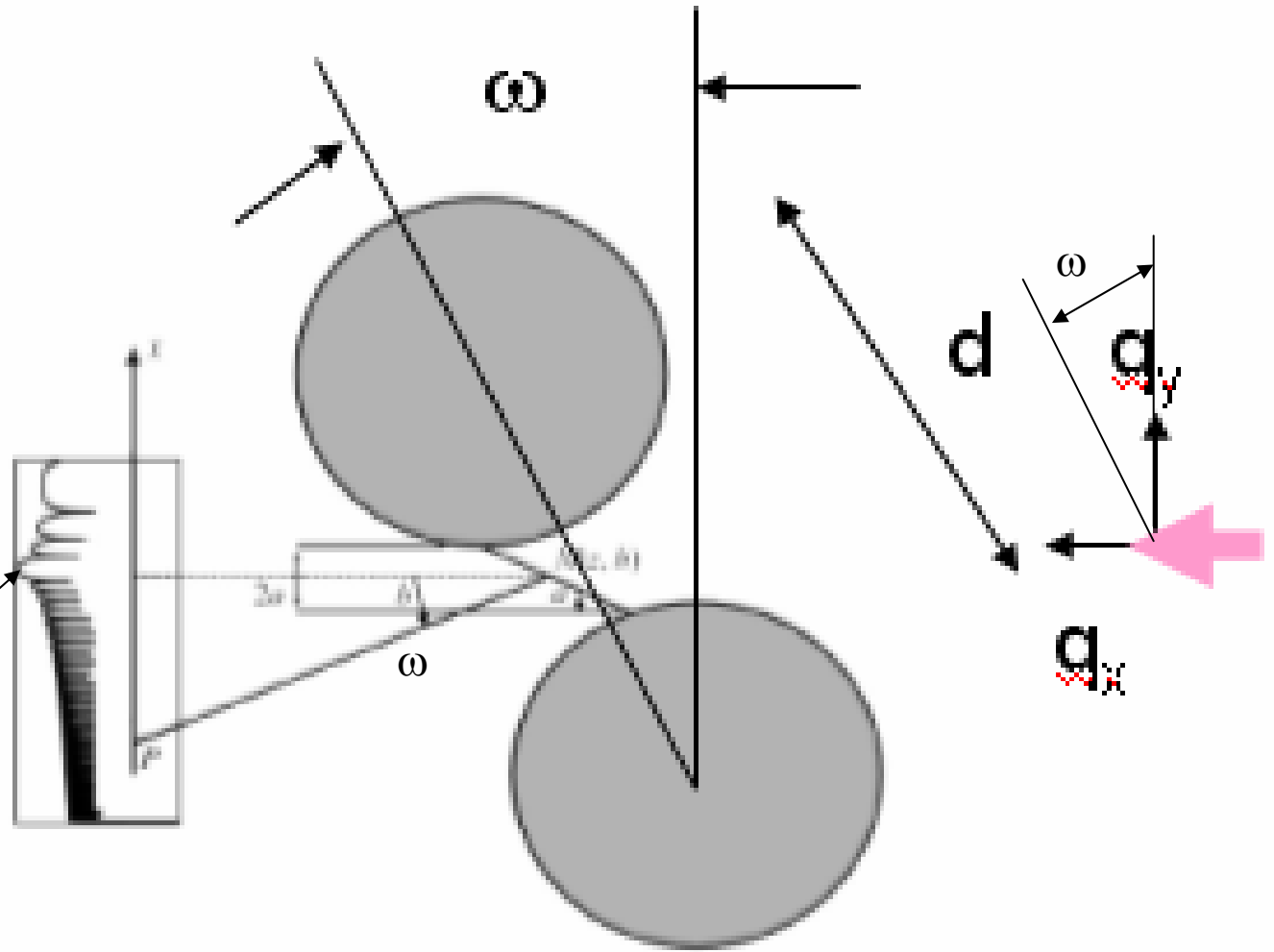
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BW4, GIUSAXS 13m,  $\alpha_i=0^\circ$   
 Polymeric nanochannels



GIUSAXS @  $\alpha_i=0^\circ$



Zero order

$$q_y \cos\omega + q_x \sin\omega = 0$$

In direction of d

$$q_x = 2\pi/\lambda (\cos(\alpha_f) - \cos(\alpha_i))$$

$$q_y + 2\pi/\lambda \cdot 1/2 \alpha_f^2 / \omega = 0$$

Calculate tilt angle  $\omega$

# The End